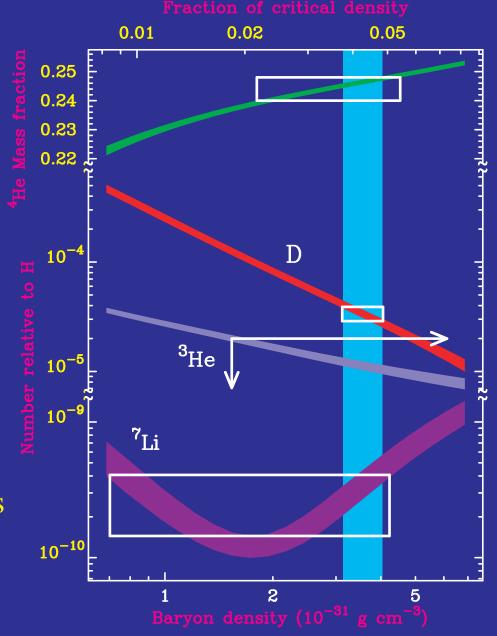
Predicting the CMB: Nucleosynthesis

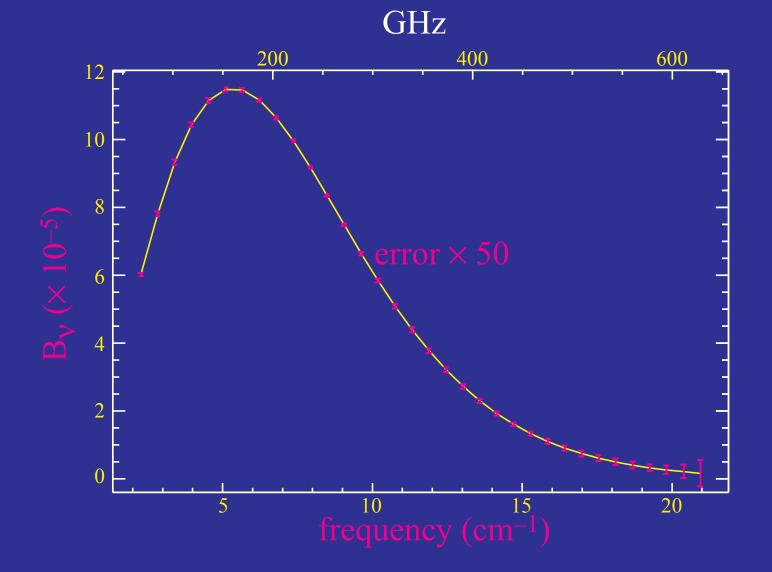
- Light element abundance depends on baryon/photon ratio
- Existence and temperature of CMB originally predicted (Gamow 1948) by light elements + visible baryons
- With the CMB photon number density fixed by the temperature light elements imply dark baryons
- Peaks say that photon-baryon ratio at MeV and eV scales are same



Burles, Nollett, Turner (1999)

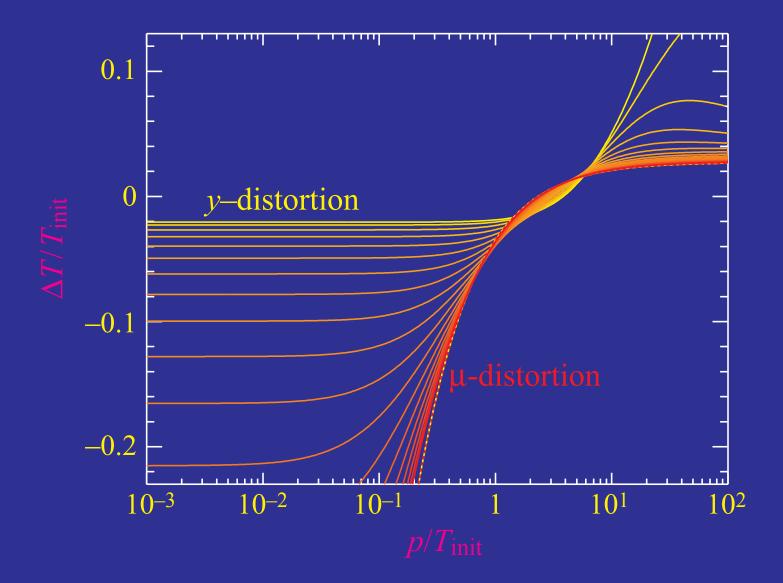
Spectrum

- FIRAS Spectrum
- Perfect Blackbody $\mu=0$ (t=1yr equilibrium)



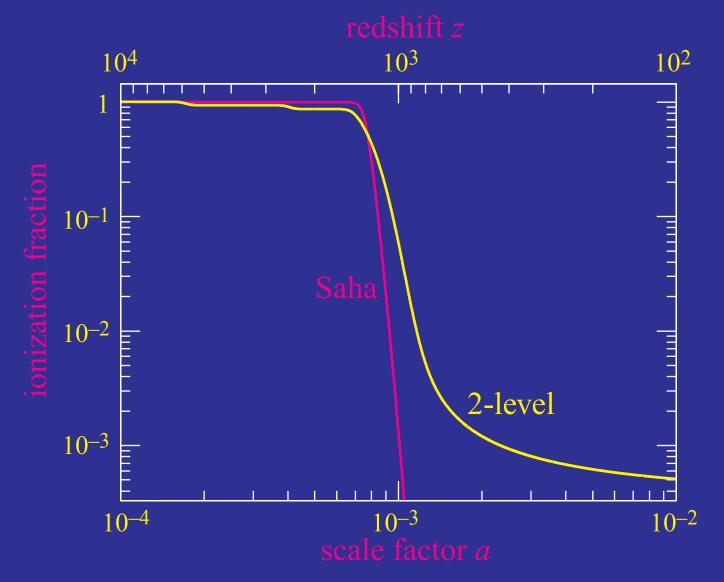
Comptonization

- Compton upscattering: *y*-distortion seen in Galaxy clusters
- Redistribution: µ-distortion

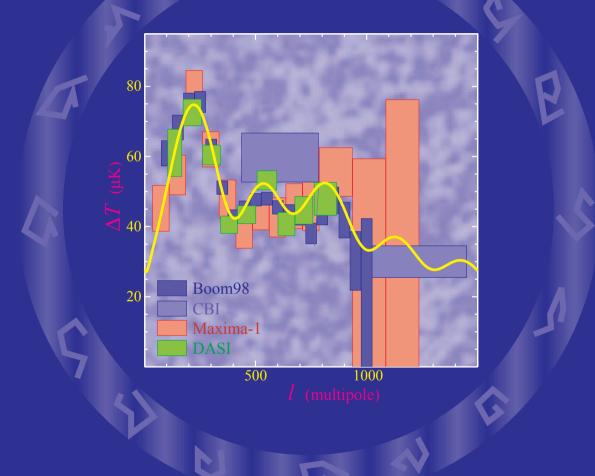


Recombination

- Hung up by Ly α opacity (2 γ forbidden transition + redshifting)
- Frozen out with a finite residual ionization fraction

