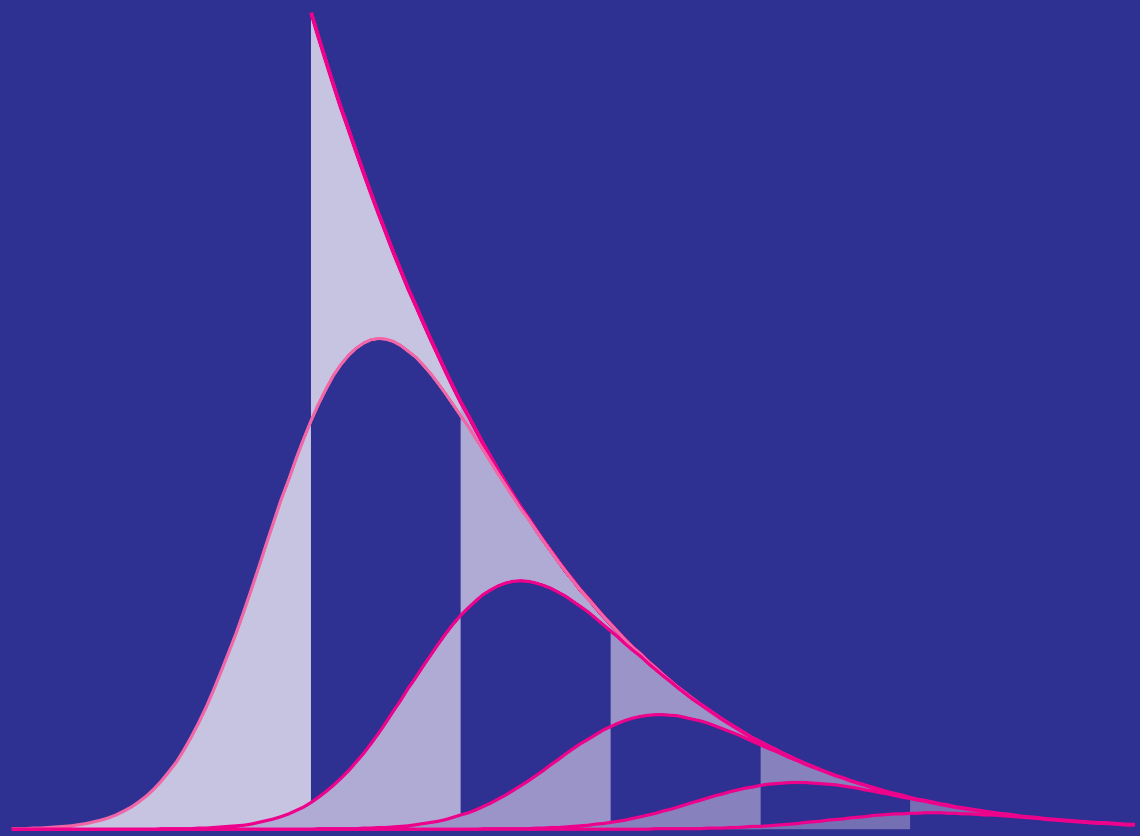
# Self Calibration of Cluster Counts:



# Observable-Mass Distribution

*Wayne Hu*

Kona, March 2005

# Scattered Forecasts

- Scatter, or a distribution in the observable mass, causes uncertainty in dark energy constraints at high z
- Related work:
  Holder et al (2000): bias from scatter in a signal-to-noise cut
  Levine et al (2002): marginalization of constant M-T bias & scatter

- This work:
  Lima & Hu (2005):

  abstract/general analysis of the impact of scatter and bias in the distribution

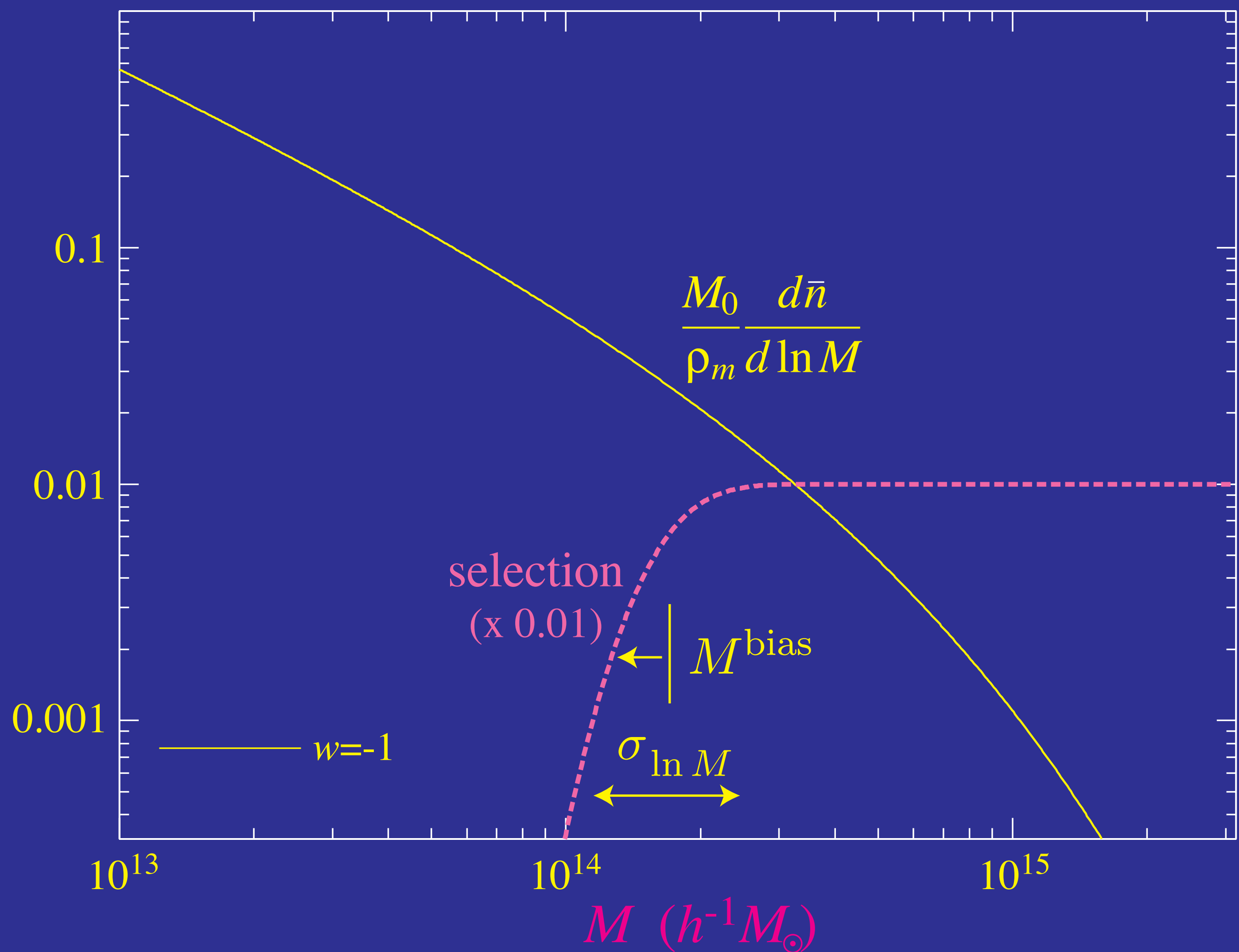
  prospects for self-calibration of a simple, Gaussian, mass independent distribution that evolves

  shape: Hu (2003); power: Majumdar & Mohr (2003)

# Observable Mass Distribution

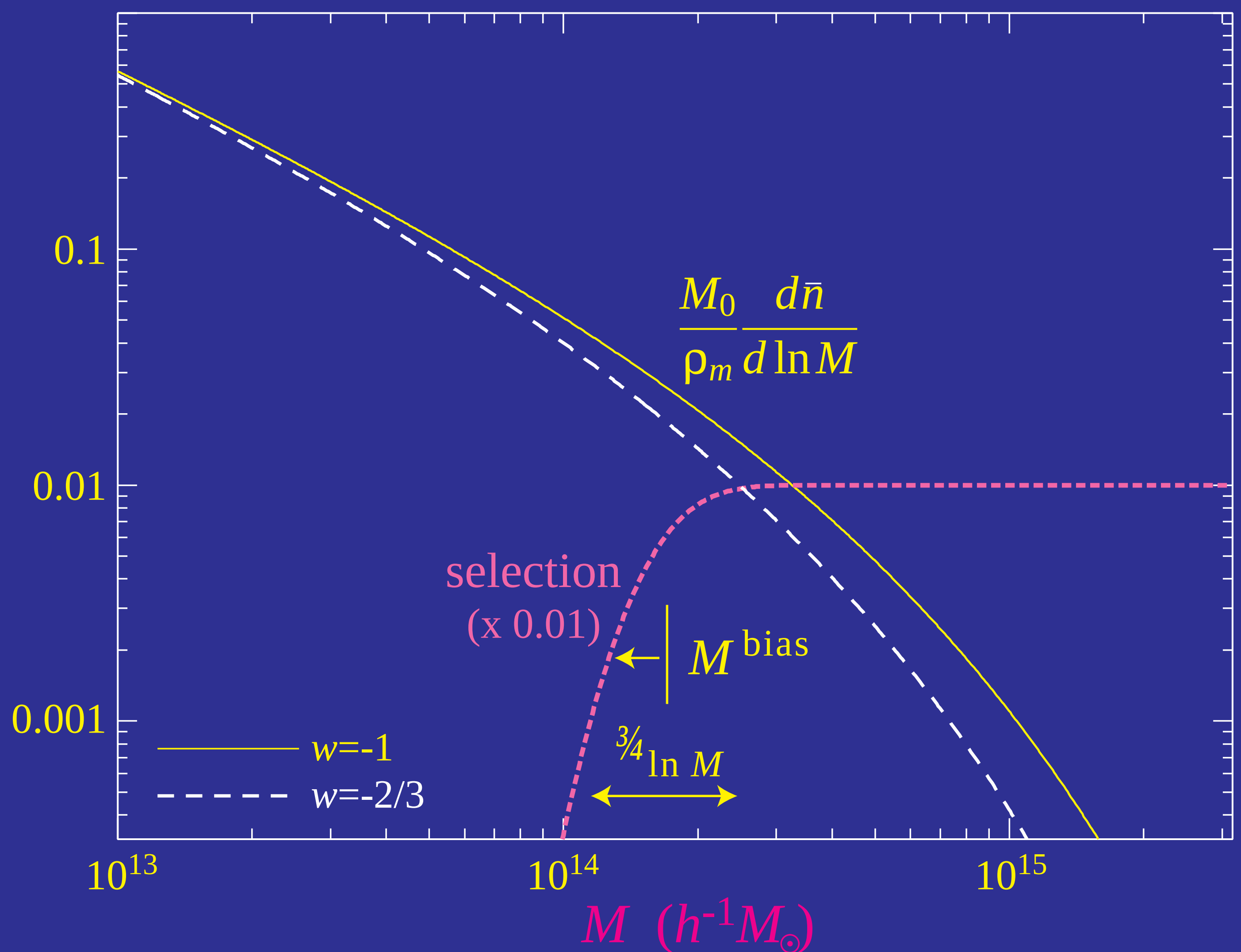
- Gaussian scatter and bias of a mass estimator

$$p(M^{\rm obs}|M) = \frac{1}{\sqrt{2\pi\sigma^2_{\ln M}}} \exp\left[ -\frac{(\ln M^{\rm obs} - \ln M - \ln M^{\rm bias})^2}{2\sigma^2_{\ln M}} \right]$$



