

The Silk Damping Tail of the CMB



Wayne Hu
Oxford, December 2002

Outline

- Damping tail of temperature power spectrum and its use as a standard ruler
- Generation of polarization through damping
- Unveiling of gravitational lensing from features in the damping tail

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 - Takemi Okamoto
 - Joe Silk
 - Martin White
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- Generation of **polarization** through damping
- Unveiling of **gravitational lensing** from features in the damping tail

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<http://background.uchicago.edu>
("Presentations" in PDF)



Damping Tail

Photon-Baryon Plasma

- Before $z \sim 1000$ when the CMB had $T > 3000\text{K}$, hydrogen ionized
- Free electrons act as "glue" between photons and baryons by Compton scattering and Coulomb interactions
- Nearly perfect fluid

Anisotropy Power Spectrum

Damping

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- $\lambda_D / \eta_* \sim$ **few %**, so expect the **peaks > 3rd** to be affected by **dissipation**

Equations of Motion

- Continuity

$$\dot{\Theta} = -\frac{k}{3}v_{\gamma}, \quad \dot{\delta}_b = -kv_b$$

where gravitational effects ignored and $\Theta \equiv \Delta T/T$.

- Euler

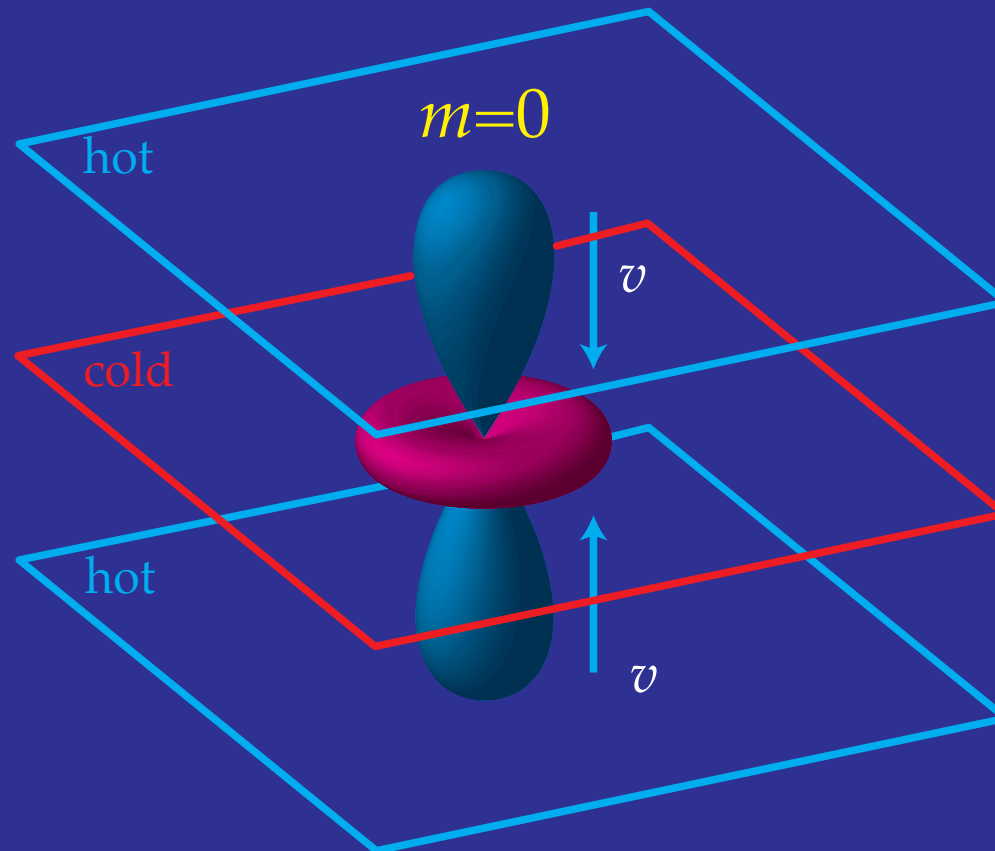
$$\dot{v}_{\gamma} = k\Theta - \frac{k}{6}\pi_{\gamma} - \dot{\tau}(v_{\gamma} - v_b)$$

$$\dot{v}_b = -\frac{\dot{a}}{a}v_b + \dot{\tau}(v_{\gamma} - v_b)/R$$

where $k\Theta$ is the pressure gradient term, $k\pi_{\gamma}$ is the viscous stress term, and $v_{\gamma} - v_b$ is the **momentum exchange** term with $R \equiv 3\rho_b/4\rho_{\gamma}$ the baryon-photon momentum ratio.

Viscosity & Heat Conduction

- Both fluid imperfections are related to the gradient of the velocity kv_γ by opacity $\dot{\tau}$: slippage of fluids $v_\gamma - v_b$.
- Viscosity** is an anisotropic stress or **quadrupole moment** formed by radiation **streaming** from hot to cold regions



Damping Term

- Oscillator equation contains a $\dot{\Theta}$ damping term

$$\ddot{\Theta} + \frac{k^2}{\dot{\tau}} A_d \dot{\Theta} + k^2 c_s^2 \Theta = 0$$

- Solve in the adiabatic approximation

$$\Theta \propto \exp(i \int \omega d\eta)$$

$$\exp(i \int \omega d\eta) = e^{\pm i k \int c_s d\eta} \exp[-(k/k_D)^2]$$

- Diffusion wavenumber, geometric mean between horizon and mfp:

$$k_D^{-2} = \frac{1}{2} \int \frac{d\eta}{\dot{\tau}} A_d \sim \frac{\eta}{\dot{\tau}}$$