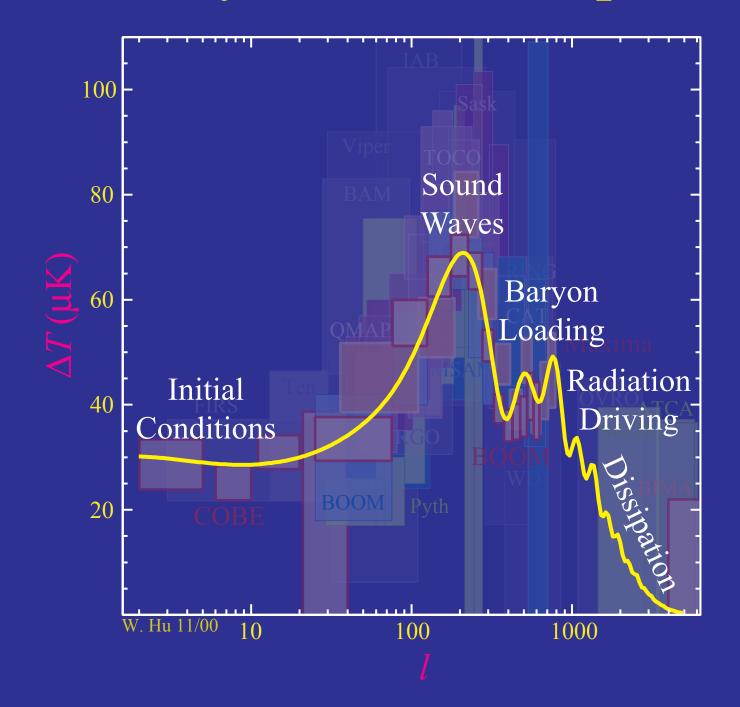


CMB Anisotropies: The Acoustic Peaks



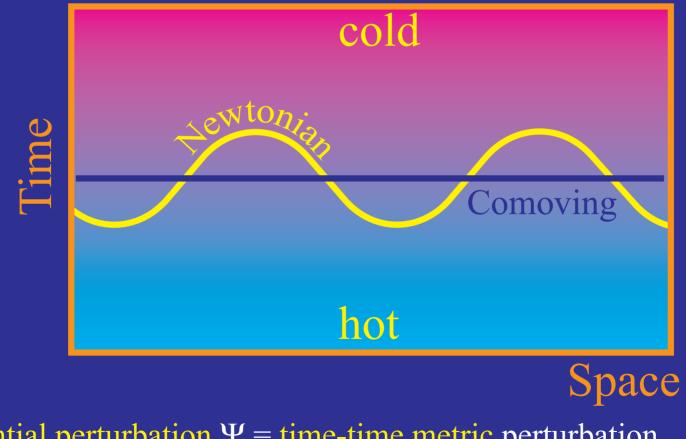
Astro 282, Spring 2006 *Wavne Hu*

Physical Landscape



Inflation and the Initial Conditions

- Inflation: (nearly) scale-invariant curvature (potential) perturbations
- Superluminal expansion \rightarrow superhorizon scales \rightarrow "initial conditions"
- Accompanying temperture perturbations due to cosmological redshift



• Potential perturbation Ψ = time-time metric perturbation $\delta t/t = \Psi \rightarrow \delta T/T = -\delta a/a = -2/3 \delta t/t = -2/3 \Psi$

Sachs & Wolfe (1967); White & Hu (1997)

Gravitational Ringing

- Potential wells = inflationary seeds of structure
- Fluid falls into wells, pressure resists: acoustic oscillations

Plane Waves

- Potential wells: part of a fluctuation spectrum
- Plane wave decomposition

Harmonic Modes

- Frequency proportional to wavenumber: $\omega = kc_s$
- Twice the wavenumber = twice the frequency of oscillation

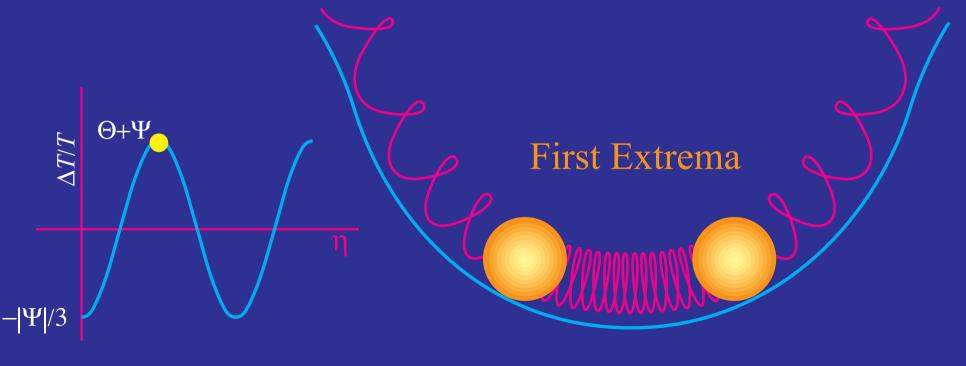


- Oscillations frozen at recombination
- Compression=hot spots, Rarefaction=cold spots

Acoustic Oscillations

- Photon pressure resists compression in potential wells
- Acoustic oscillations
- Gravity displaces zero point $\Theta \equiv \delta T/T = -\Psi$

- Oscillation amplitude = initial displacement from zero pt.
 Θ-(-Ψ)=1/3Ψ
- Gravitational redshift: observed $(\delta T/T)_{obs} = \Theta + \Psi$ oscillates around zero



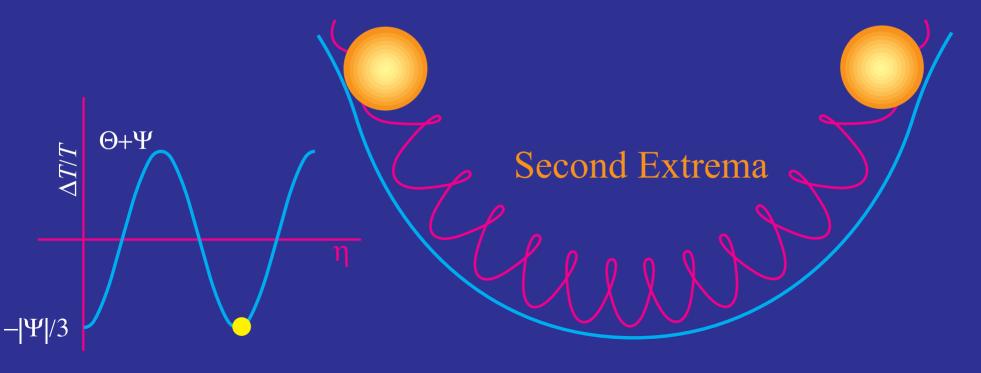
Peebles & Yu (1970)

Hu & Sugyama (1995); Hu, Sugiyama & Silk (1997)

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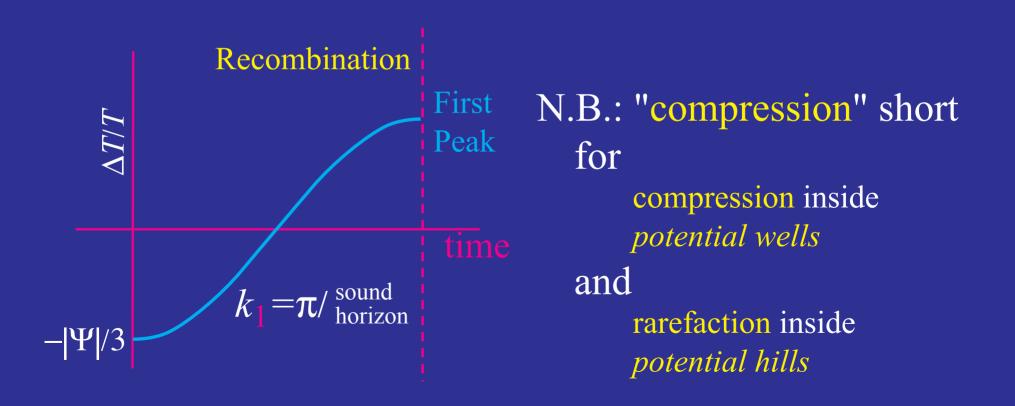


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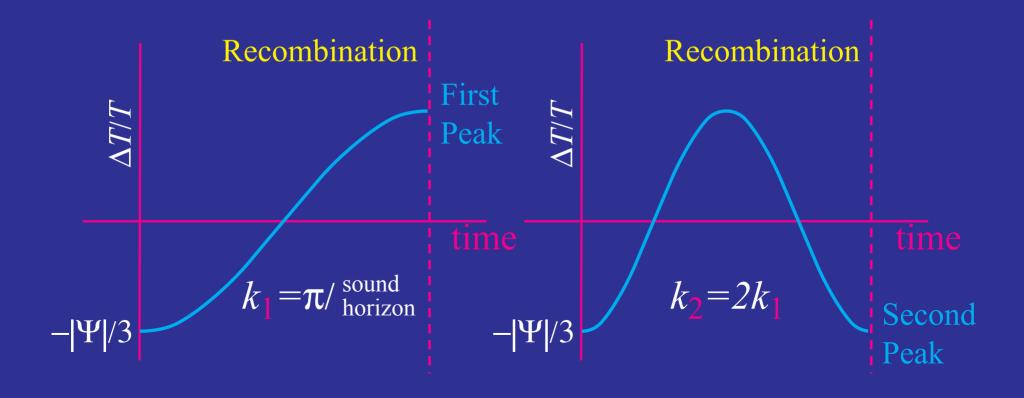
Extrema=Peaks