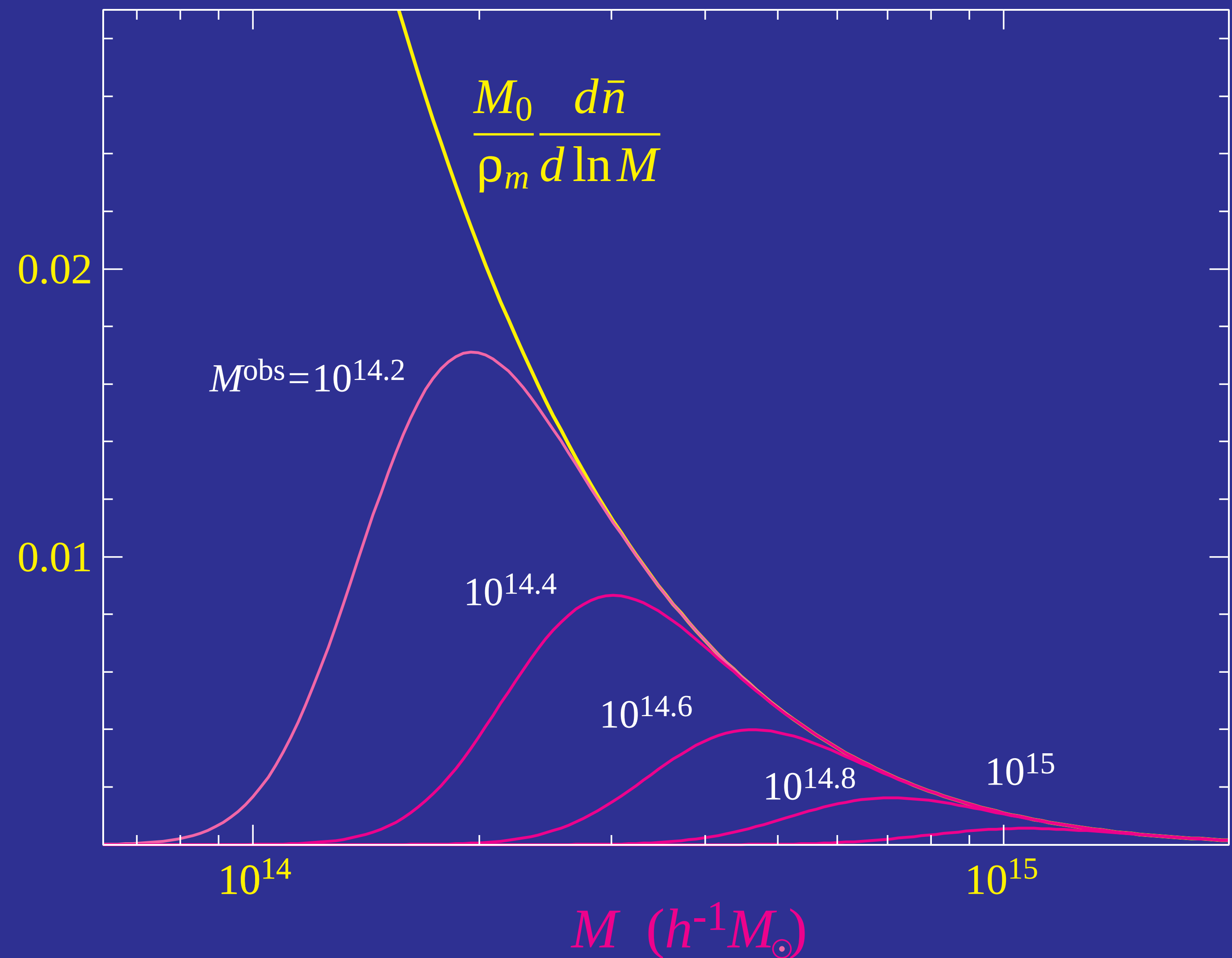
# Degeneracy

- Uncertainties in bias and scatter cause degeneracies with dark energy



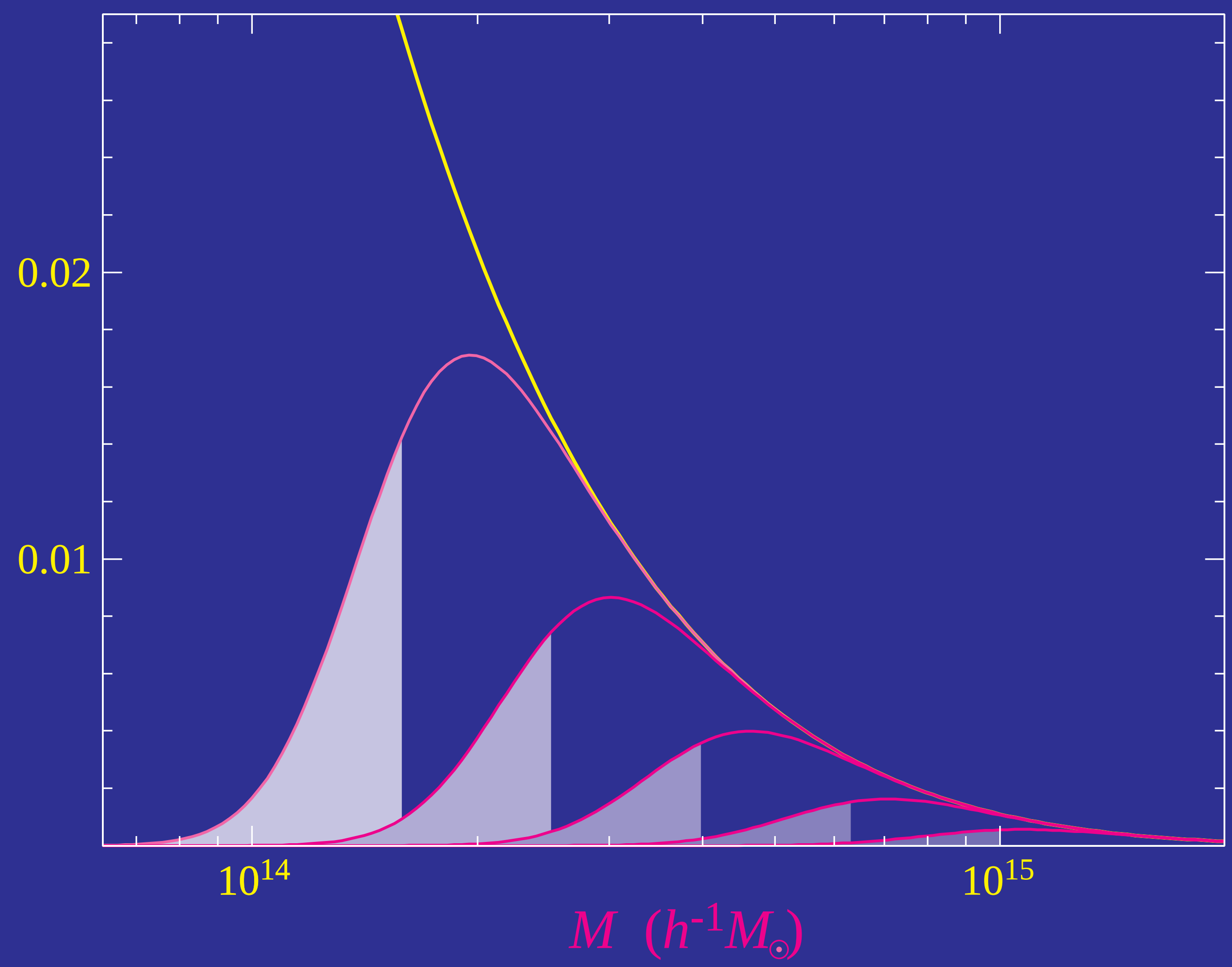
# Selection Bias

- Exponential tail of mass function
- Threshold cut in the observable mass



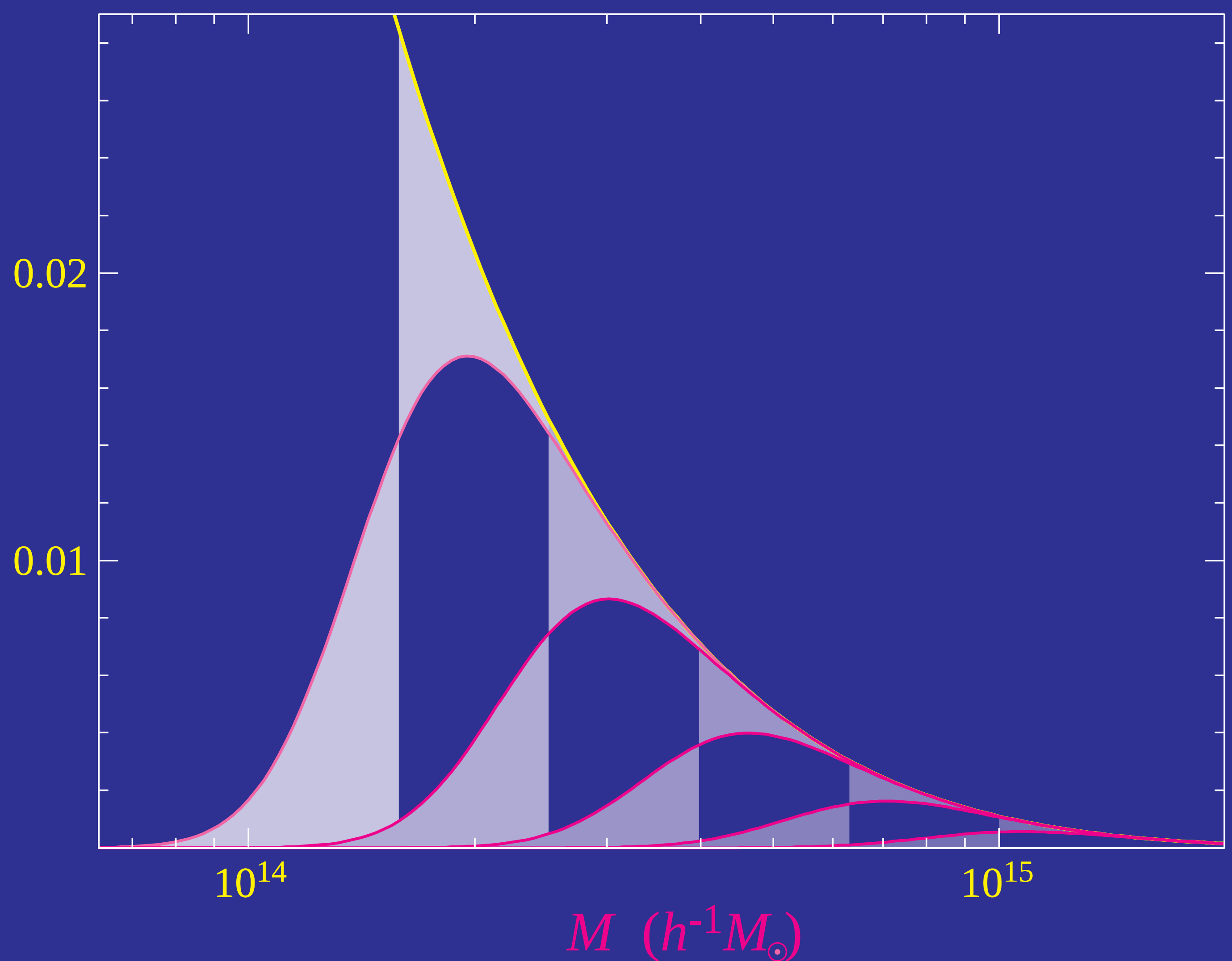
# Selection Bias

- Clusters upscattered into threshold



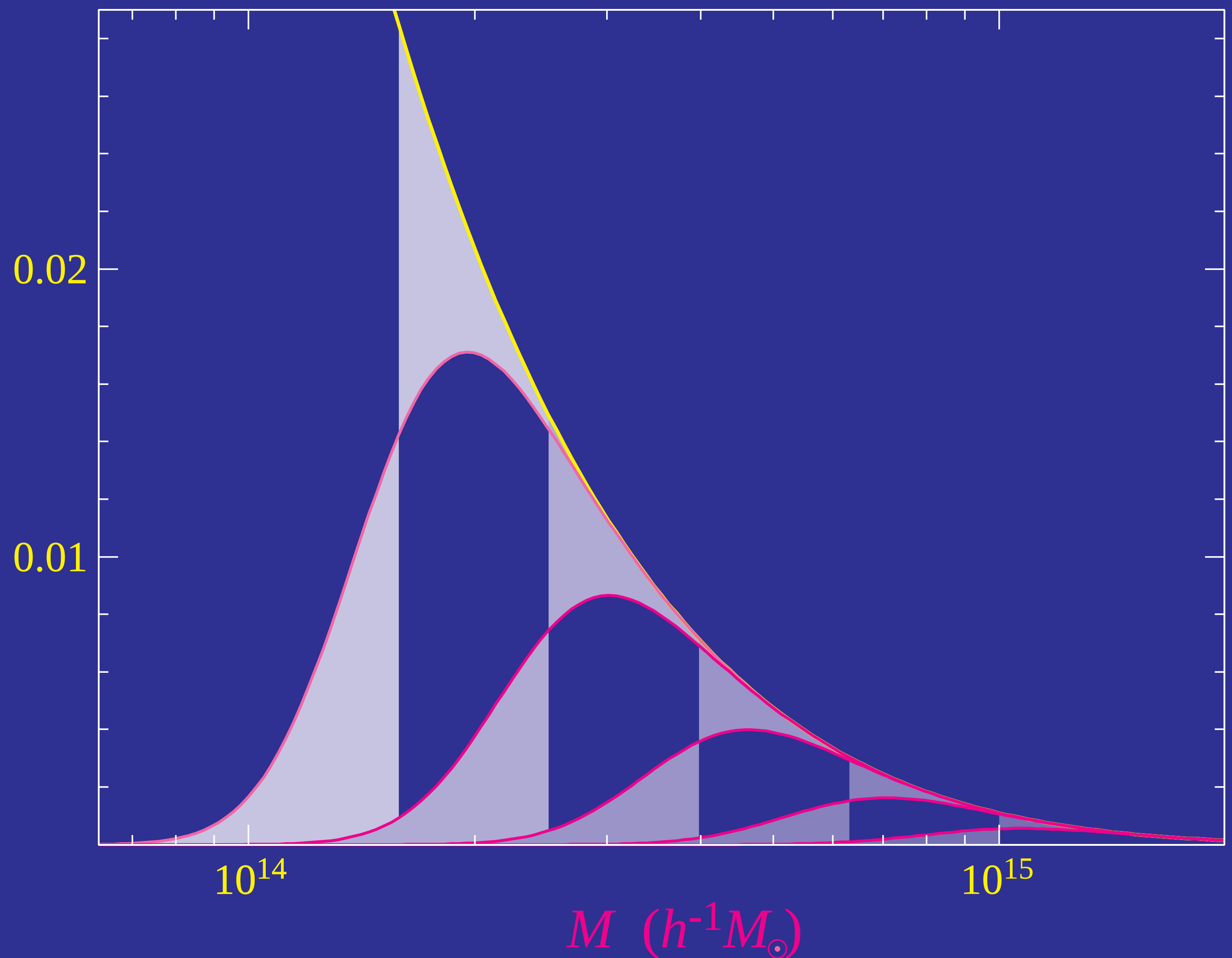
# Selection Bias

- Clusters upscattered into threshold