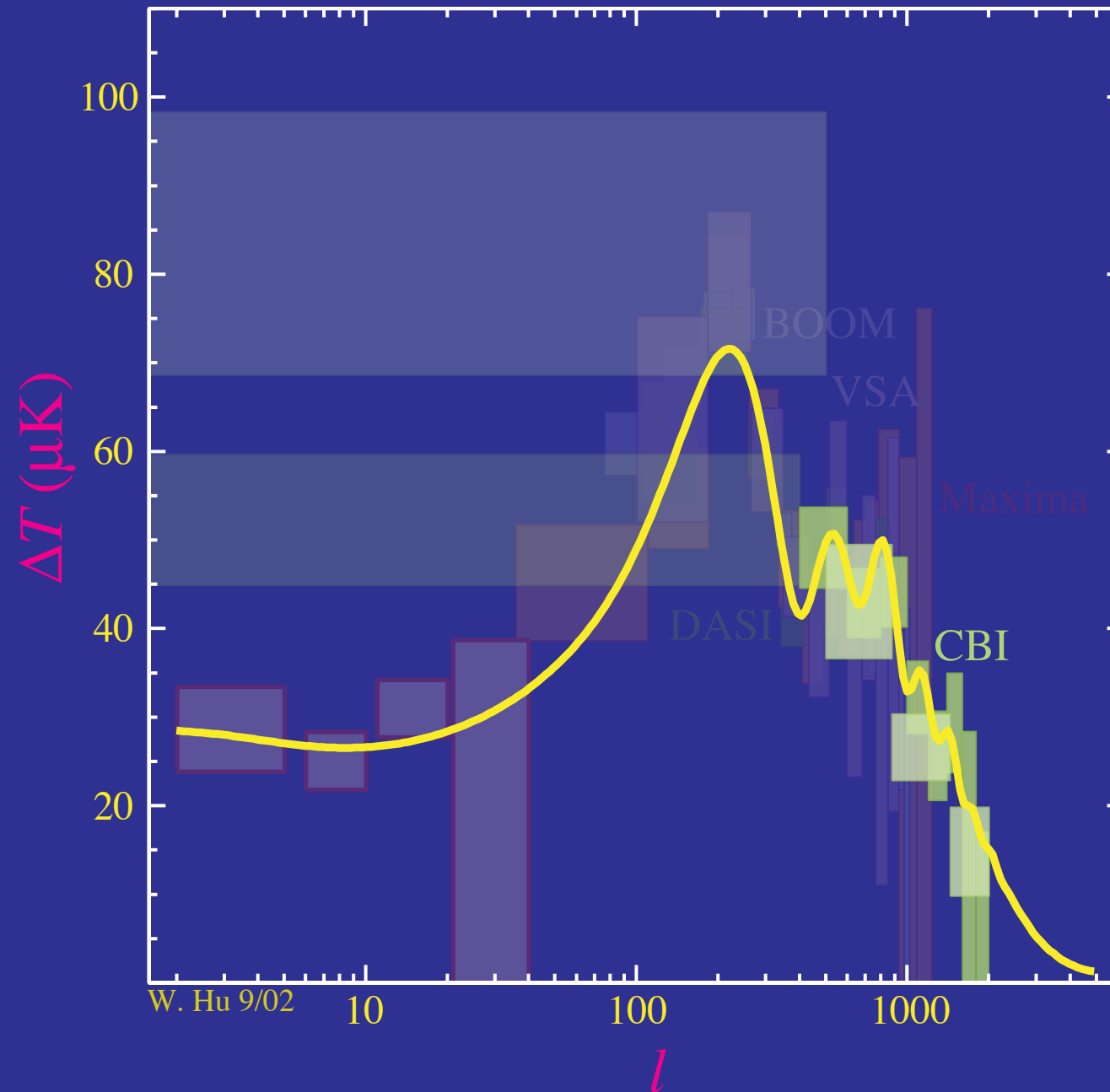
Standard Ruler

- Damping length is a fixed physical scale given properties at recombination
- Geometric mean of mean free path and horizon: depends on baryon-photon ratio and matter-radiation ratio

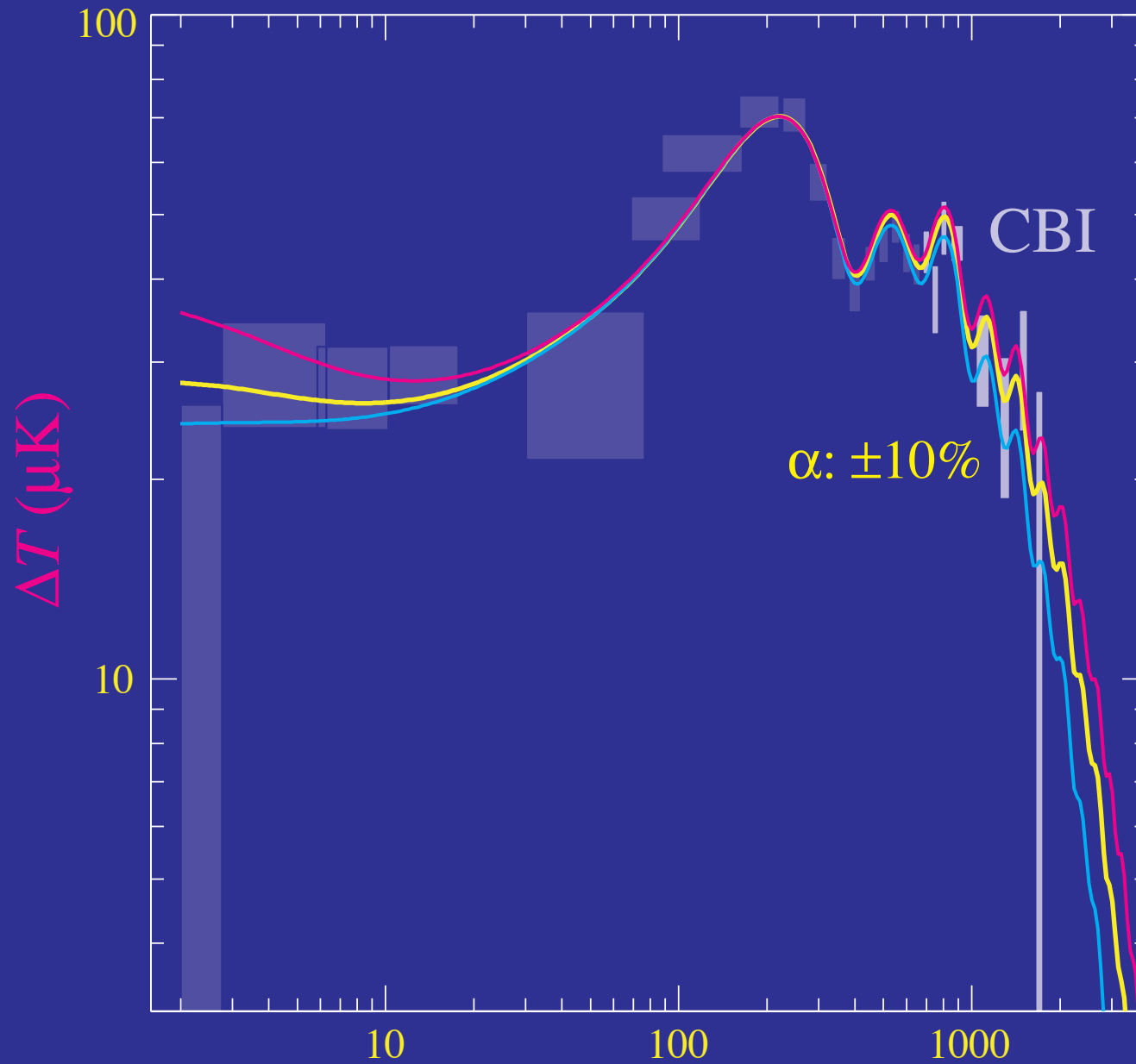
Curvature

- Calibration from lower peaks of $\Omega_b h^2$ and $\Omega_m h^2$ allows measurement of **curvature** from damping scale
- **Independently** of peak scale, confirms **flat geometry**

Damping Tail Measured



Beyond the Standard Model



fixed l_A , ρ_b/ρ_γ , ρ_m/ρ_r



Polarization

Damped Acoustic Oscillations

- From inhomogeneity to anisotropy:

Polarization from Thomson Scattering

- Differential cross section depends on polarization and angle

Polarization from Thomson Scattering

- Isotropic radiation scatters into unpolarized radiation

Polarization from Thomson Scattering

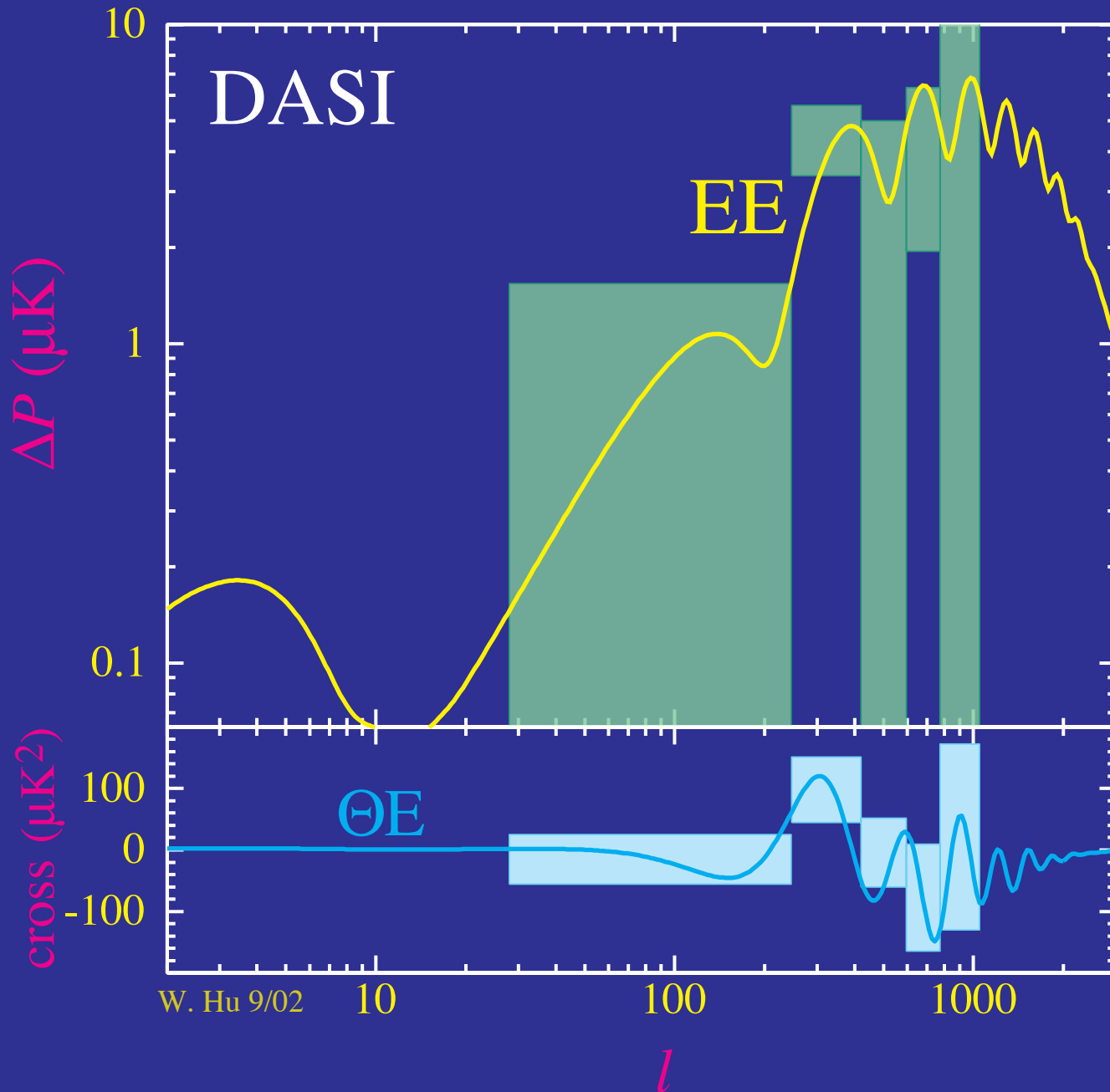
- Quadrupole anisotropies scatter into linear polarization