• First peak = mode that just compresses



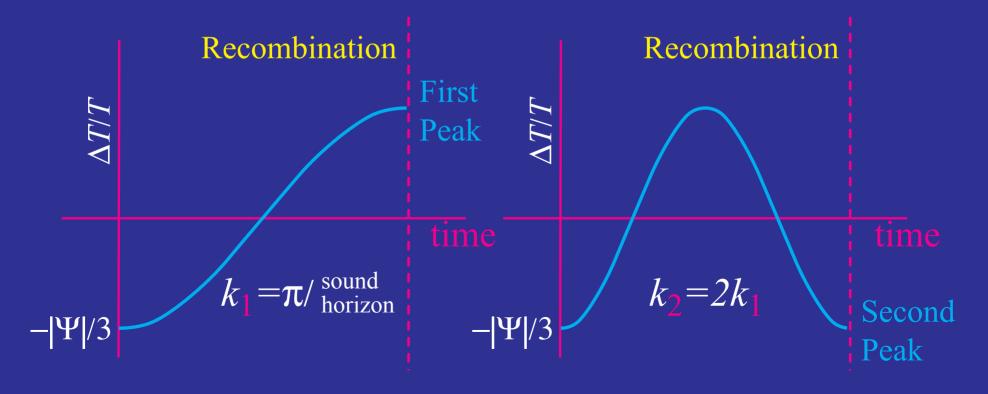
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- Second peak = mode that compresses then rarefies: twice the wavenumber



Extrema=Peaks

- First peak = mode that just compresses
- Second peak = mode that compresses then rarefies: twice the wavenumber
- Harmonic peaks: 1:2:3 in wavenumber



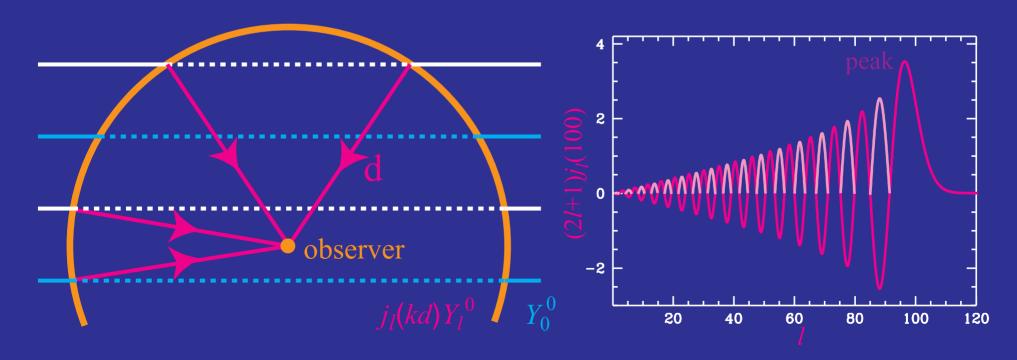
Angular Peaks

Peaks in Angular Power
The Anisotropy Formation Process

Projection into Angular Peaks

- Peaks in spatial power spectrum
- Projection on sphere
- Spherical harmonic decomposition

- Maximum power at *l=kd*
- Extended tail to $l \ll kd$
- Described by spherical bessel function j_l(kd)



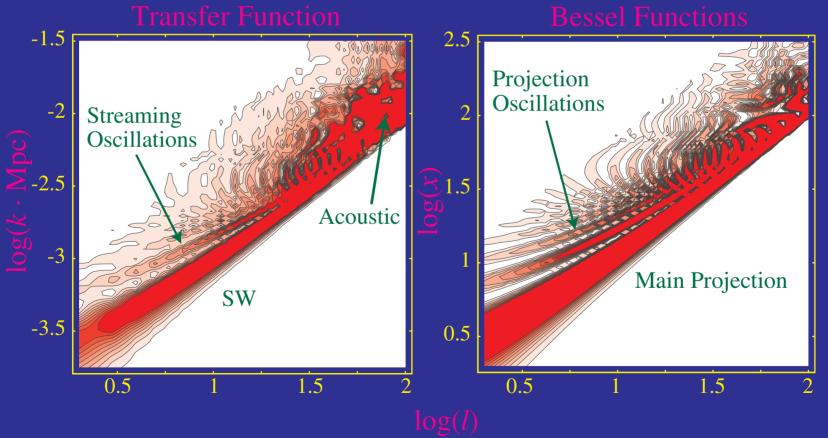
Bond & Efstathiou (1987)

Hu & Sugiyama (1995); Hu & White (1997)

Projection into Angular Peaks

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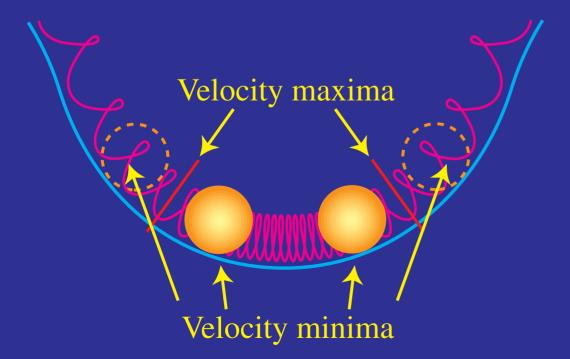
- Maximum power at l = kd
- Extended tail to $l \ll kd$
- 2D Transfer Function $T^2(k,l) \sim (2l+1)^2 [\Delta T/T]^2 j_l^2(kd)$



Hu & Sugiyama (1995)

Doppler Effect

- Relative velocity of fluid and observer
- Extrema of oscillations are turning points or velocity zero points
- Velocity $\pi/2$ out of phase with temperature



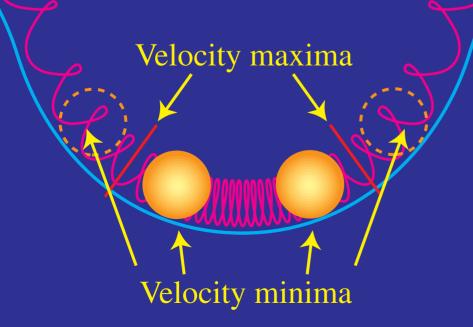
Doppler Effect

No baryons

 $-|\Psi|/3$

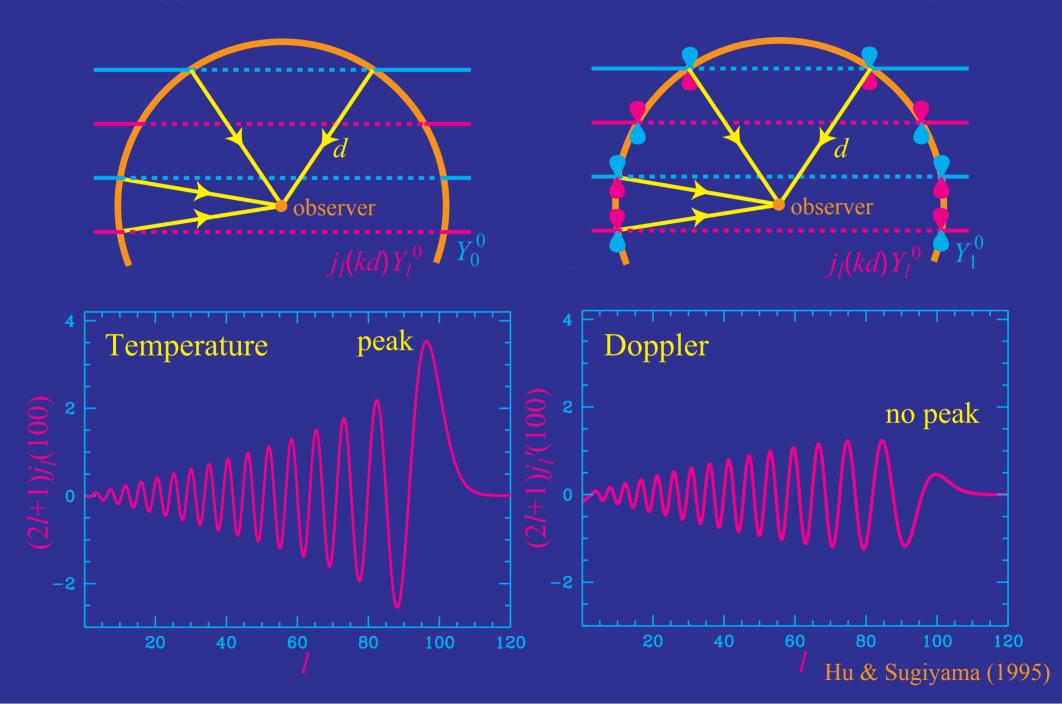
Baryons

- Relative velocity of fluid and observer
- Extrema of oscillations are turning points or velocity zero points
- Velocity $\pi/2$ out of phase with temperature
- Zero point not shifted by baryon drag
- Increased baryon inertia decreases effect $m_{\rm eff} V^2 = {\rm const.} \quad V \propto \ m_{\rm eff}^{-1/2} = (1+R)^{-1/2}$