- Out number downscattered across threshold



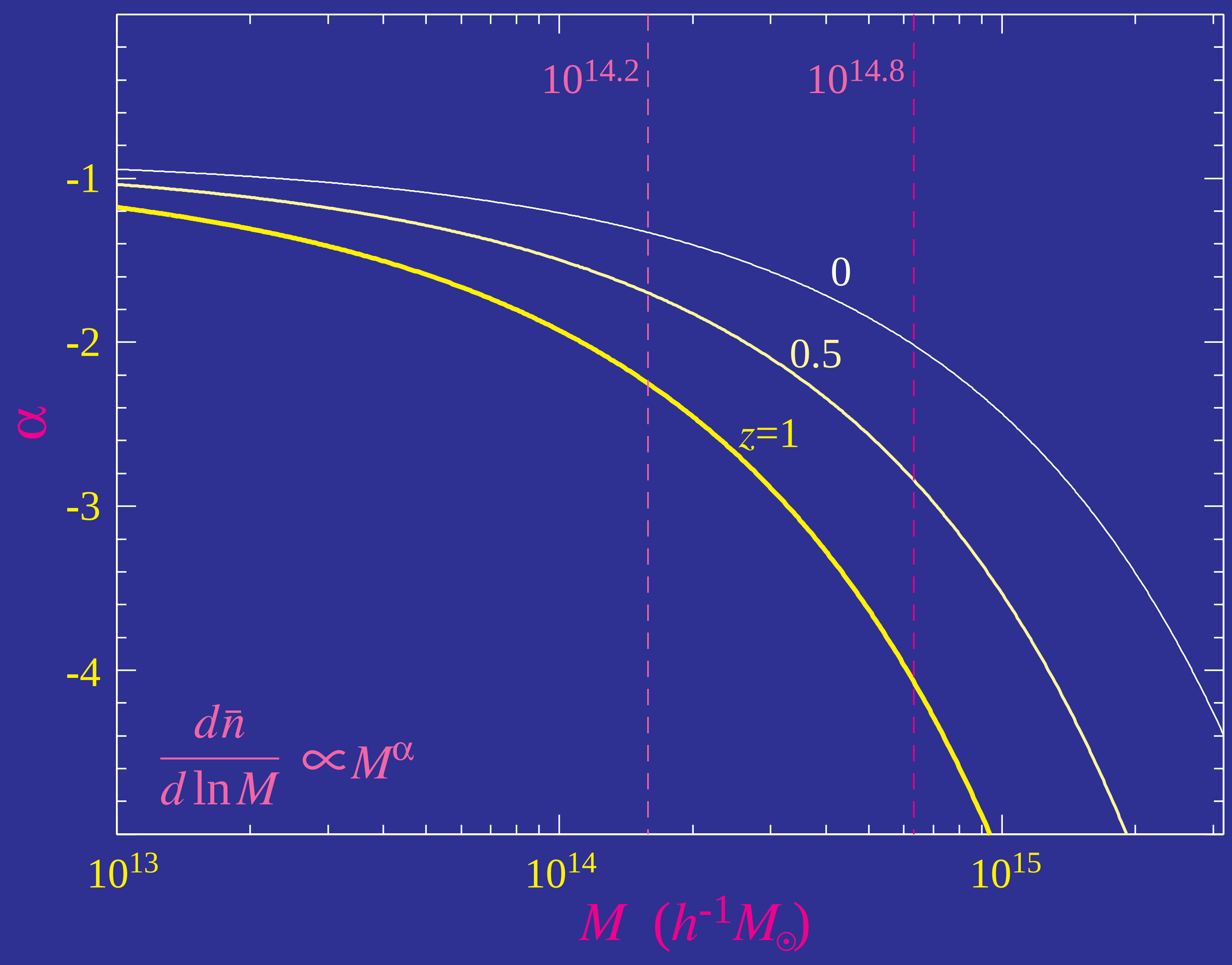
# Selection Bias

- Bias proportional to variance of distribution and mass function slope
- Introduces trend in redshift even if scatter is constant



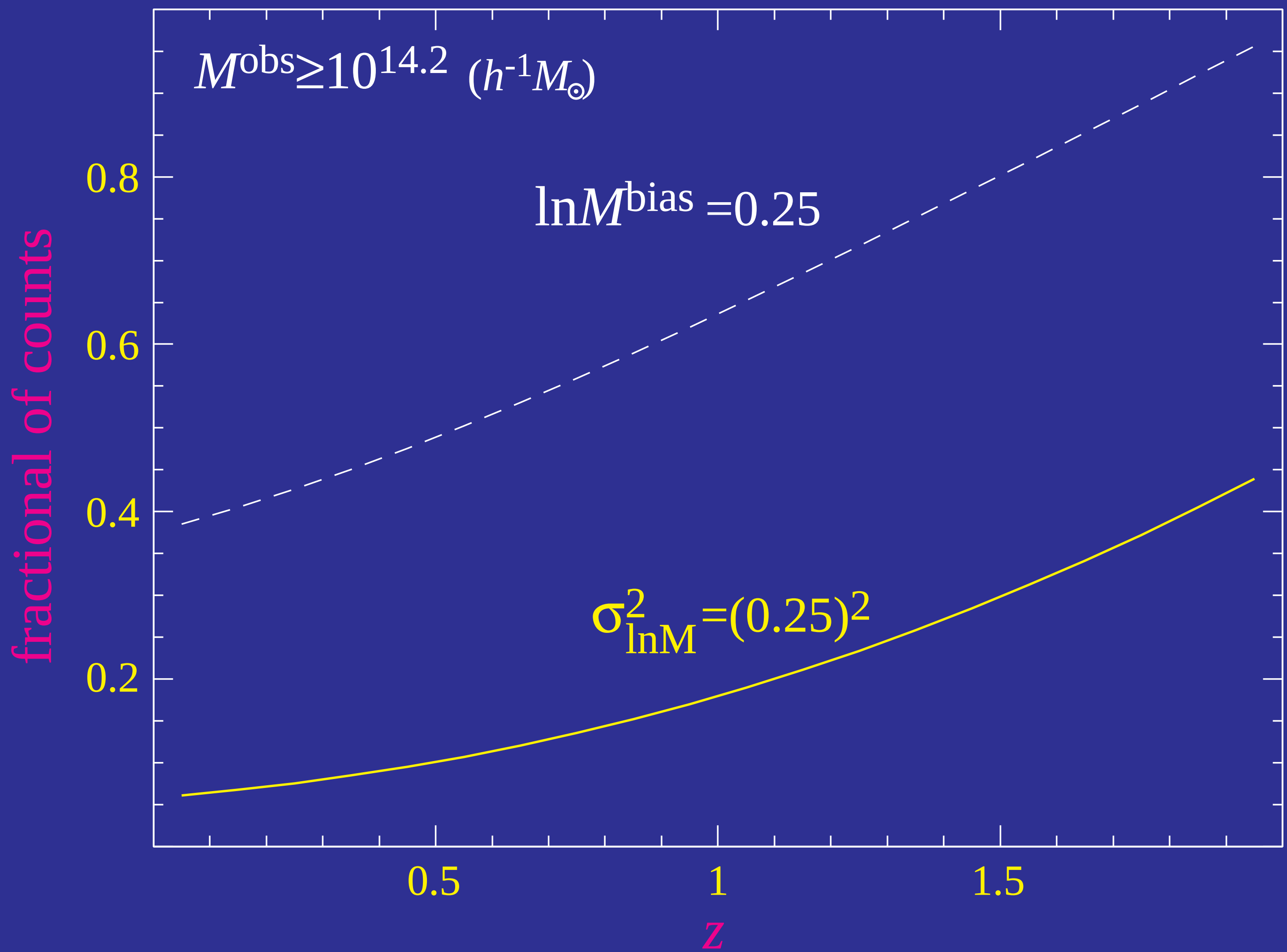
# Relative Importance of Scatter

- In the small scatter limit, relative importance of variance vs. bias proportional to local power law slope of mass function
- Increases with increasing mass or redshift