aligned with
cold lobe

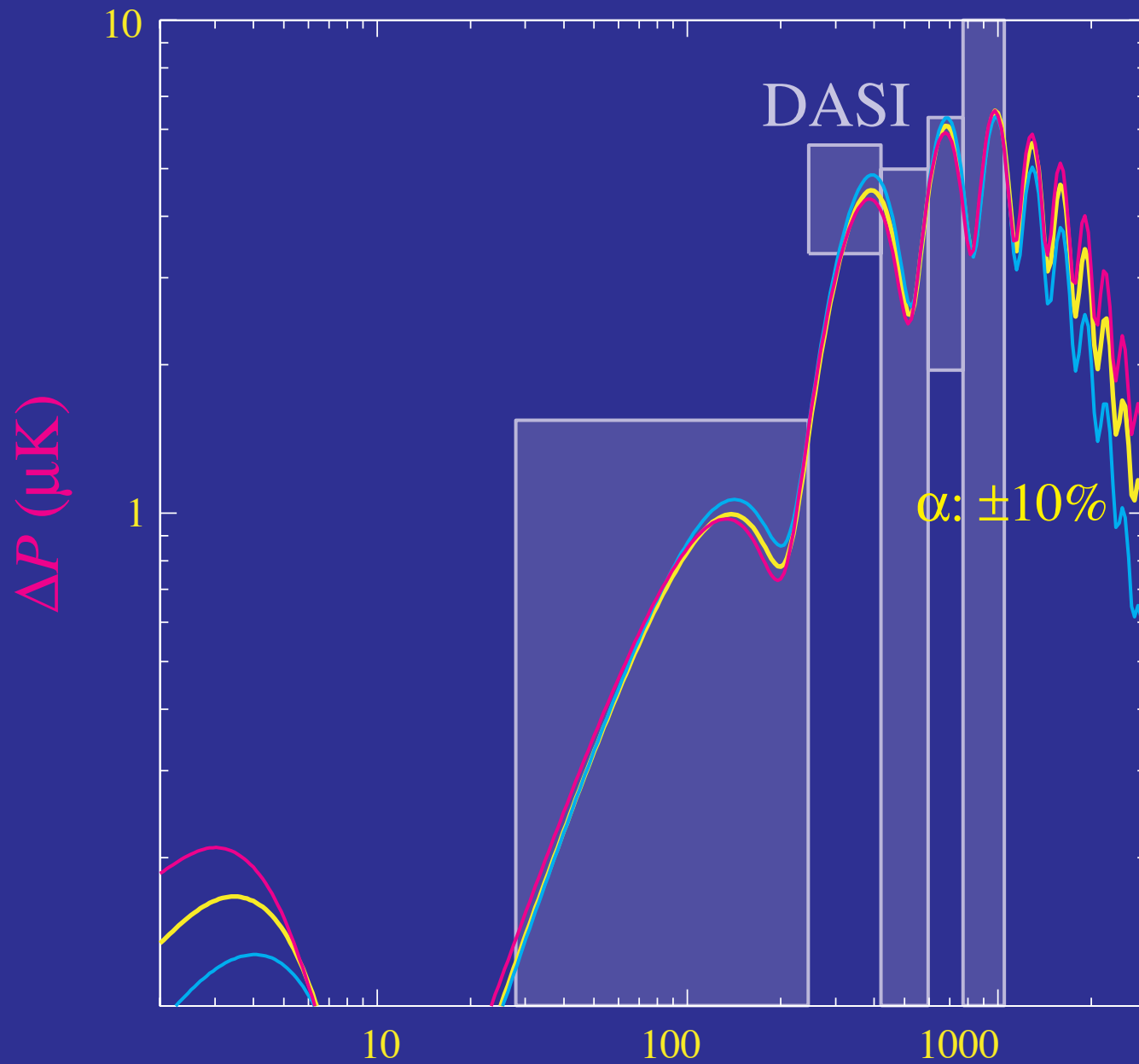
Polarization on the Sphere

- **Polarization** direction oriented with the **cold lobe** of the quadrupole
- A local observer will see a **$\sin^2\theta$** pattern of **Q -polarization**: spin–spherical harmonic: $l=2, m=0, s=2$: ${}_2Y_2^0$.