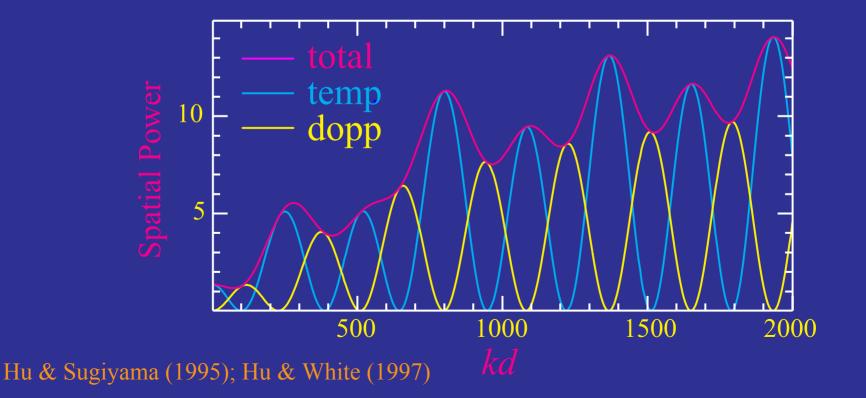


Doppler Peaks?

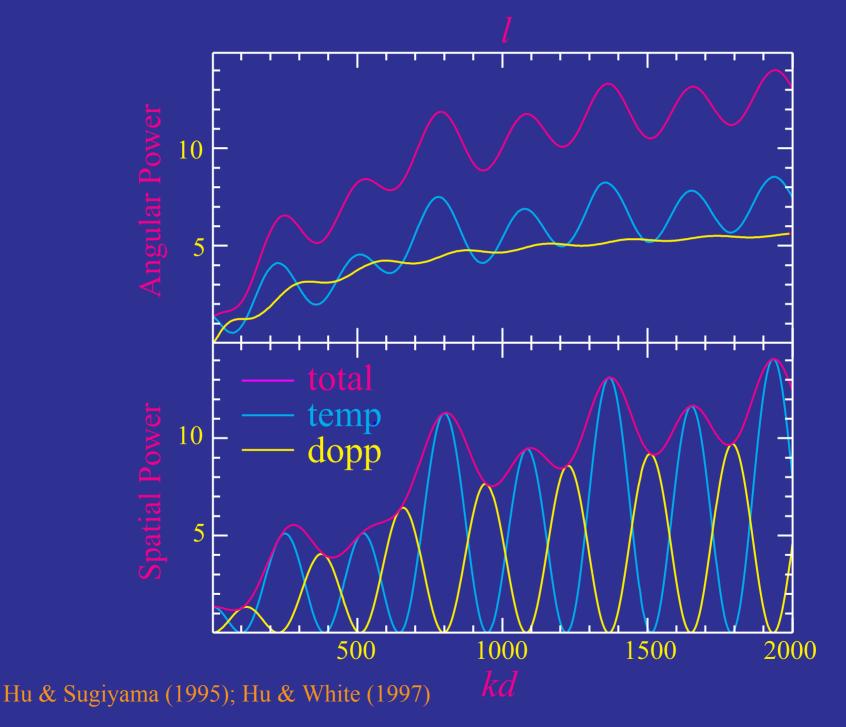
• Doppler effect has lower amplitude and weak features from projection