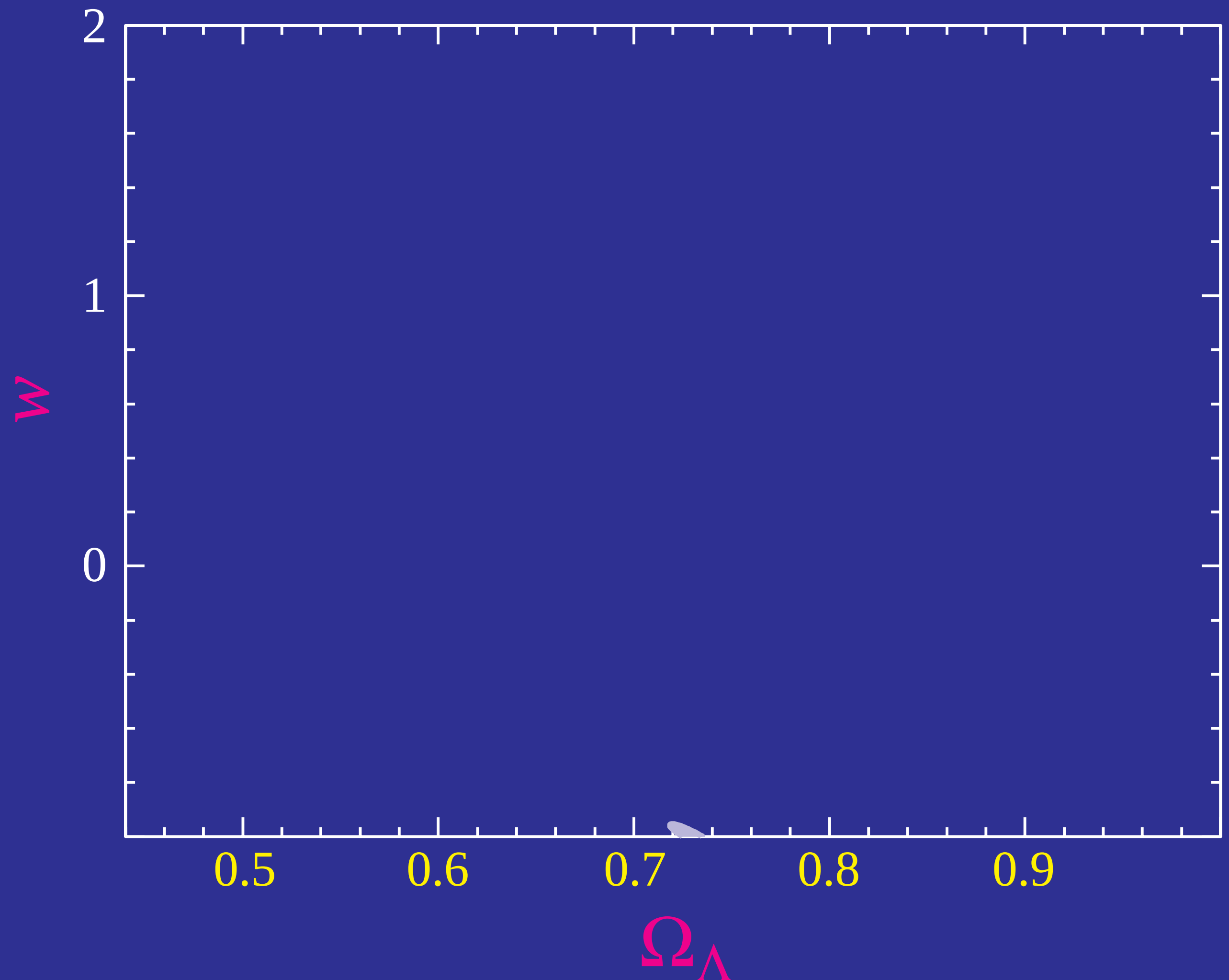
# Sensitivity to Uncertainties

- A 25% bias would produce a ~100% change in high-z cluster counts
- A 25% scatter a ~50% change - but scales as variance



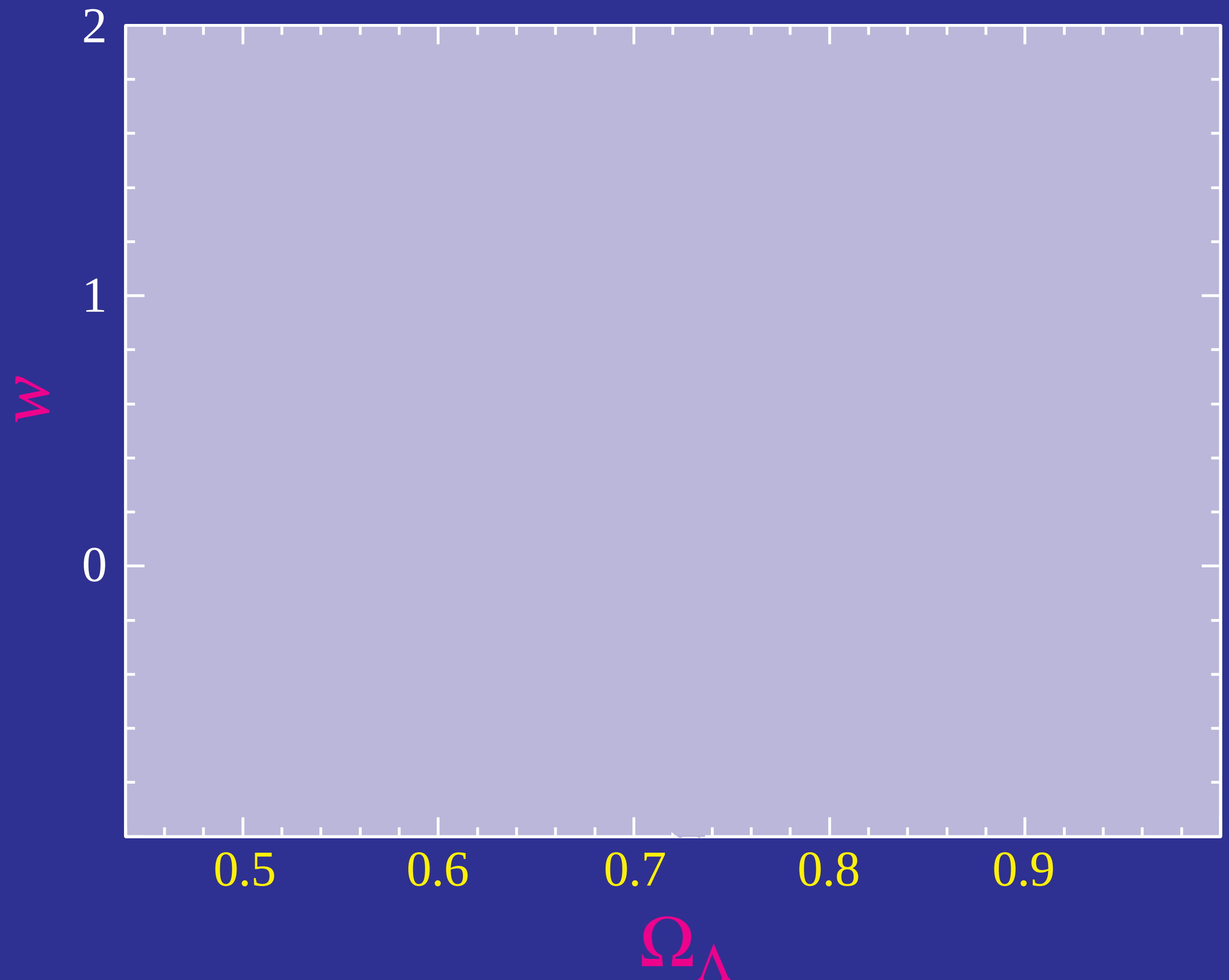
# Fully Calibrated

- Given a completely known observable-mass distribution dark energy constraints are quite tight (4000 sq deg, $z$<2)



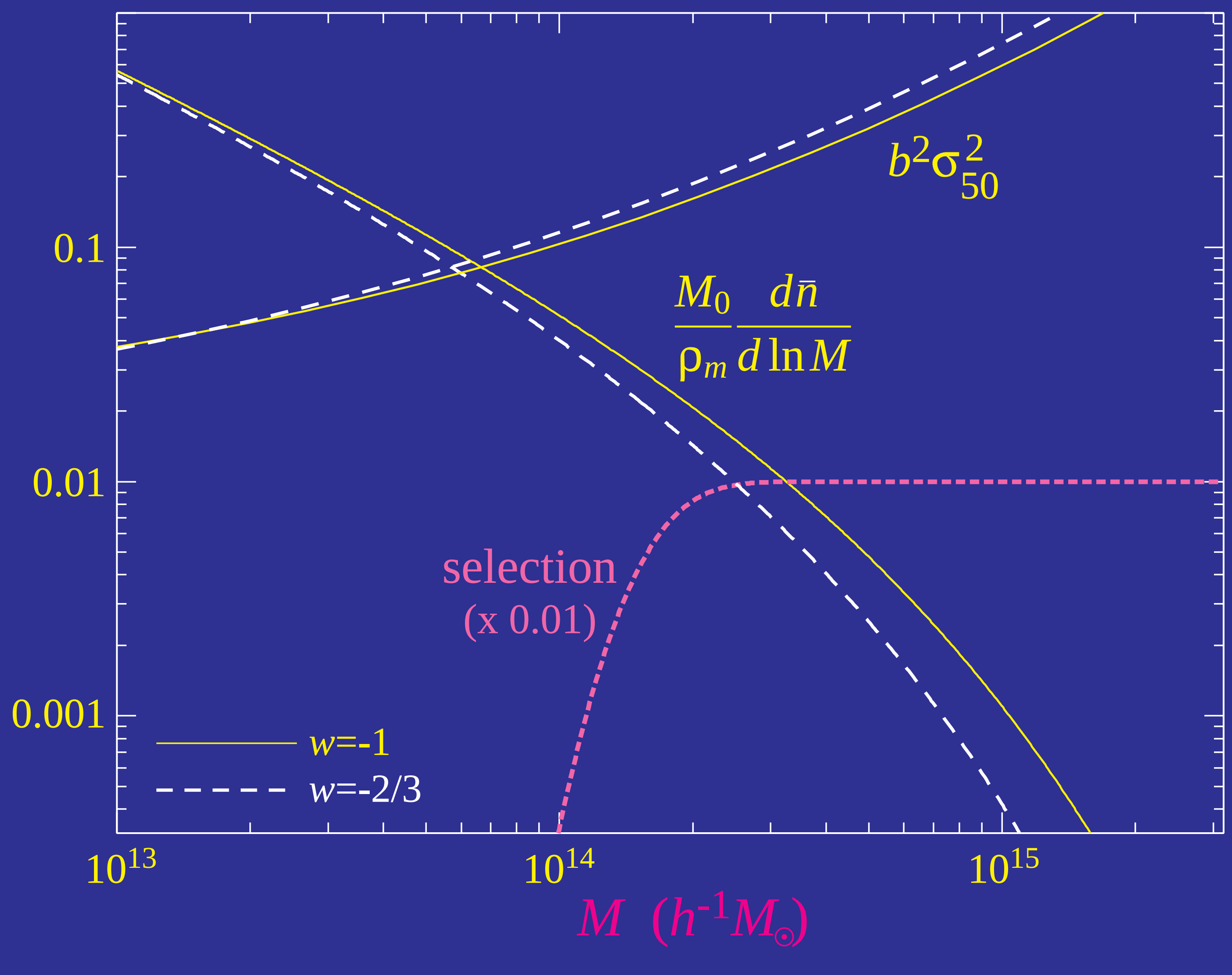
# Un-Calibrated

- Marginalizing scatter (linear $z$ evolution) and bias (power law evolution) destroys all dark energy information