Polarization Detected



Beyond the Standard Model



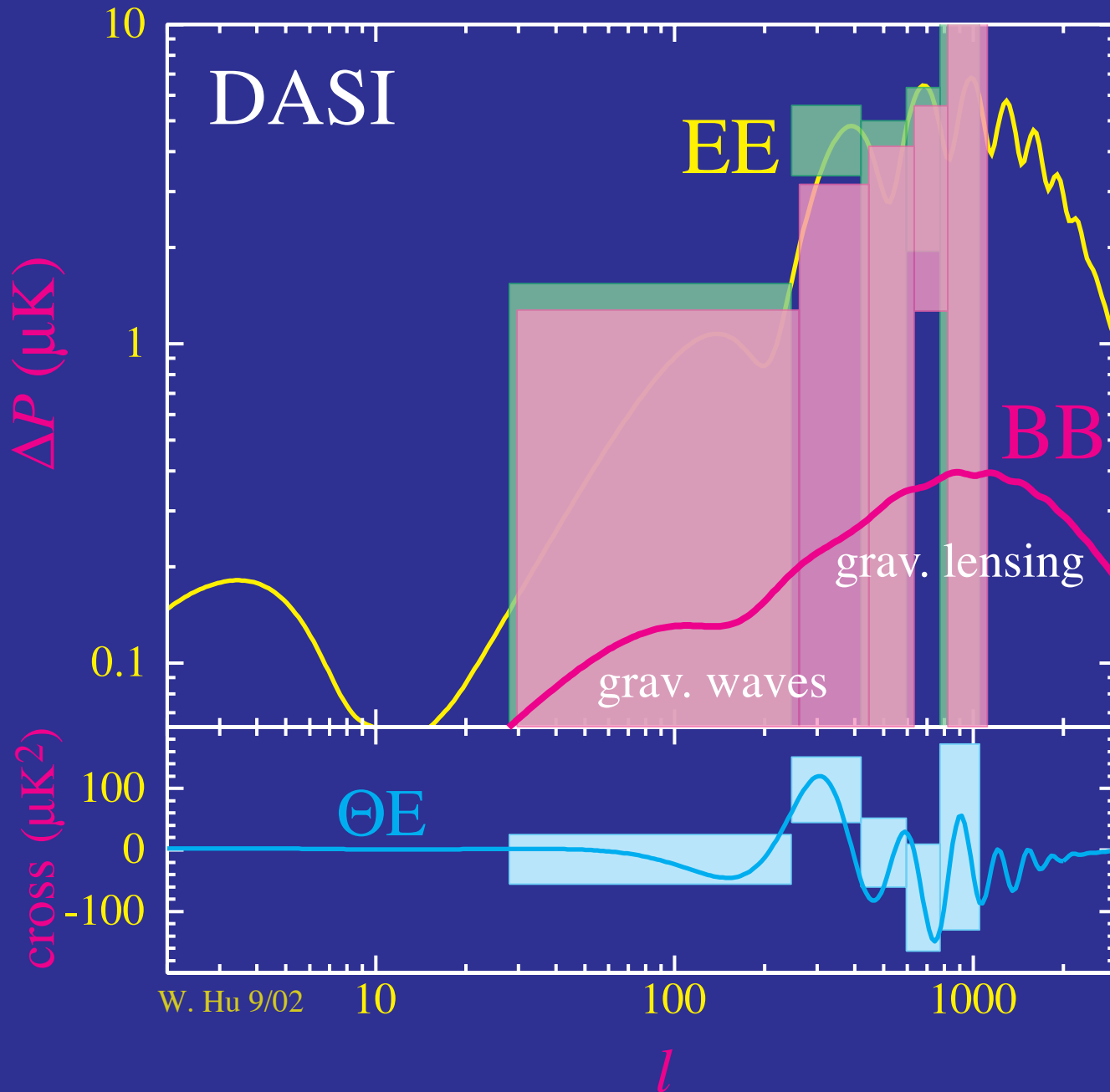
fixed l_A , ρ_b/ρ_γ , ρ_m/ρ_r

Polarization on the Sphere

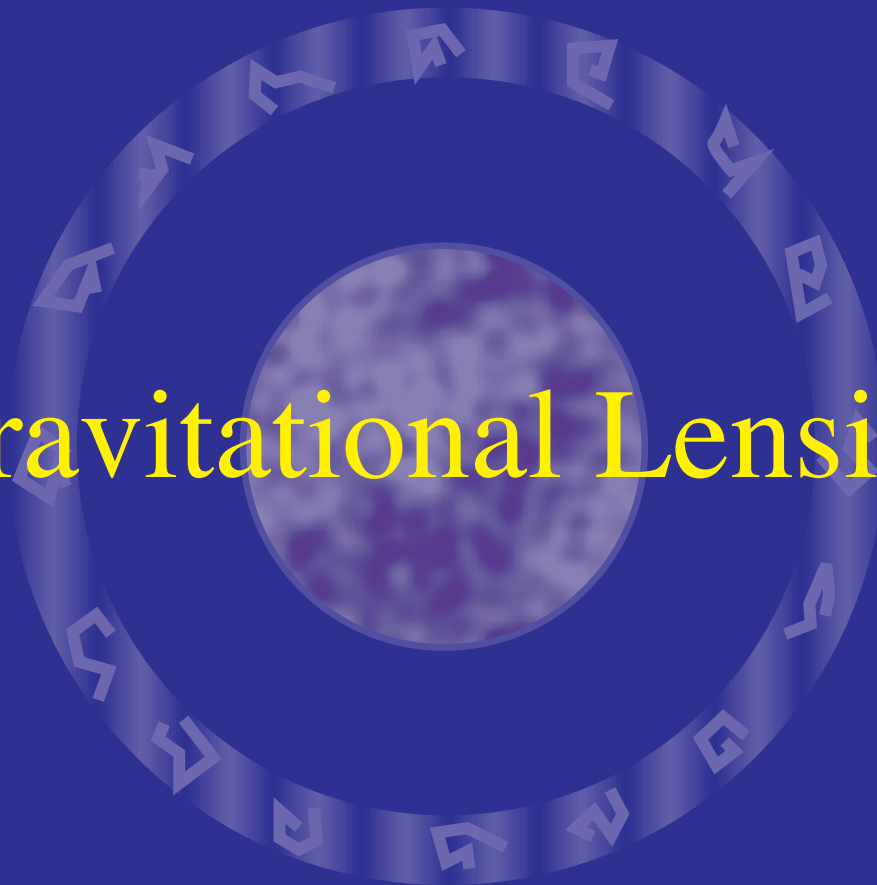
- Polarization due to gravitational waves follows similarly
- $m=\pm 2$ quadrupole viewed at different angles

- Difference: no symmetry – Q and U polarization
- Coordinate independent description of polarization

B-mode Spectrum



Gravitational Lensing

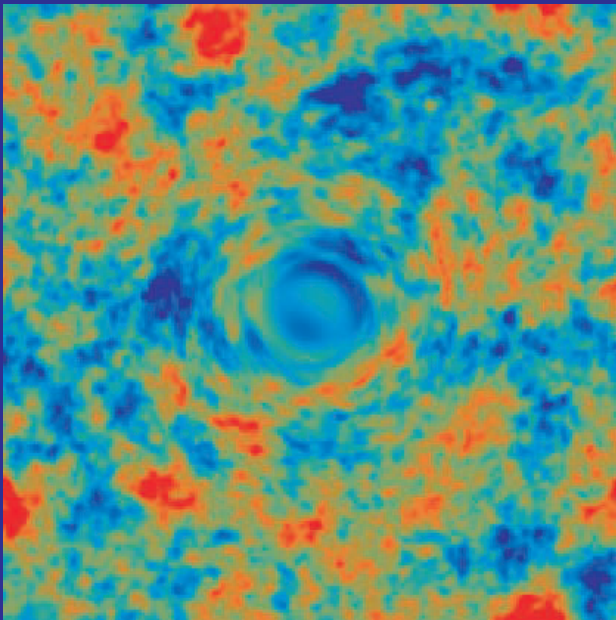


Lensing of a Gaussian Random Field

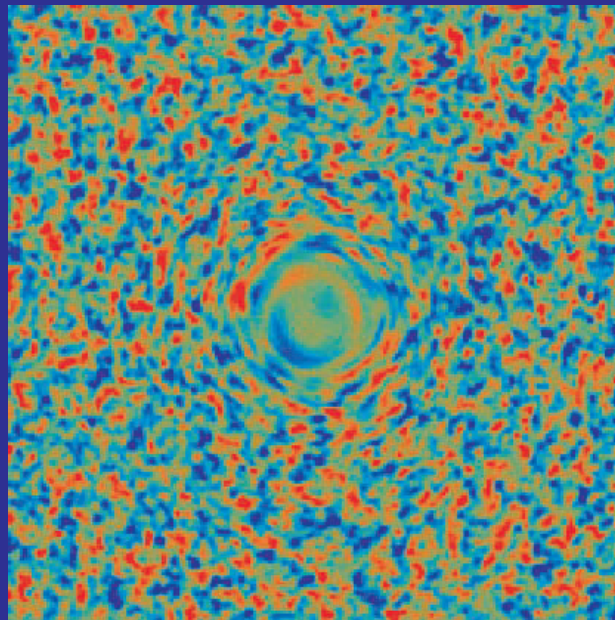
- CMB temperature and polarization anisotropies are Gaussian random fields – unlike galaxy weak lensing
- Average over many noisy images – like galaxy weak lensing

B-Mode Mapping

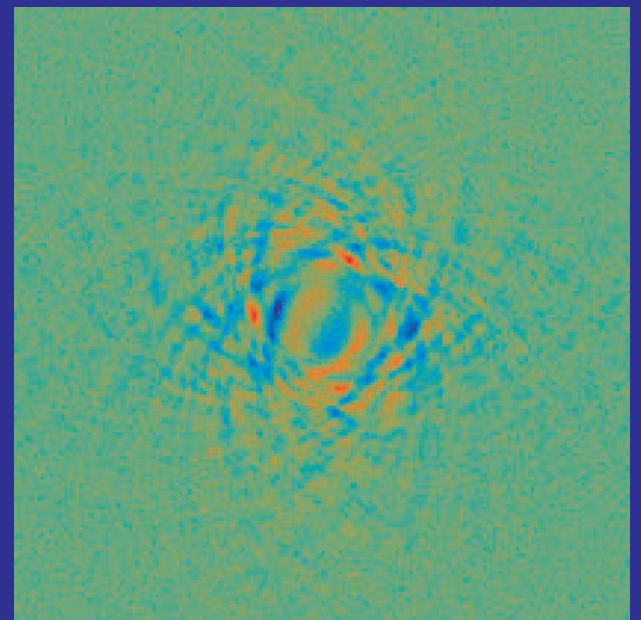
- **Lensing** warps polarization field and generates **B-modes** out of **E-mode** acoustic polarization - hence **correlation**