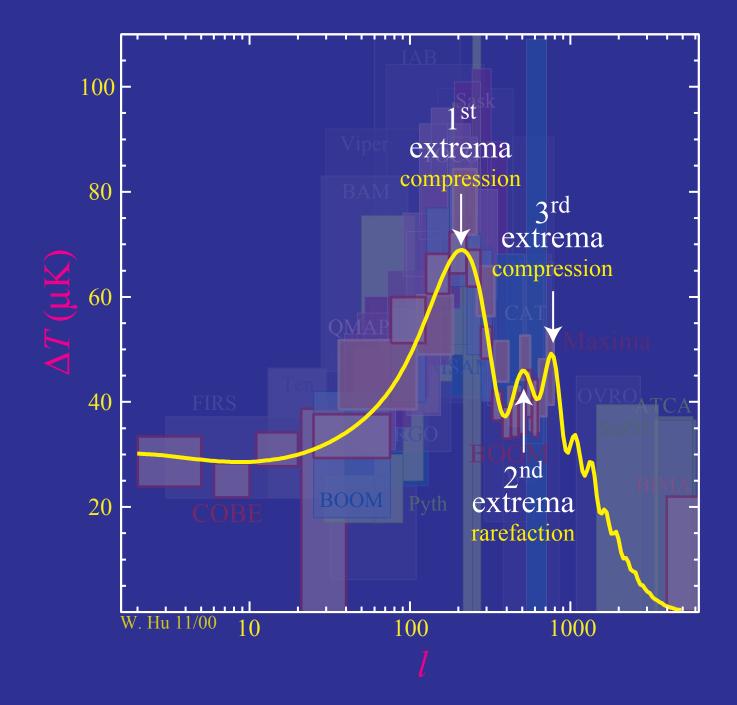
Relative Contributions



Relative Contributions



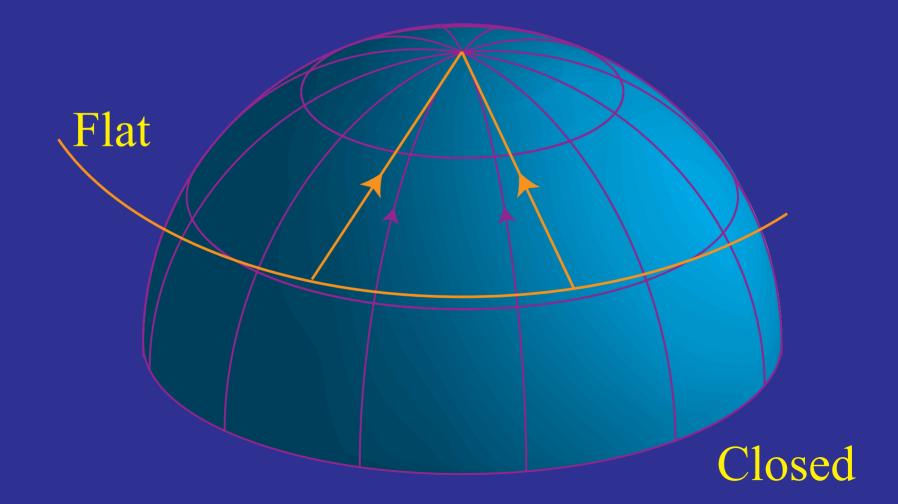
Acoustic Landscape



The First Peak

Spatial Curvature

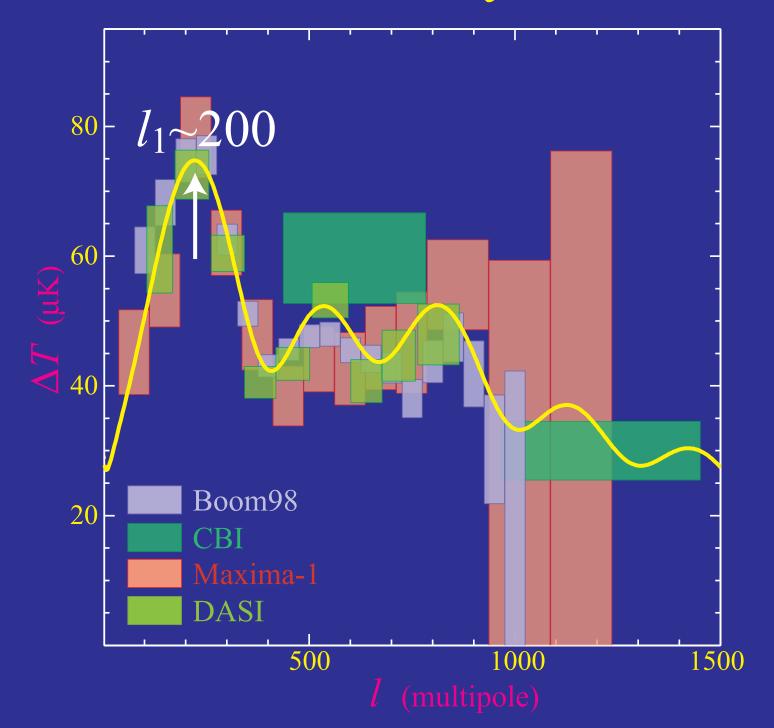
- Physical scale of peak = distance sound travels
- Angular scale measured: comoving angular diameter distance test for curvature



Curvature in the Power Spectrum

- Features scale with angular diameter distance
- Angular location of the first peak

First Peak Precisely Measured



Standard Rulers
Calibrating the Standard Rulers

Sound Horizon

Damping Scale

0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18,

Matter/Radiation —

The Second Peak

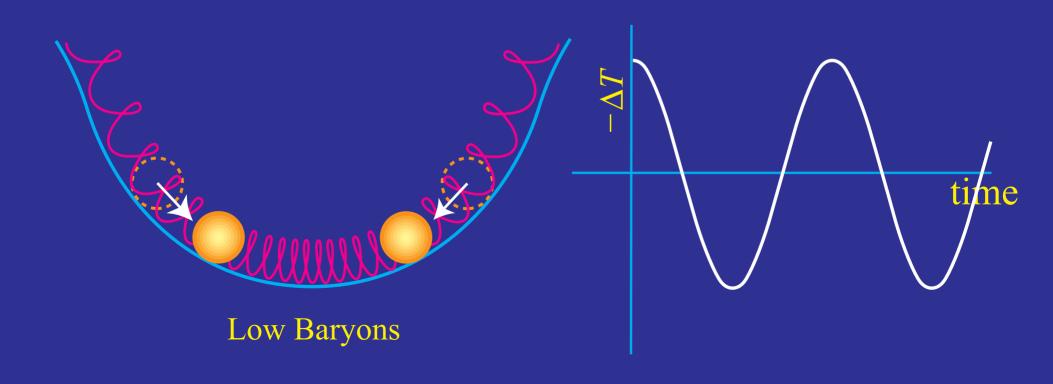
Baryon & Inertia

- Baryons add inertia to the fluid
- Equivalent to adding mass on a spring
- Same initial conditions
- Same null in fluctuations

• Unequal amplitudes of extrema

A Baryon-meter

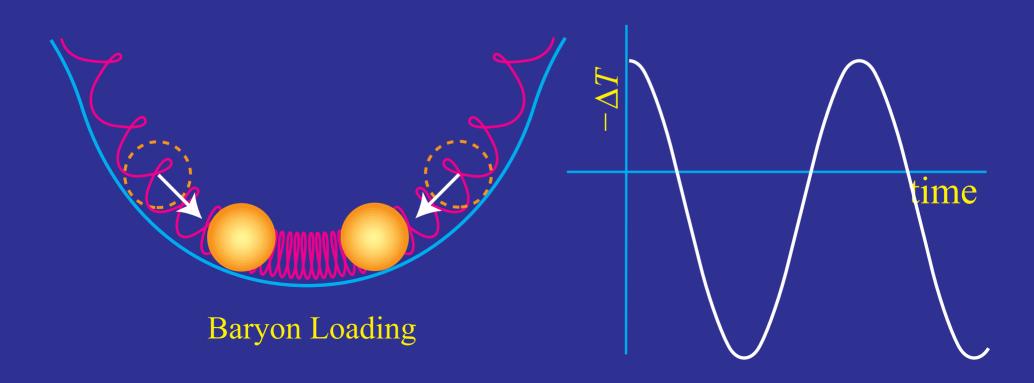
• Low baryons: symmetric compressions and rarefactions



A Baryon-meter

• Load the fluid adding to gravitational force

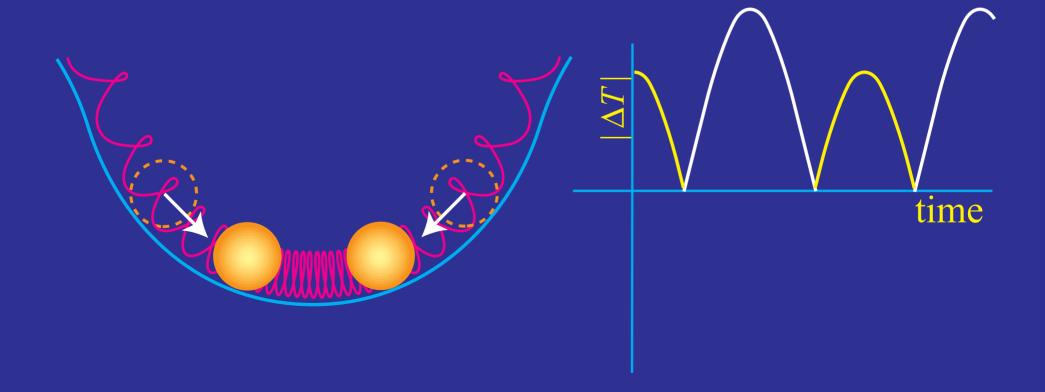
 Enhance compressional peaks (odd) over rarefaction peaks (even)



A Baryon-meter

 Enhance compressional peaks (odd) over rarefaction peaks (even)

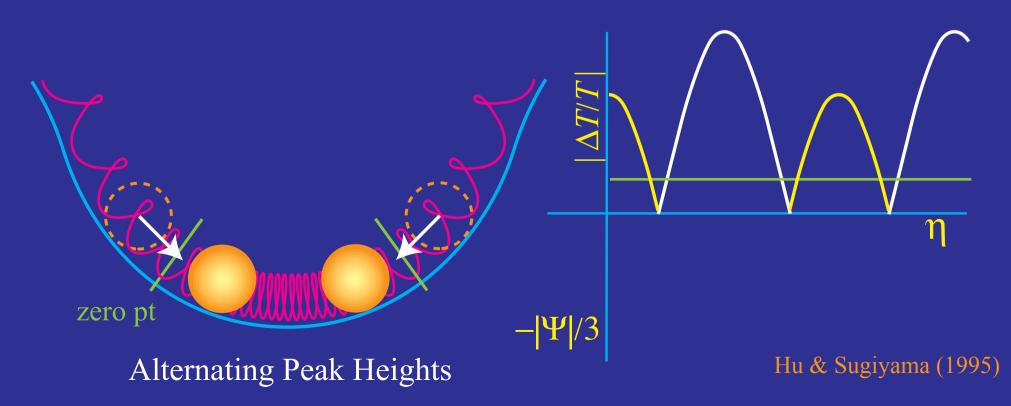
e.g. relative suppression of second peak