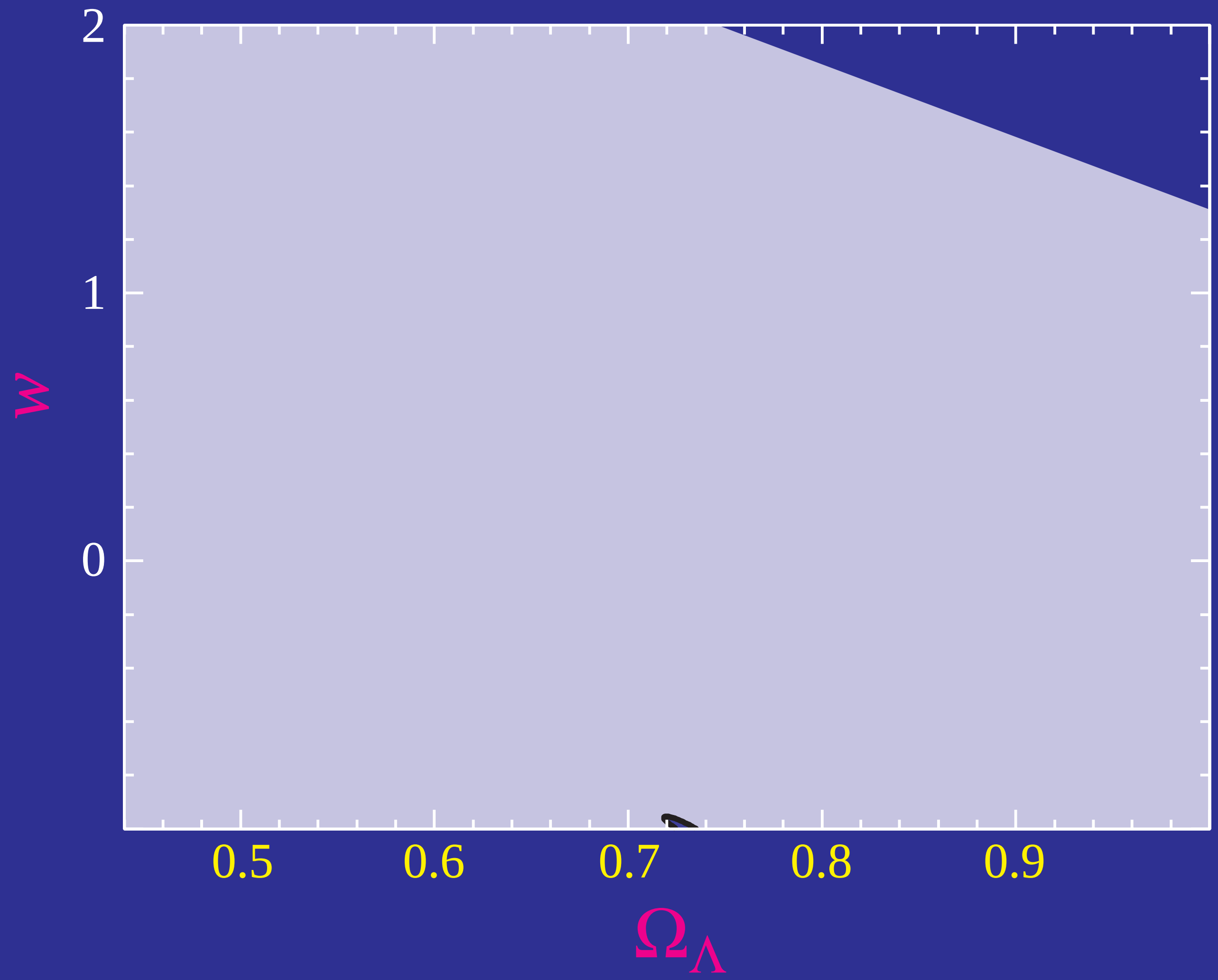
# Self-Calibration with Clustering

- Clustering bias as a function of mass is predicted in a cosmology
- Angular clustering of clusters or (co)variance of counts provides mass bias calibration but not jointly with scatter



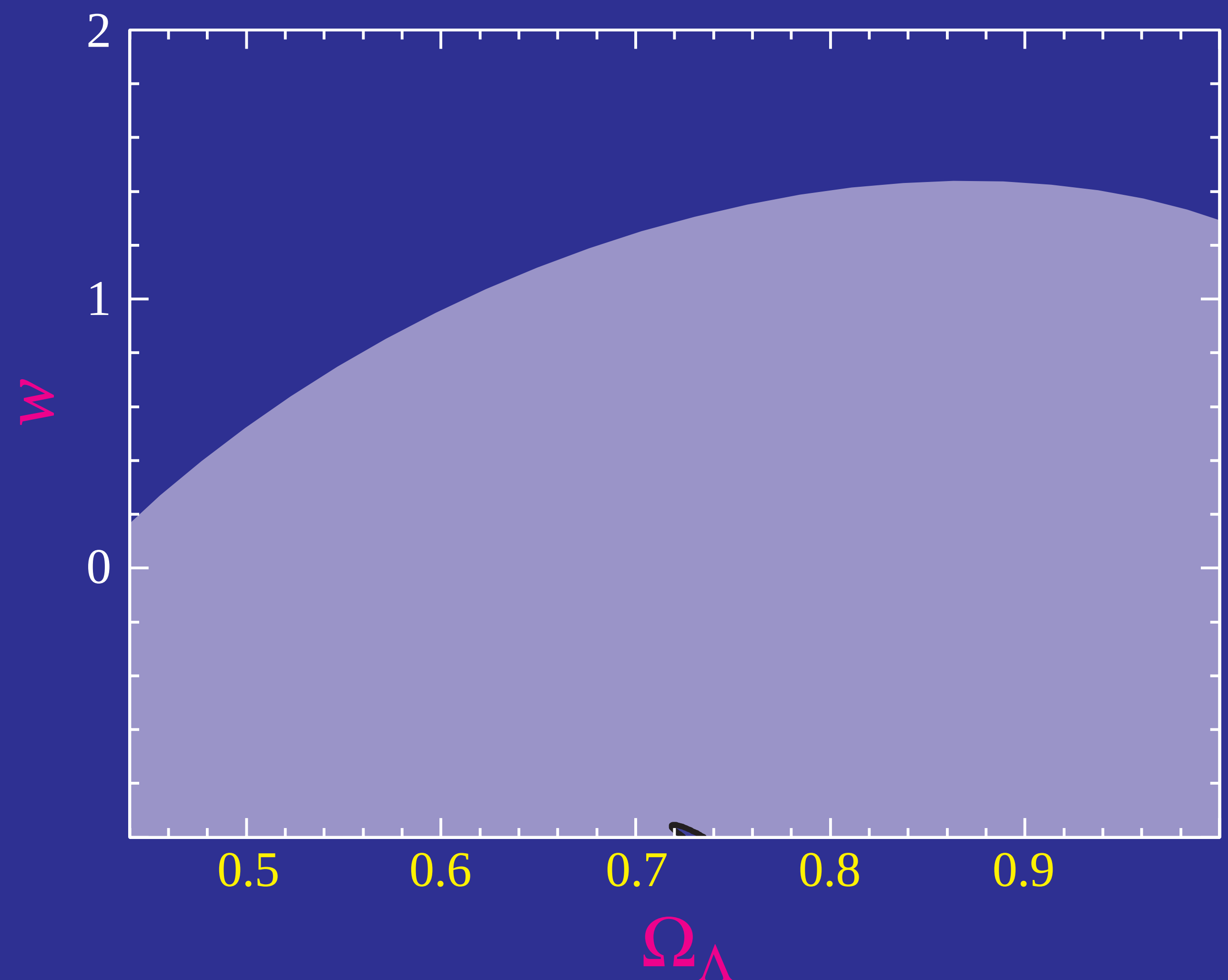
# Self-Calibration with Clustering

- Arbitrary evolution of bias and scatter in 20 bins of $\Delta z$=0.1



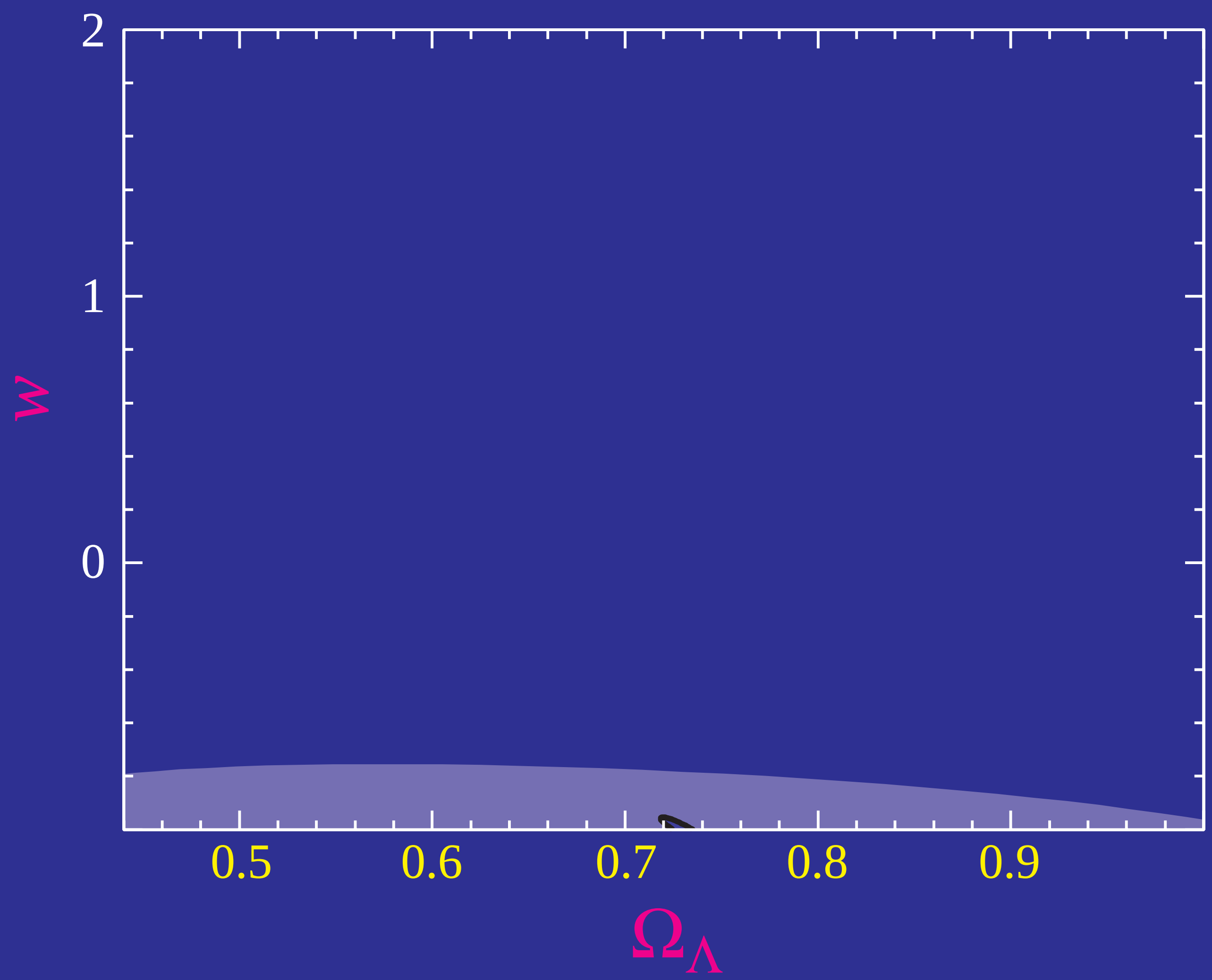
# Self-Calibration with Clustering

- Power law evolution of bias and arbitrary evolution of scatter in 20 bins of $\Delta z$=0.1