Temperature



E-polarization



B-polarization

Gravitational Lensing

- Lensing is a surface brightness conserving **remapping** of source to image planes by the gradient of the **projected potential**

$$\phi(\hat{\mathbf{n}}) = 2 \int_{\eta_*}^{\eta_0} d\eta \frac{(D_* - D)}{D D_*} \Phi(D\hat{\mathbf{n}}, \eta) .$$

such that the fields are remapped as

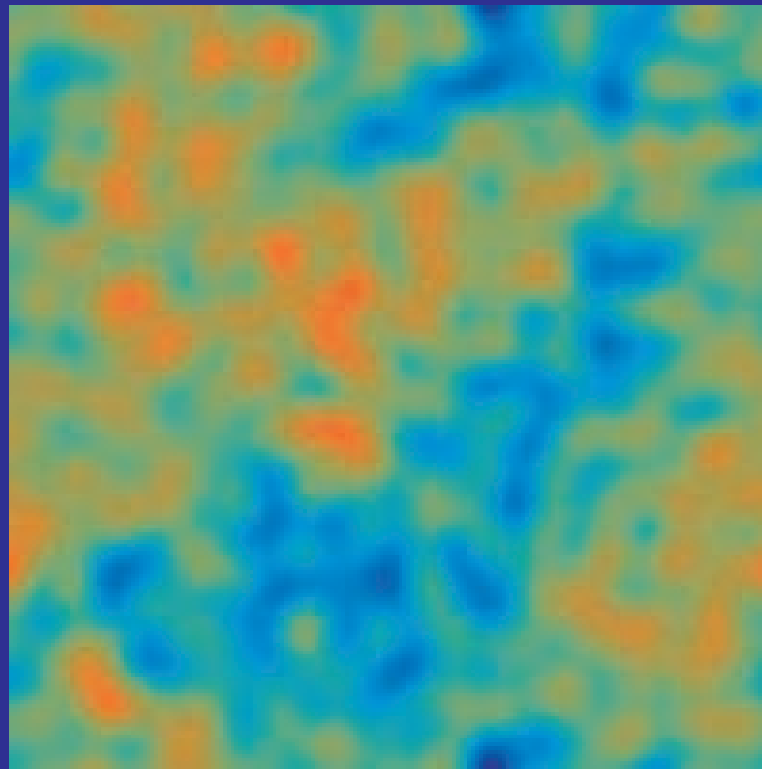
$$x(\hat{\mathbf{n}}) \rightarrow x(\hat{\mathbf{n}} + \nabla \phi) ,$$

where $x \in \{\Theta, Q, U\}$ temperature and polarization.

- Taylor expansion leads to **product** of fields and Fourier **convolution** (or mode coupling) - features in **damping tail**

Lensing by a Gaussian Random Field

- Mass distribution at large angles and high redshift in the linear regime
- Projected mass distribution (low pass filtered reflecting deflection angles): 1000 sq. deg



rms deflection

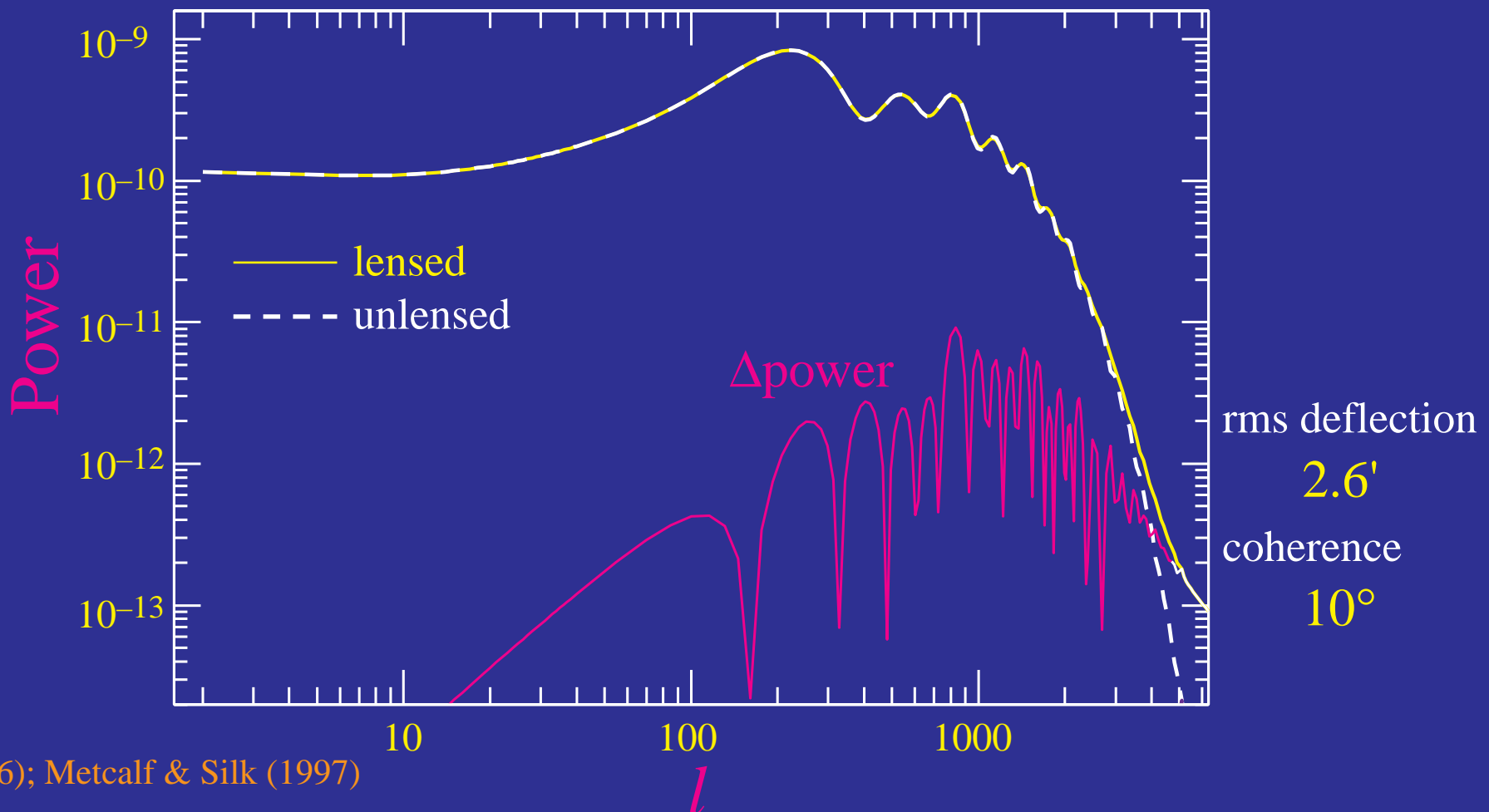
2.6'

deflection coherence

10°

Lensing in the Power Spectrum

- Lensing **smooths** the power spectrum with a width $\Delta l \sim 60$
- Sharp feature of **damping tail** is best place to see lensing