Baryon Loading

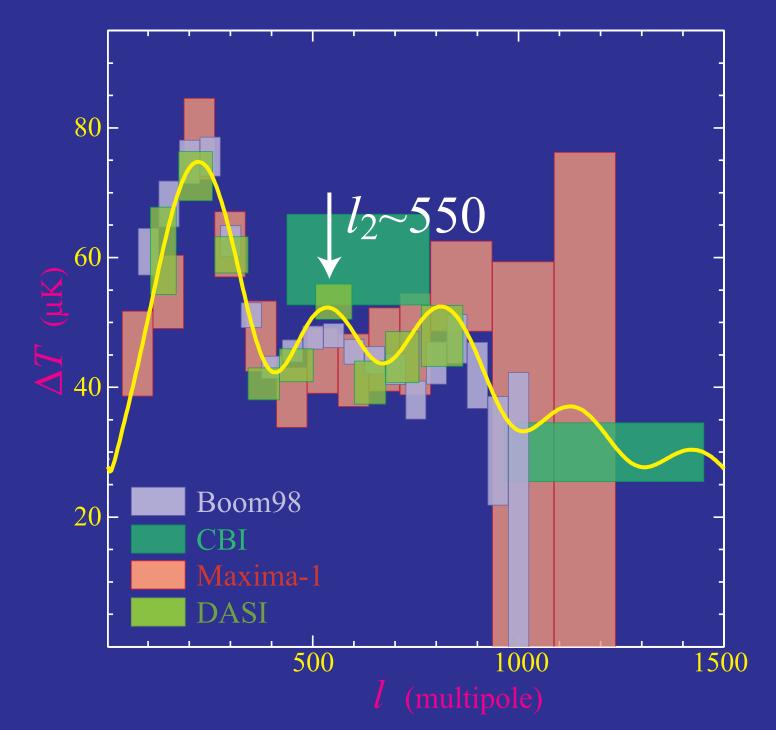
- Baryons provide inertia
- Relative momentum density $R = (\rho_{b} + p_{b})V_{b} / (\rho_{\gamma} + p_{\gamma})V_{\gamma} \propto \Omega_{b}h^{2}$
- Effective mass $m_{\text{eff}} = (1+R)$

- Baryons drag photons into potential wells → zero point ↑
- Amplitude ↑
- Frequency $\downarrow (\omega \propto m_{\rm eff}^{-1/2})$
- Constant *R*, Ψ : $(1+R)\ddot{\Theta} + (k^2/3)\Theta = -(1+R)(k^2/3)\Psi$ $\Theta + \Psi = [\Theta(0) + (1+R)\Psi(0)] \cos [k\eta/\sqrt{3}(1+R)] - R\Psi$

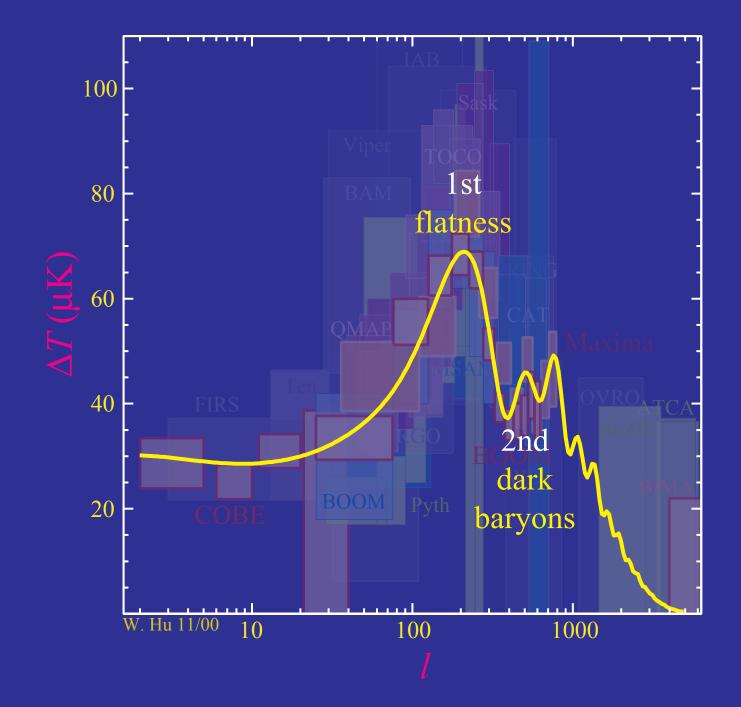


Baryons in the Power Spectrum

Second Peak Detected



Score Card





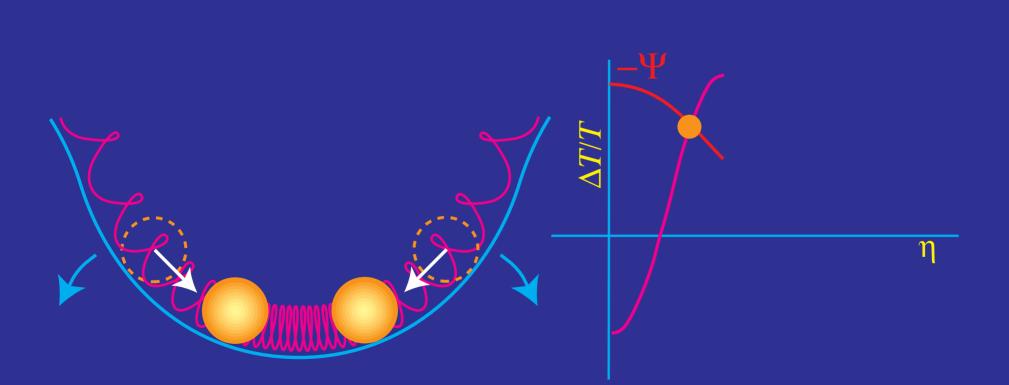
Radiation and Dark Matter

- Radiation domination: potential wells created by CMB itself
- Pressure support \Rightarrow potential decay \Rightarrow driving
- Heights measures when dark matter dominates

Driving Effects and Matter/Radiation

- Potential perturbation:
- Radiation \rightarrow Potential:

 $k^2 \Psi = -4\pi G a^2 \delta \rho$ generated by radiation inside sound horizon $\delta \rho / \rho$ pressure supported $\delta \rho$ hence Ψ decays with expansion

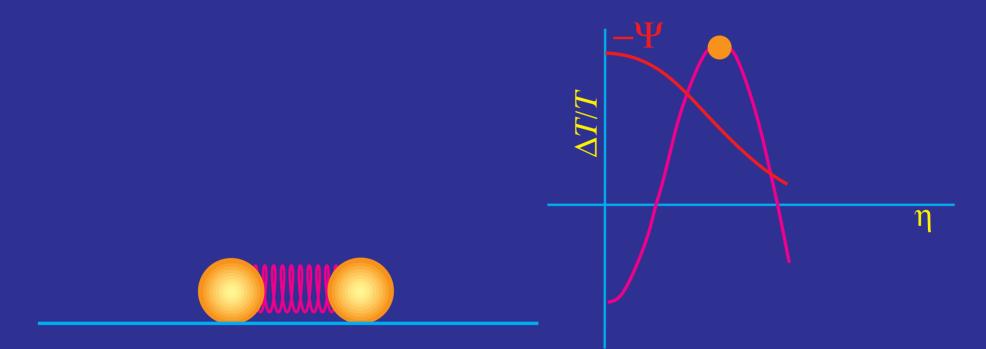


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- $-2\Psi + (1/3)\Psi = -(5/3)\Psi \rightarrow 5x \text{ boost}$
- Feedback stops at matter domination



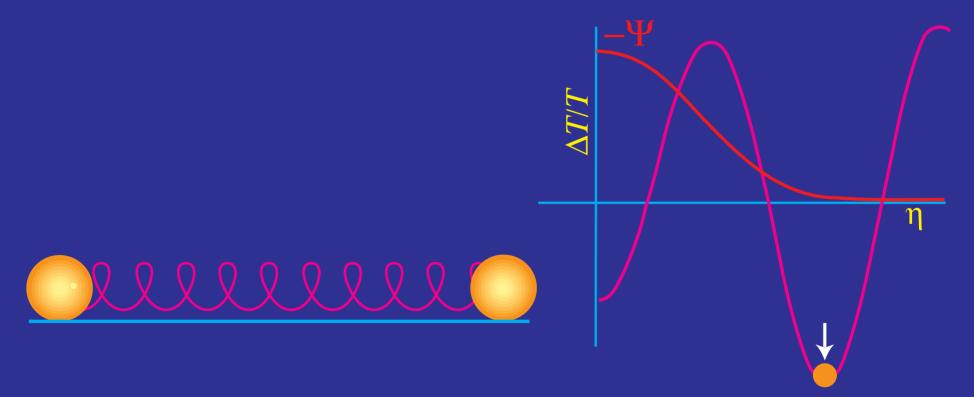
Hu & Sugiyama (1995)