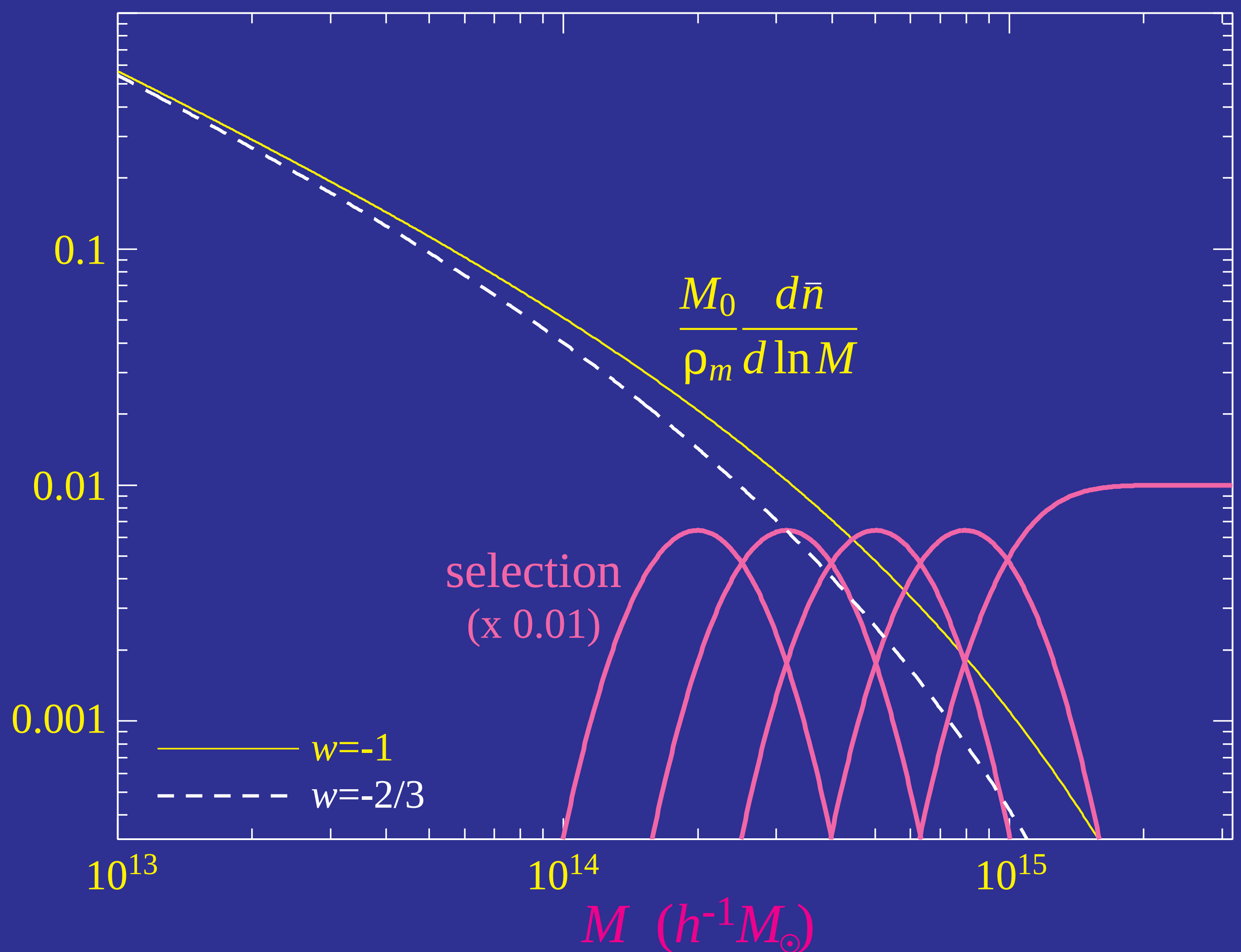
# Self-Calibration with Clustering

- Power law evolution of bias and cubic evolution of scatter in $z$



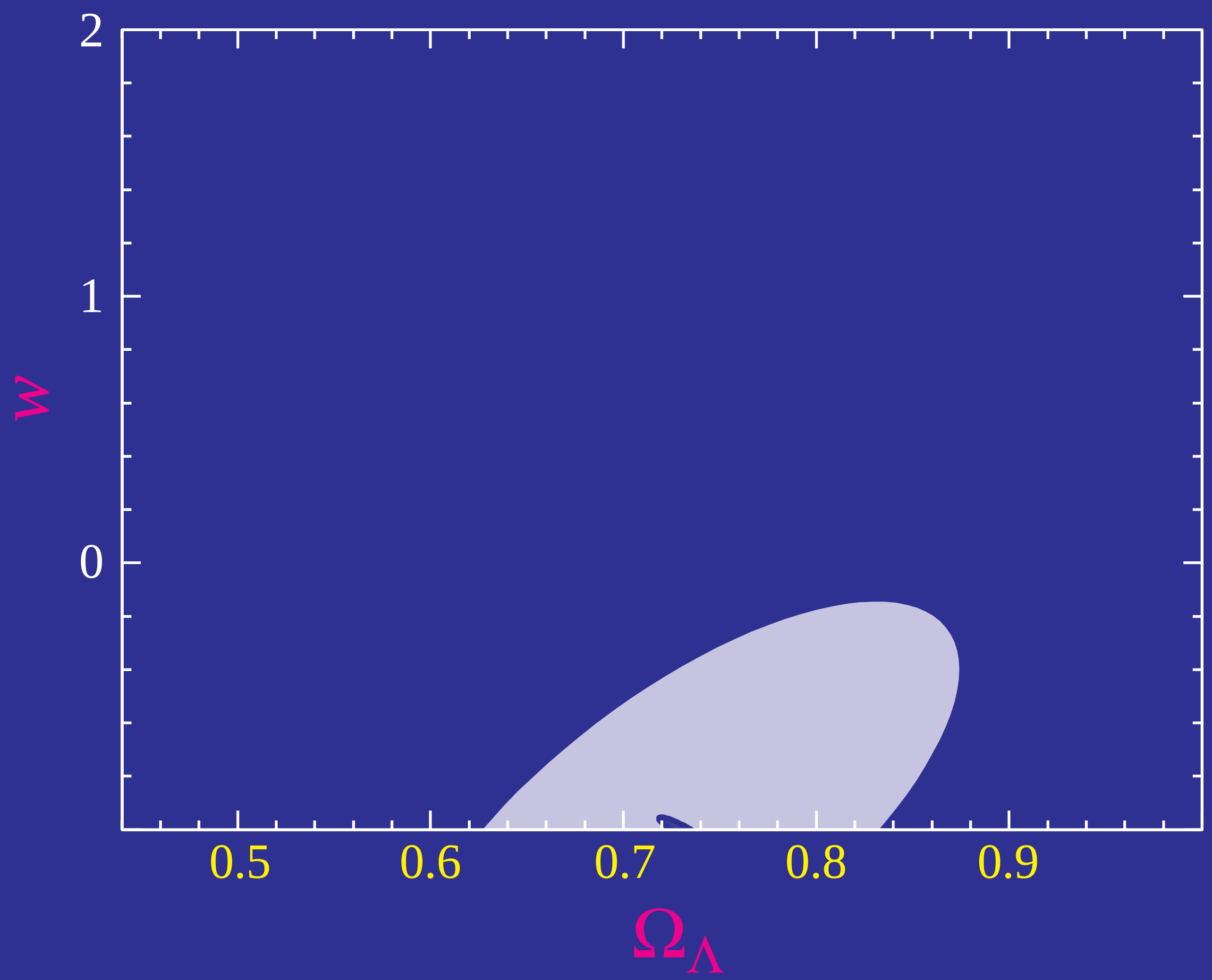
# Observable Mass Bins

- Exploit knowledge by breaking sample into observable mass bins
- Demand consistent count ratio to solve for bias and scatter