Reconstruction from the CMB

- Correlation between Fourier moments reflect lensing potential

$$\kappa = \nabla^2 \phi$$

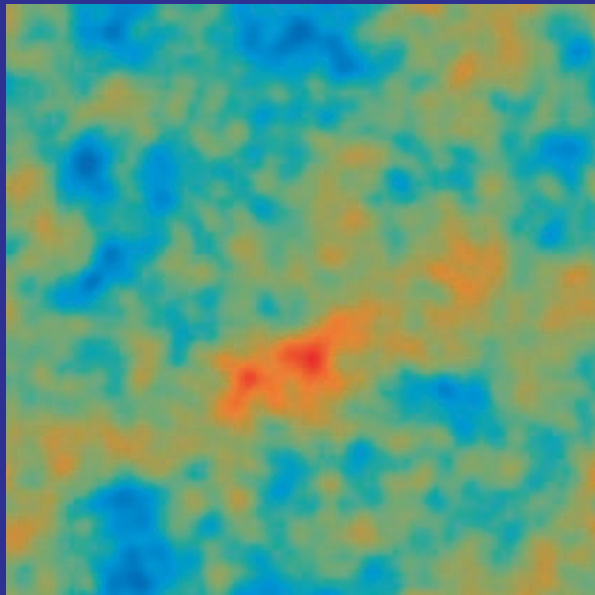
$$\langle x(\mathbf{l})x'(\mathbf{l}') \rangle_{\text{CMB}} = f_\alpha(\mathbf{l}, \mathbf{l}') \phi(\mathbf{l} + \mathbf{l}') ,$$

where $x \in$ temperature, polarization fields and f_α is a fixed weight that reflects geometry

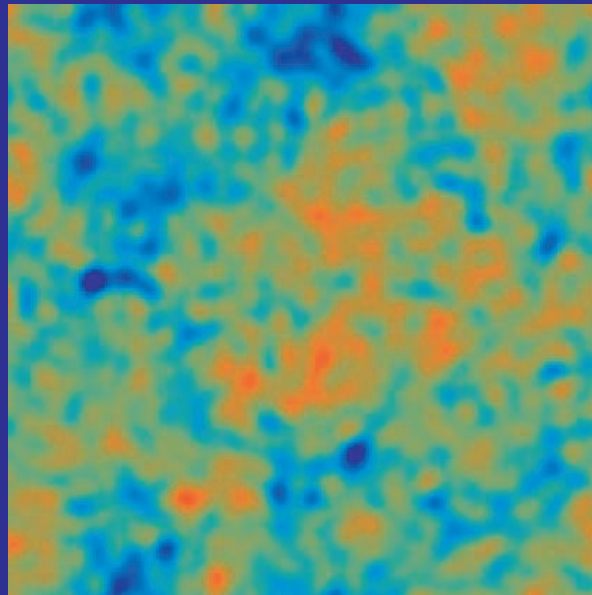
- Each pair forms a noisy estimate of the potential or projected mass
- just like a pair of galaxy shears
- Fundamentally relies on features in the power spectrum as found in the damping tail

Ultimate (Cosmic Variance) Limit

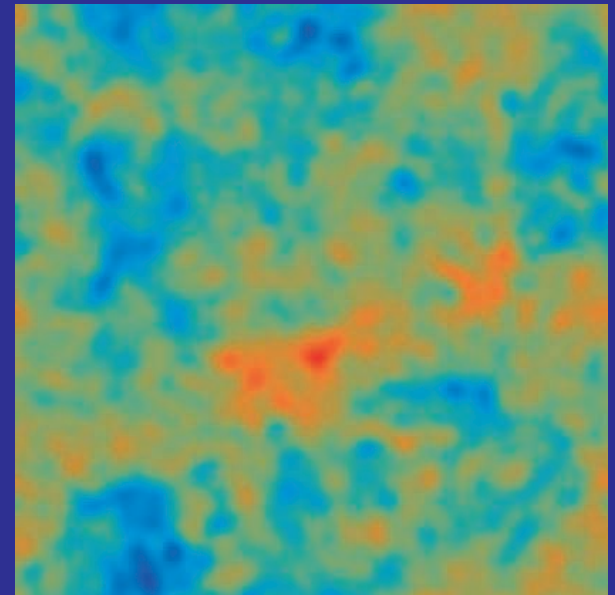
- Cosmic variance of CMB fields sets ultimate limit
- Polarization allows mapping to finer scales ($\sim 10'$)



mass



temp. reconstruction

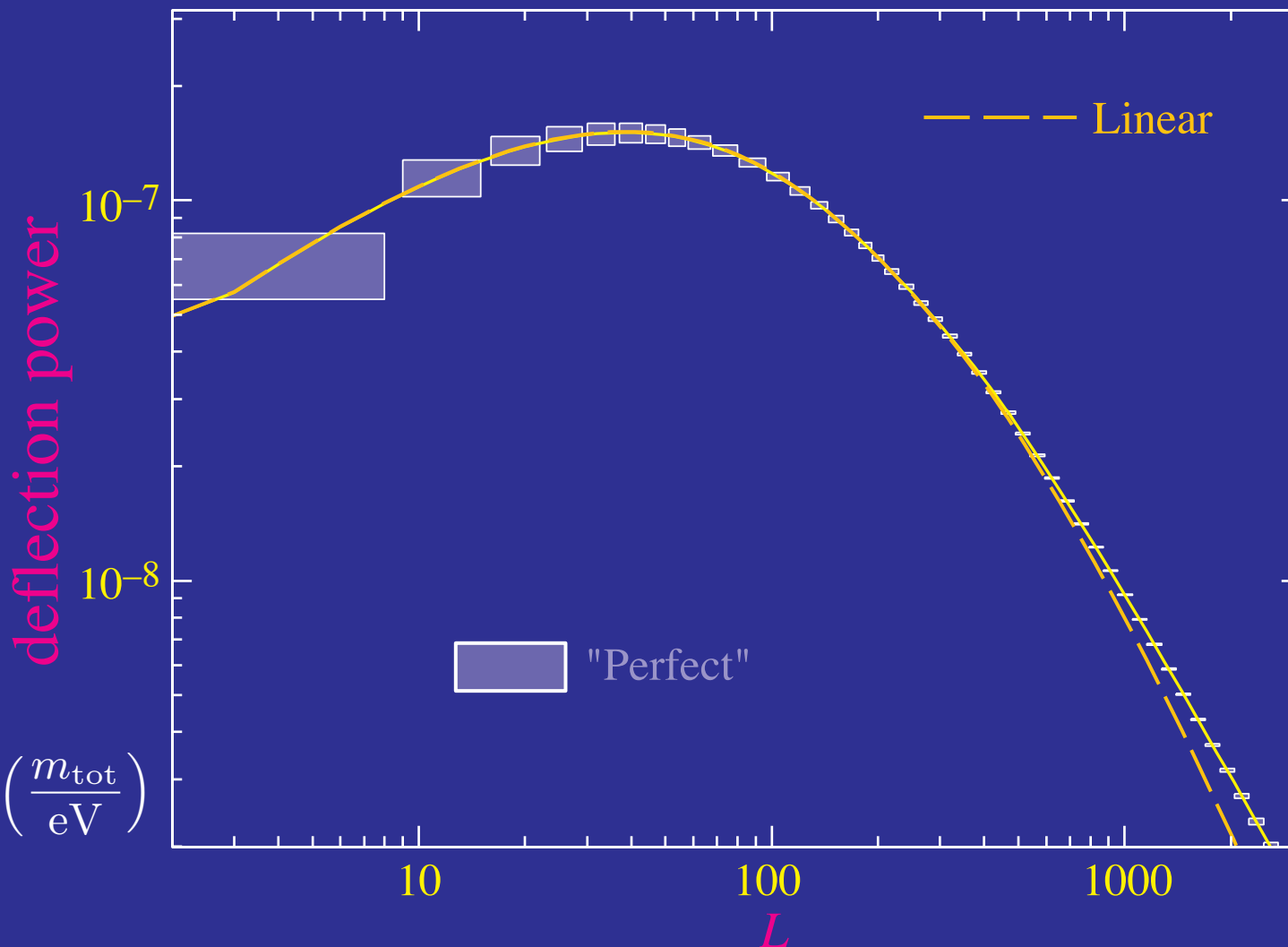


EB pol. reconstruction

100 sq. deg; 4' beam; $1\mu\text{K}$ -arcmin

Matter Power Spectrum

- Measuring projected **matter power** spectrum to cosmic variance limit across whole **linear regime** $0.002 < k < 0.2 \ h/\text{Mpc}$