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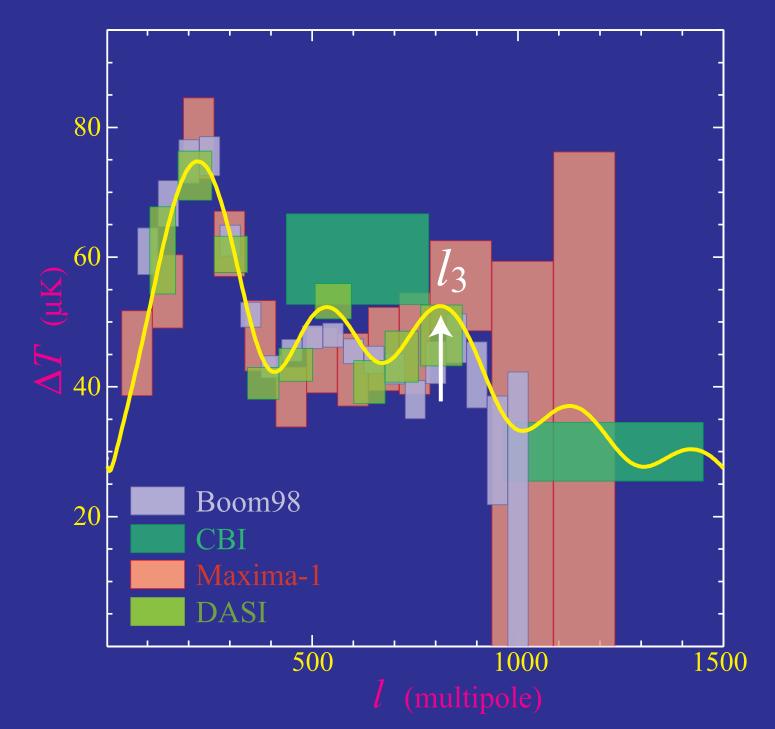
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Hu & Sugiyama (1995)

Dark Matter in the Power Spectrum

Third Peak Constrained



Clean Laundry: Standard RulersCalibrated the Standard Rulers

Sound Horizon

 $\begin{array}{c} \mathbb{P}_{1} \mathbb{P}_$

Baryon drag & Radiation driving

0, , 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18,

Damping Tail

SV

Diffusion Damping

- Diffusion inhibited by baryons
- Random walk length scale depends on time to diffuse: horizon scale at recombination

Diffusion Damping

- Random walk during recombination
- Dissipation as hot meets cold
- Physical scale for standard ruler or calibration



• Perfect fluid: no anisotropic stresses due to scattering isotropization; baryons and photons move as single fluid

Damping

- Perfect fluid: no anisotropic stresses due to scattering isotropization; baryons and photons move as single fluid
- Fluid imperfections are related to the mean free path of the photons in the baryons

$$\lambda_C = \dot{\tau}^{-1}$$
 where $\dot{\tau} = n_e \sigma_T a$

is the conformal opacity to Thomson scattering

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$$\lambda_D = \sqrt{N}\lambda_C = \sqrt{\eta/\lambda_C}\,\lambda_C = \sqrt{\eta\lambda_C}$$

the geometric mean between the horizon and mean free path

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the geometric mean between the horizon and mean free path

λ_D/η_{*} ~ few %, so expect the peaks > 3rd to be affected by dissipation

Equations of Motion

• Continuity

$$\dot{\Theta} = -\frac{k}{3}v_{\gamma}, \quad \dot{\delta}_{b} = -kv_{b}$$

where gravitational effects ignored and $\Theta \equiv \Delta T/T$.

• Euler

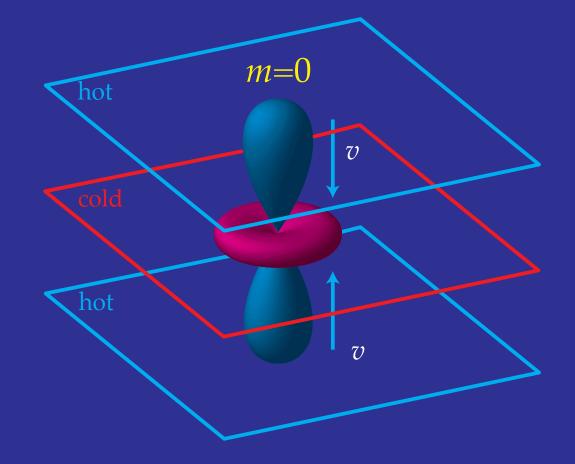
$$\dot{v}_{\gamma} = k\Theta - rac{k}{6}\pi_{\gamma} - \dot{\tau}(v_{\gamma} - v_b)$$

 $\dot{v}_b = -rac{\dot{a}}{a}v_b + \dot{\tau}(v_{\gamma} - v_b)/R$

where $k\Theta$ is the pressure gradient term, $k\pi_{\gamma}$ is the viscous stress term, and $v_{\gamma} - v_b$ is the momentum exchange term with $R \equiv 3\rho_b/4\rho_{\gamma}$ the baryon-photon momentum ratio.

Viscosity & Heat Conduction

- Both fluid imperfections are related to the gradient of the velocity kv_{γ} by opacity $\dot{\tau}$: slippage of fluids $v_{\gamma} v_b$.
- Viscosity is an anisotropic stress or quadrupole moment formed by radiation streaming from hot to cold regions



Damping Term

• Oscillator equation contains a $\dot{\Theta}$ damping term

$$\ddot{\Theta} + \frac{k^2}{\dot{\tau}} A_{\rm d} \dot{\Theta} + k^2 c_s^2 \Theta = 0$$

• Solve in the adiabatic approximation

$$\Theta \propto \exp(i \int \omega d\eta)$$

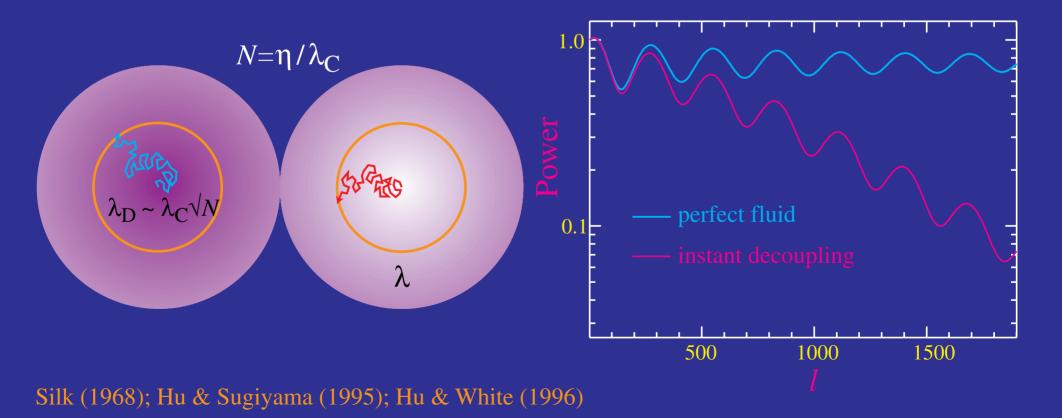
$$\exp(i\int\omega d\eta) = e^{\pm ik\int c_s d\eta} \exp[-(k/k_D)^2]$$

• Diffusion wavenumber, geometric mean between horizon and mfp:

$$k_D^{-2} = \frac{1}{2} \int \frac{d\eta}{\dot{\tau}} A_{\rm d} \sim \frac{\eta}{\dot{\tau}}$$