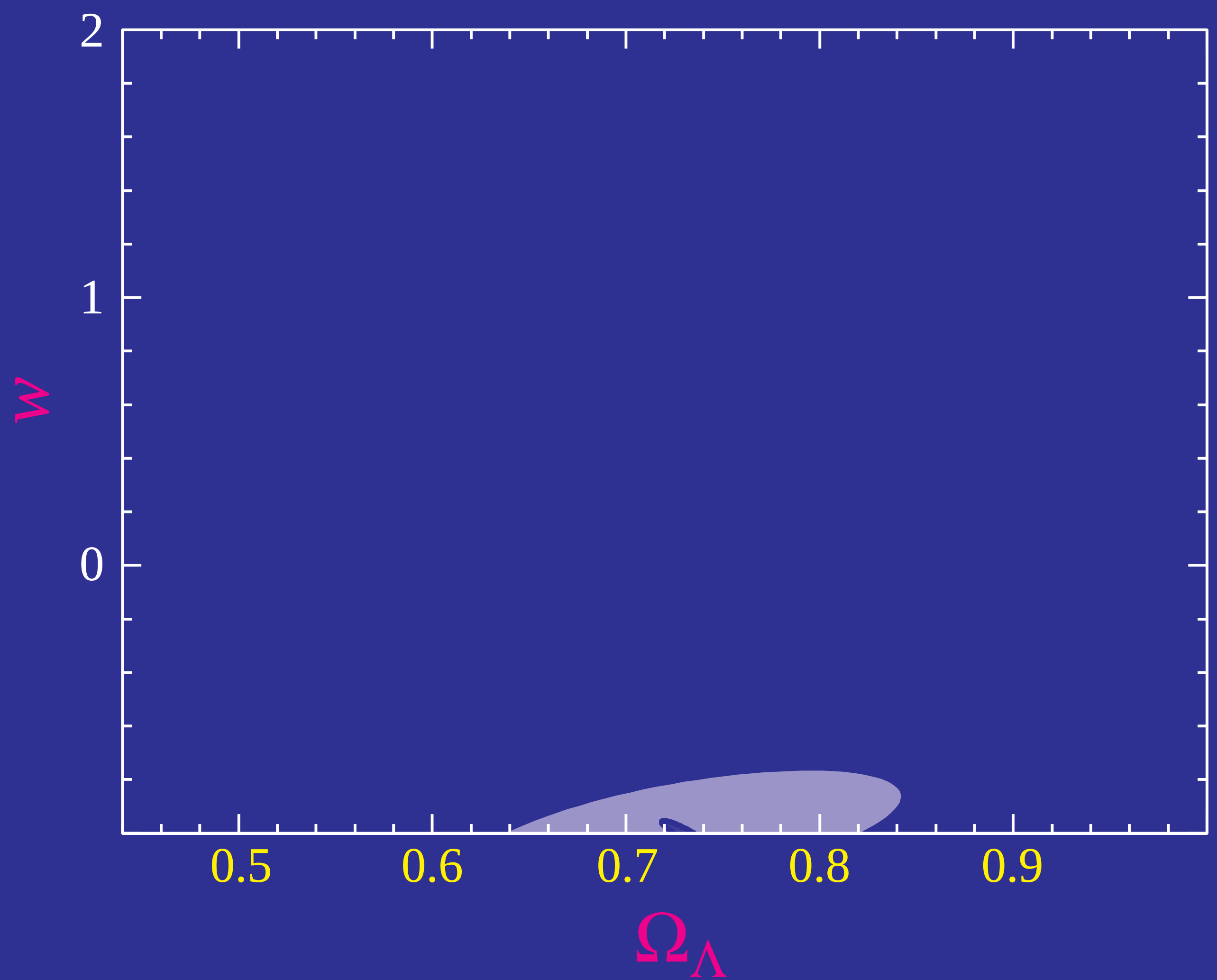
# Self-Calibration with Binning

- Arbitrary evolution of bias and scatter in 20 bins of $\Delta z$=0.1



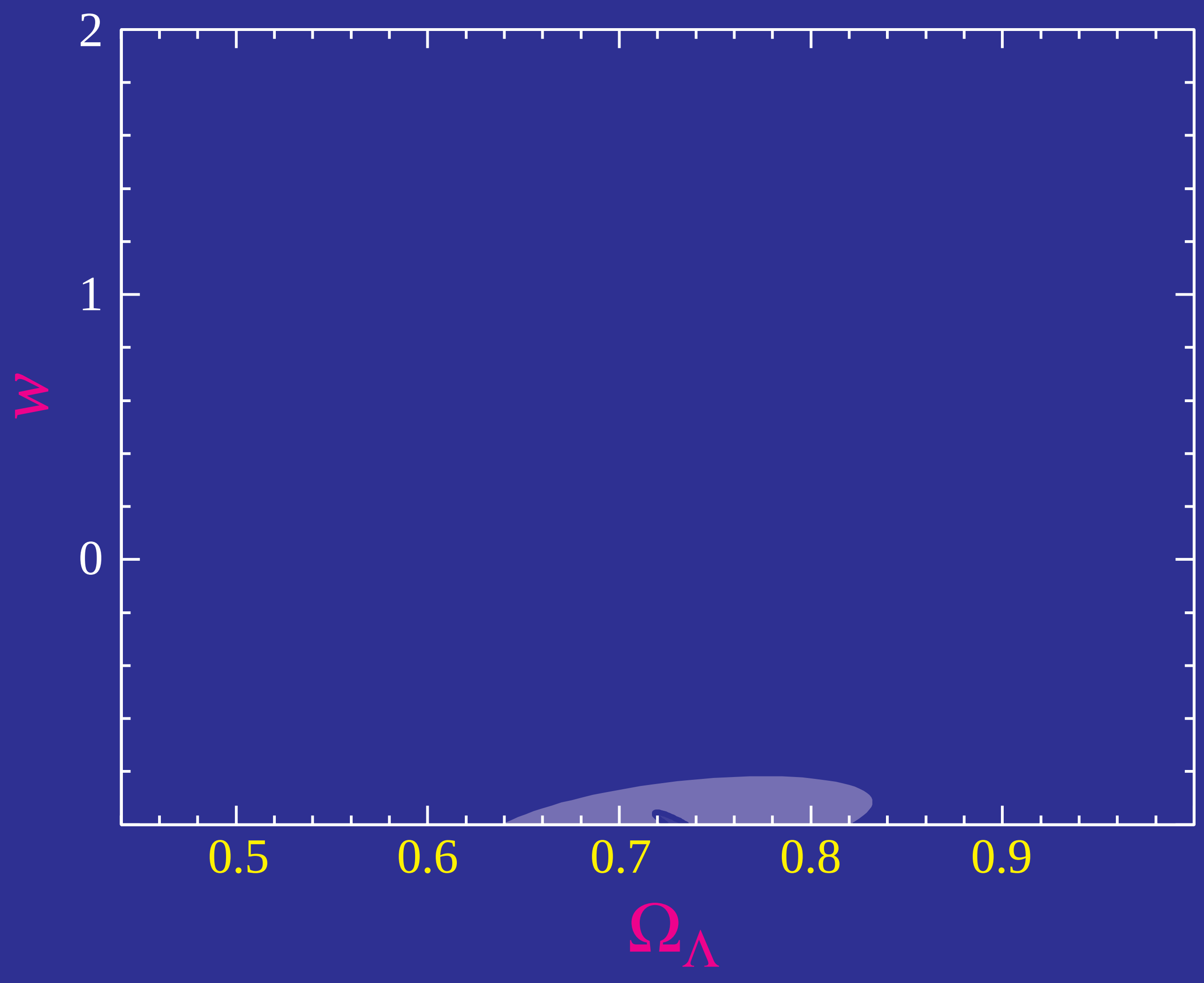
# Self-Calibration with Binning

- Power law evolution of bias and arbitrary evolution of scatter in 20 bins of $\Delta z$=0.1



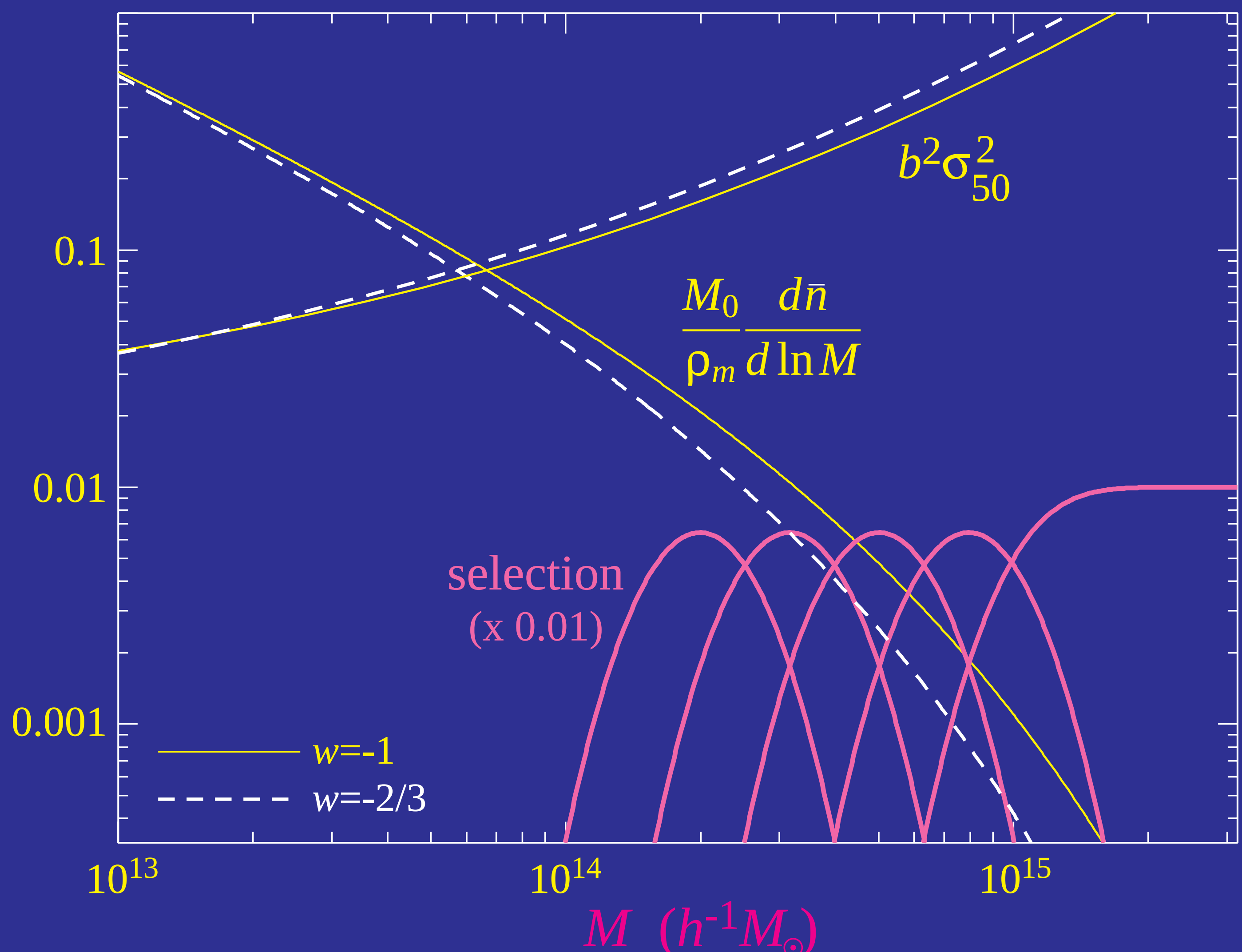
# Self-Calibration with Binning

- Power law evolution of bias and cubic evolution of scatter in $z$



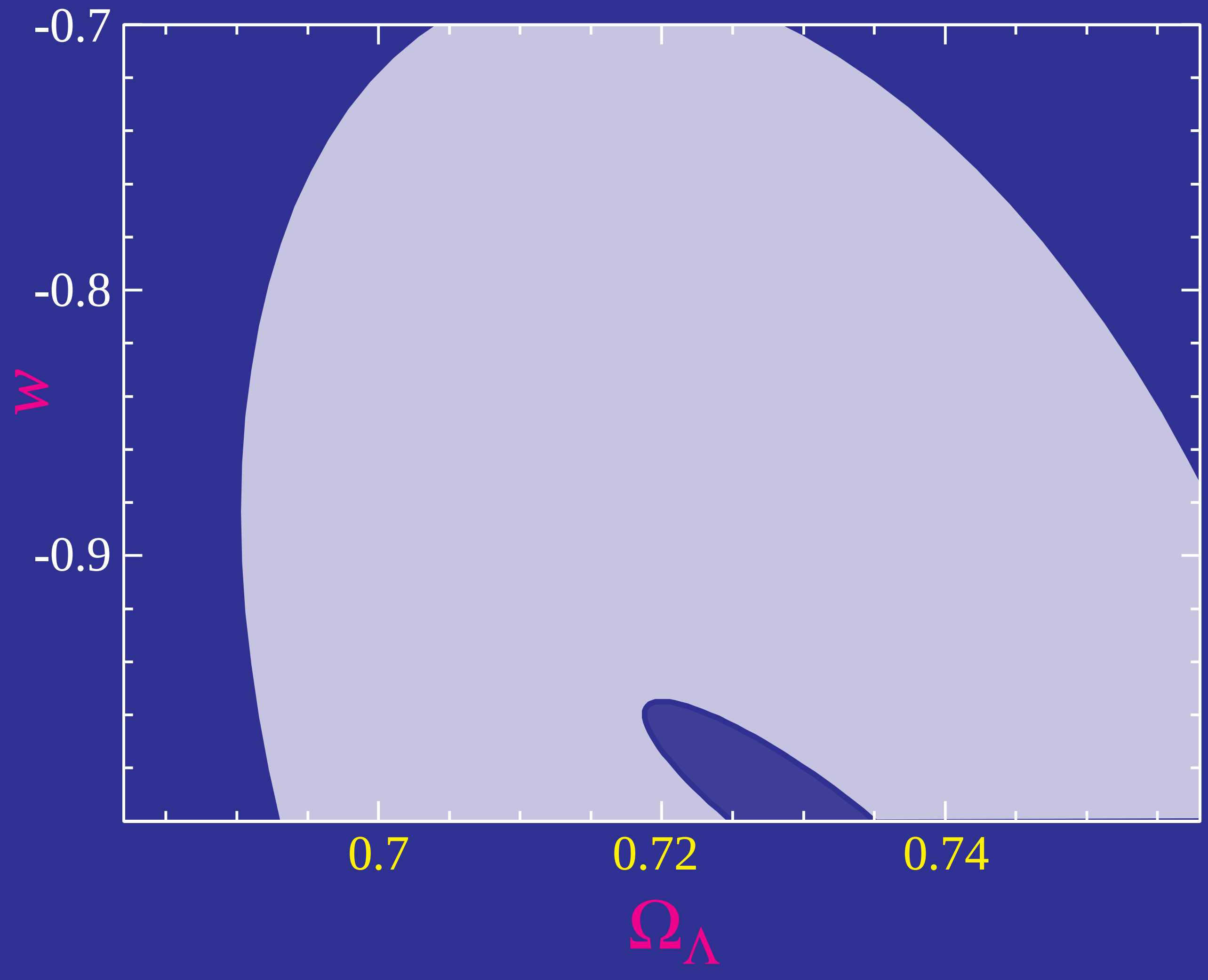
# Joint Self-Calibration

- Both counts and their variance as a function of binned observable
- Many observables allows for a joint solution of a mass independent bias and scatter with cosmology