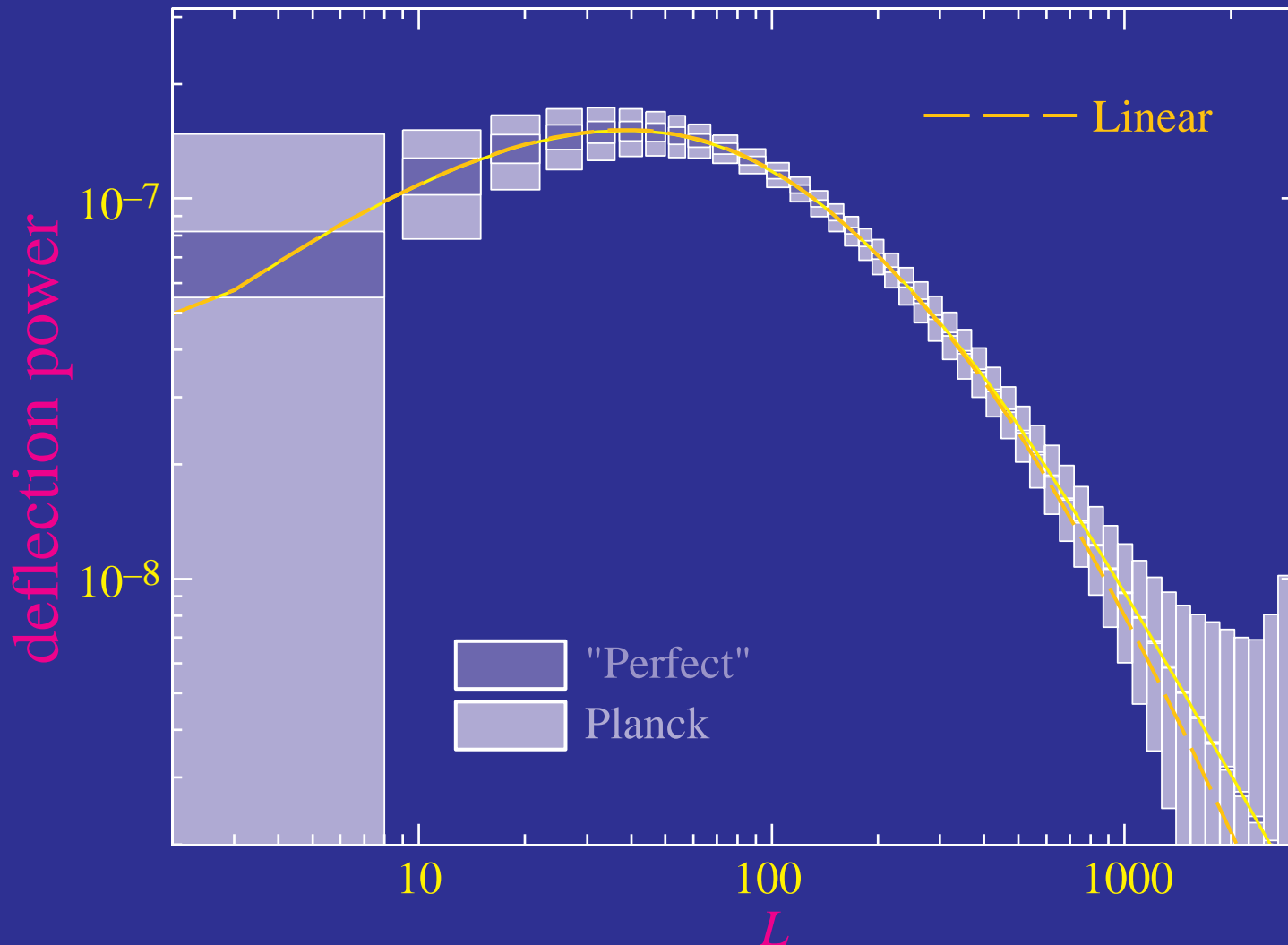
$$\frac{\Delta P}{P} \approx -0.6 \left(\frac{m_{\text{tot}}}{\text{eV}} \right)$$

Hu & Okamoto (2001)

$\sigma(w) \sim 0.06$

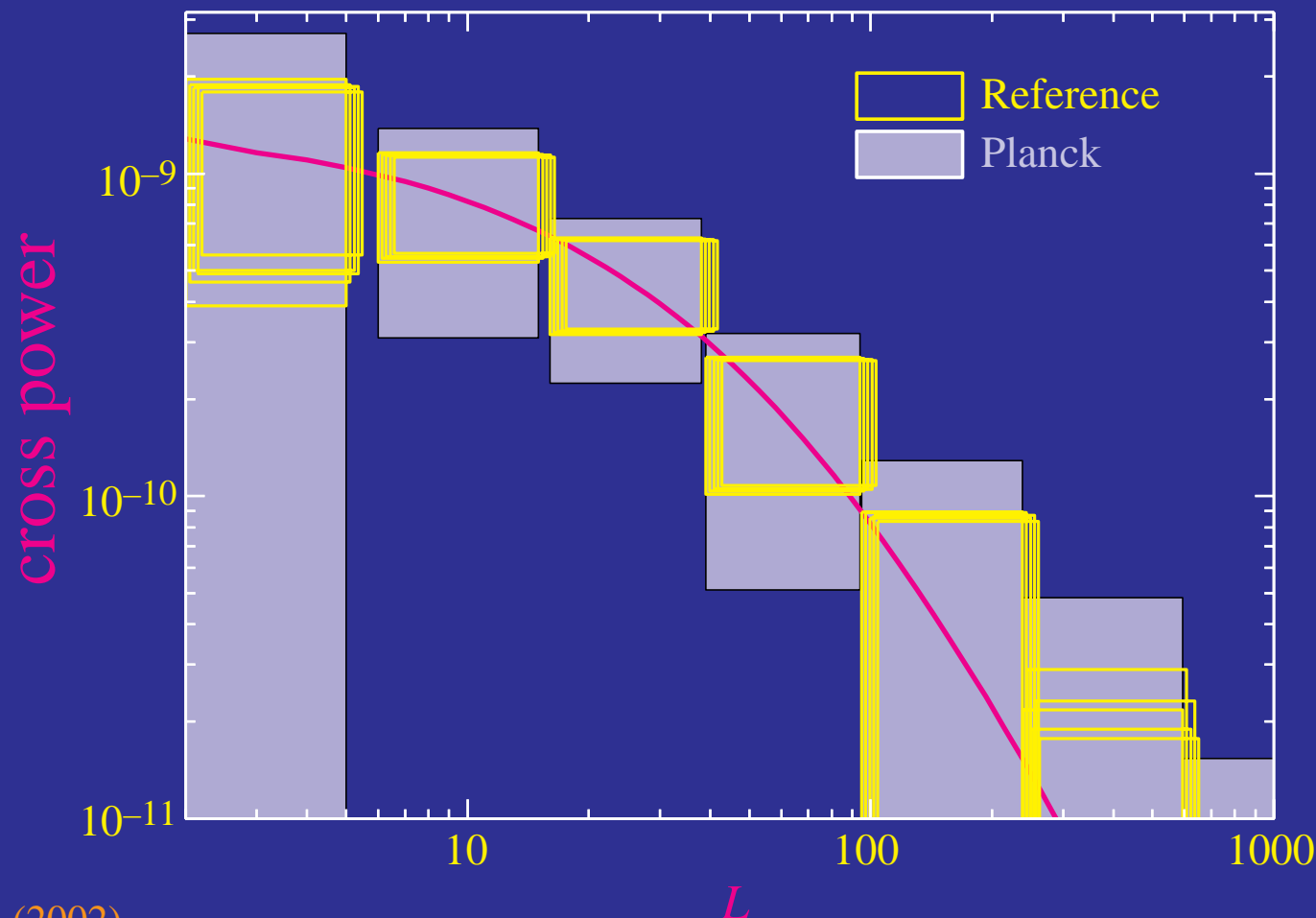
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Cross Correlation with Temperature