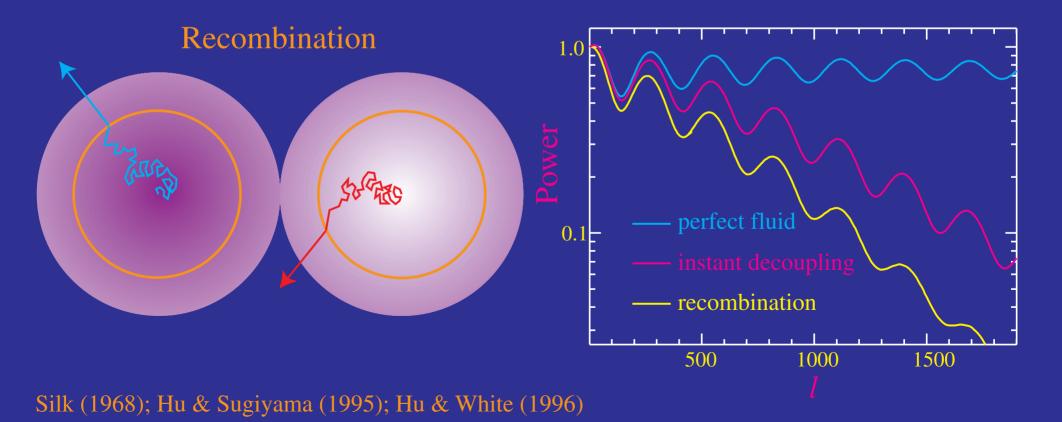
Dissipation / Diffusion Damping

- Imperfections in the coupled fluid \rightarrow mean free path λ_C in the baryons
- Random walk over diffusion scale: geometric mean of mfp & horizon $\lambda_D \sim \lambda_C \sqrt{N} \sim \sqrt{\lambda_C} \eta \gg \lambda_C$
- Overtake wavelength: $\lambda_D \sim \lambda$; second order in λ_C/λ
- Viscous damping for *R*<1; heat conduction damping for *R*>1



Dissipation / Diffusion Damping

- Rapid increase at recombination as mfp \uparrow
- Independent of (robust to changes in) perturbation spectrum
- Robust physical scale for angular diameter distance test ($\Omega_{\rm K}, \Omega_{\Lambda}$)



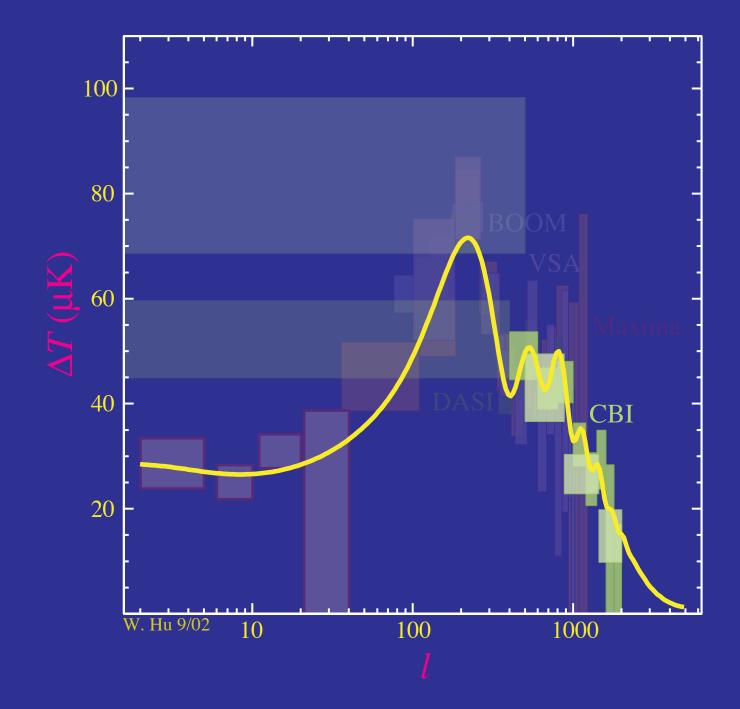
Standard Ruler

- Damping length is a fixed physical scale given properties at recombination
- Gemoetric mean of mean free path and horizon: depends on baryon-photon ratio and matter-radiation ratio

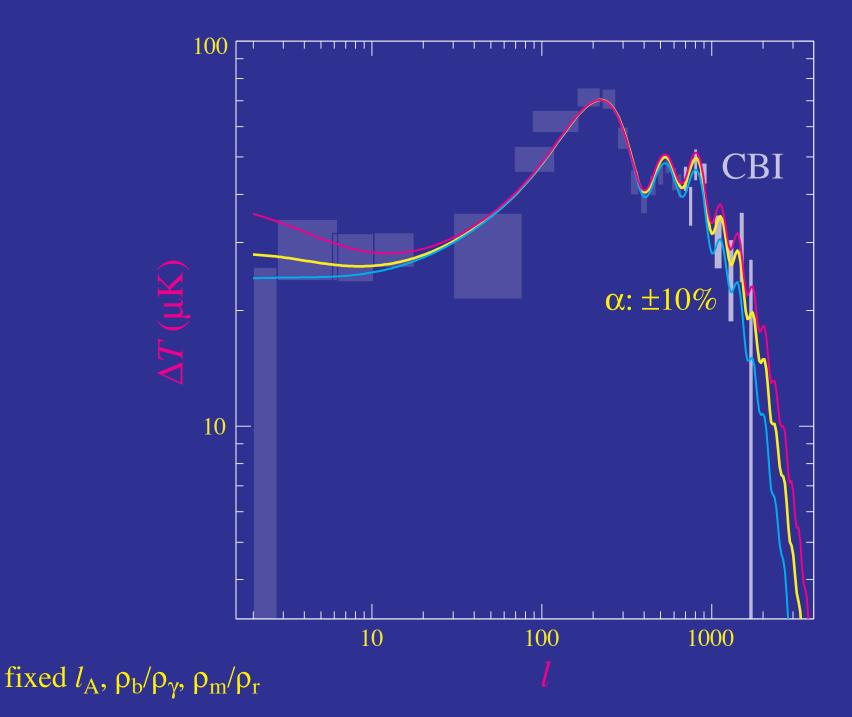
Curvature

- Calibration from lower peaks of $\Omega_b h^2$ and $\Omega_m h^2$ allows measurement of curvature from damping scale
- Independently of peak scale, confirms flat geometry

Damping Tail Measured



Beyond the Standard Model



Implications of Damping

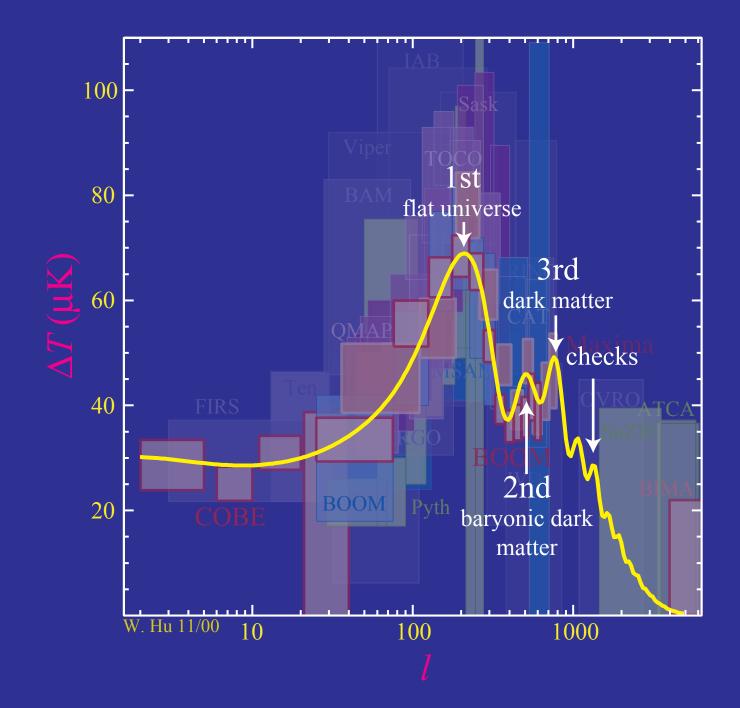
CMB anisotropies ~10% polarized

dissipation -> viscosity -> quadrupole anisotropy -> linear polarization

• Secondary anisotropies are observable

dissipation -> exponential suppression of primary anisotropy -> uncovery of secondary anisotropy

The Peaks



Summary

- Precision cosmology has arrived
- Sound physics seen (pun intended)
- Consistent with inflationary initial conditions
- First peak nailed: nearly flat universe
- Second determined: baryonic dark matter (consistent with Big Bang Nucleosynthesis)
- Third measured: cold dark matter required but does not add up to critical: dark energy
- Damping detected: consistency checks passed