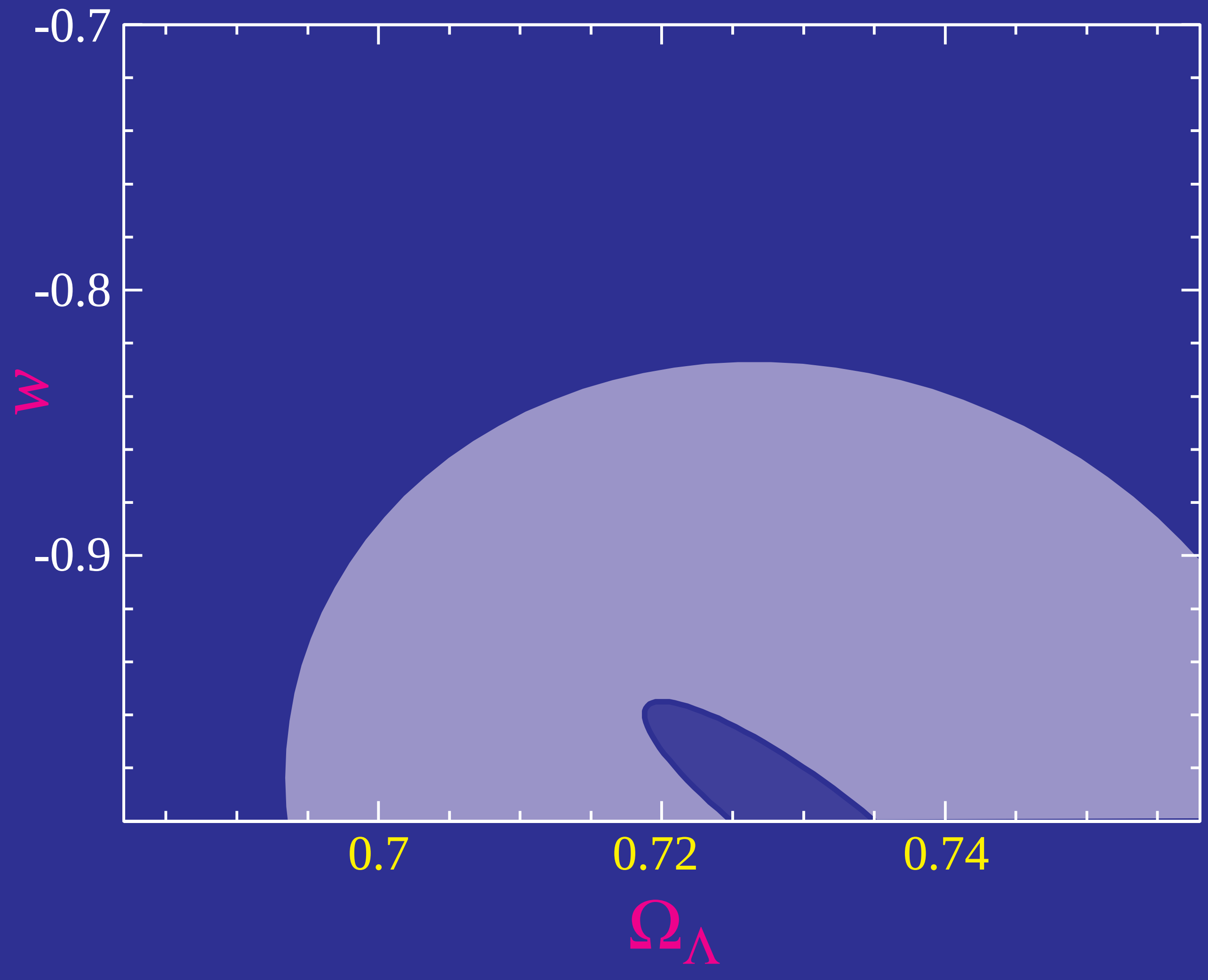
# Joint Self Calibration

- Arbitrary evolution of bias and scatter in 20 bins of $\Delta z$=0.1



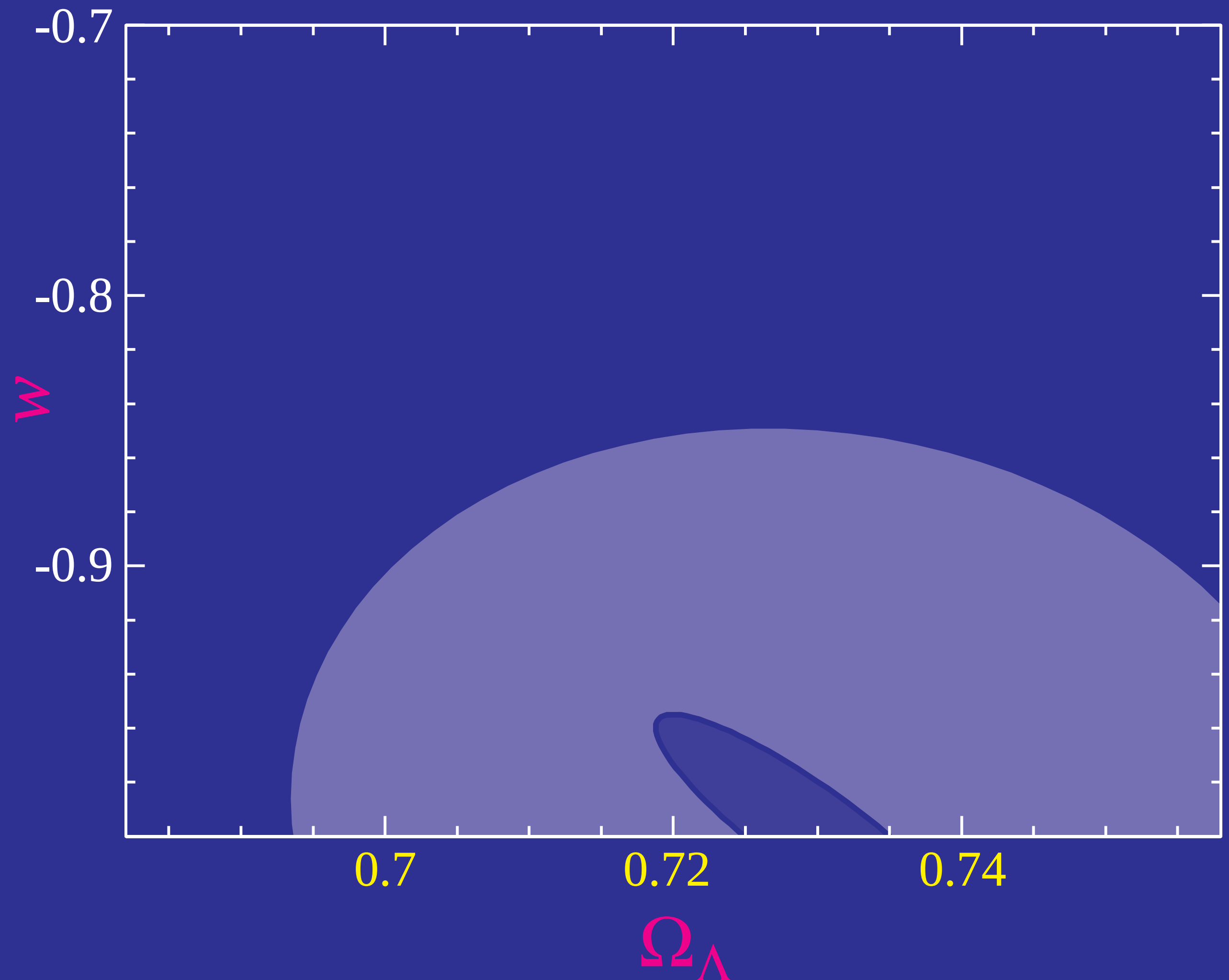
# Joint Self Calibration

- Power law evolution of bias and arbitrary evolution of scatter in 20 bins of $\Delta z$=0.1



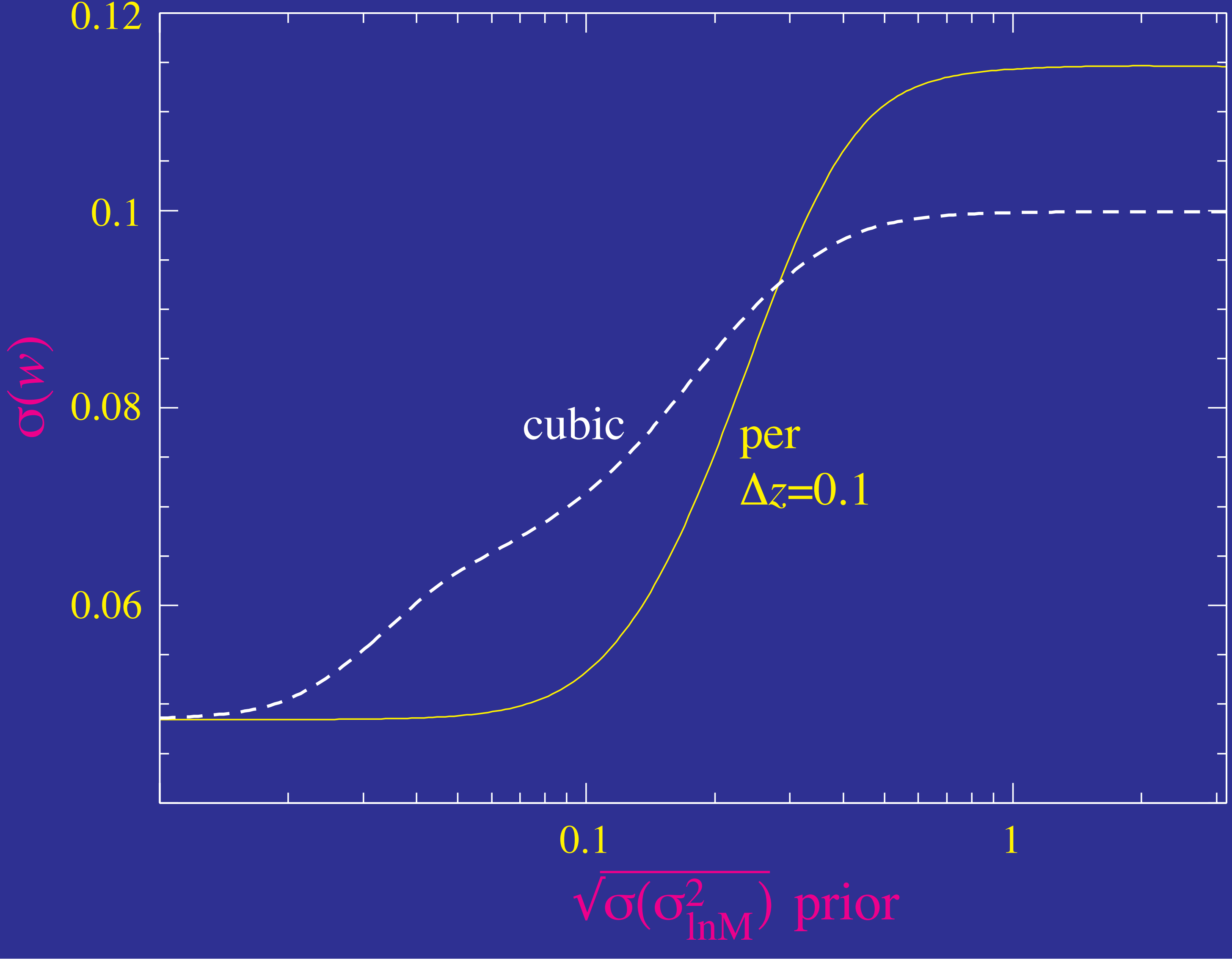
# Joint Self Calibration

- Power law evolution of bias and cubic evolution of scatter in $z$



# Prior Knowledge of Scatter

- Priors on the 20 independent scatter parameters of 10% each
- Or 2% on the evolution of scatter to $z$~1 improves constraints x2 beyond self-calibration



# Forecasts: Scatters with Partial Clearing

- Unknown scatter at the 10% level at z>1 will significantly degrade the cosmological utility of such clusters
- Self-calibration from the power spectrum or clustering of clusters alone is insufficient to solve internally for both a bias and a scatter
- Self-calibration from the shape of the counts in the observable can jointly provide for calibration with a sufficiently deep sample
- External calibration will assist self calibration at the level of 2-10% scatter uncertainties at z~1

- Caveats:

  trends in the distribution versus the mass must be known and taken out

  non-Gaussian tails in the distribution must be understood

  self calibration ↔ self consistency

  divide up data in as many ways as possible, check assumptions!