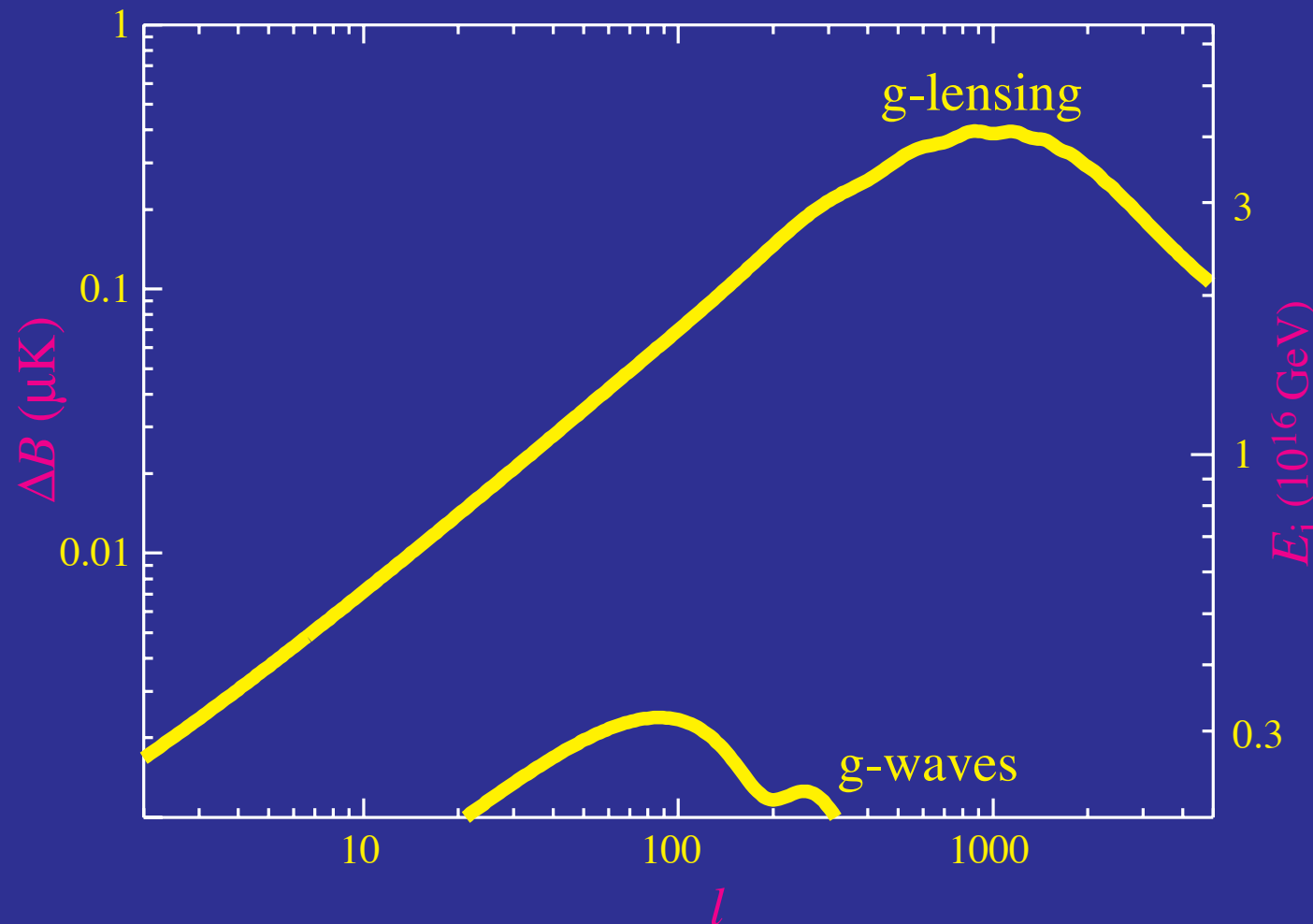
- Any correlation is a **direct detection** of a **smooth energy density** component through the **ISW** effect
- Dark energy smooth **>5-6 Gpc** scale, **test scalar field** nature



Contamination for Gravitational Waves

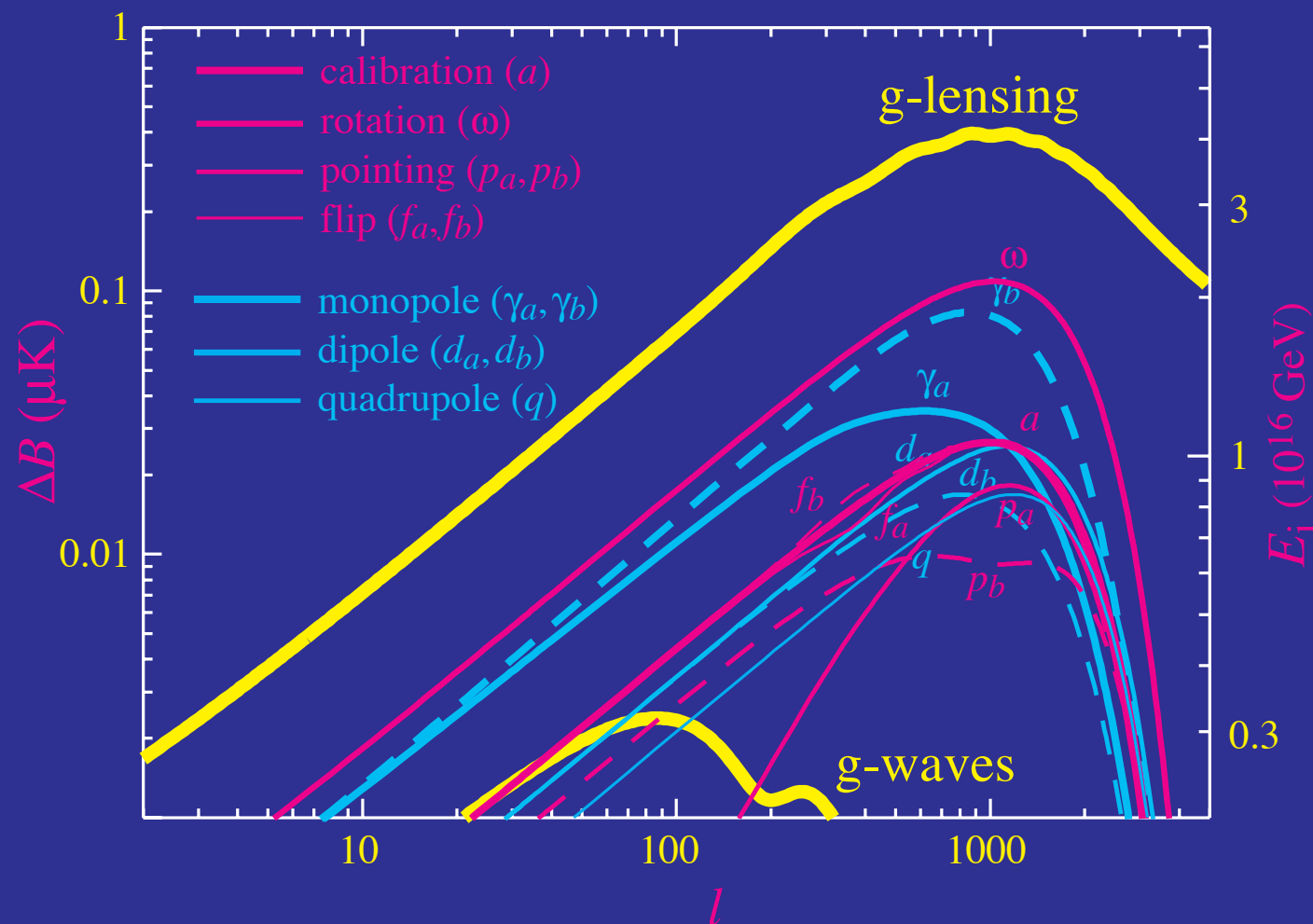
- Gravitational lensing contamination of B-modes from gravitational waves cleaned to $E_i \sim 0.3 \times 10^{16}$ GeV

Hu & Okamoto (2002) limits by Knox & Song (2002); Cooray, Kedsen, Kamionkowski (2002)



Contamination for Gravitational Waves

- A long road ahead:
catalogue of some systematics



Summary

- **Damping** of acoustic oscillations in CMB is due to the finite opacity of the plasma during recombination
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- **Damping** of acoustic oscillations in CMB is due to the finite opacity of the plasma during recombination
- **Damping length** is a standard ruler for cosmology: independent of peak scale and tests recombination physics, e.g. α
- Damping is the fundamental source of **acoustic polarization**, recently detected
- **Features** in damping tail allow the distribution of matter to be mapped through **gravitational lensing**
- Damping eliminates primary anisotropy and allows smaller **secondary signals** to be measured at arcminute scales, e.g. the SZE.