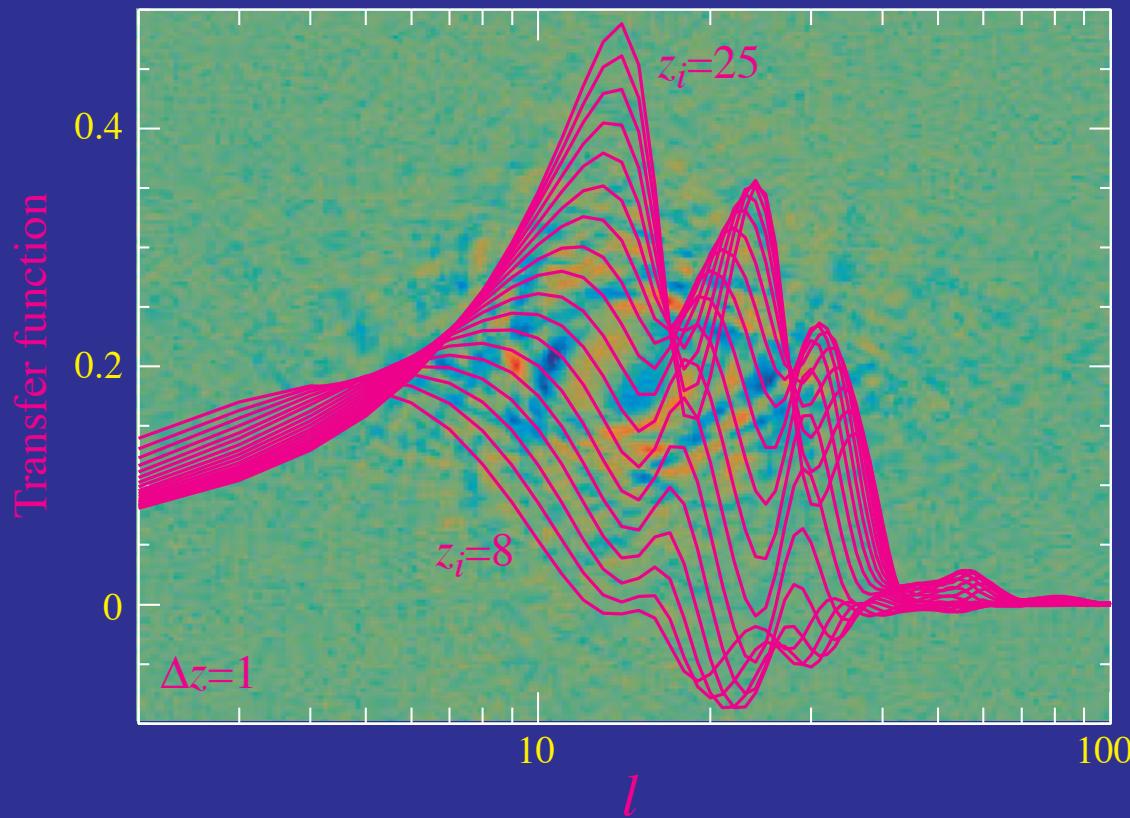


# Secondary Polarization



Reionization and Gravitational Lensing

*Wayne Hu*

Minnesota, March 2003

# Outline

- Reionization Bump

- Model independent treatment of ionization history

- Linear response and the inverse problem

- Compact representation in principal components

- Unbiased measurement of initial amplitude

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- Minimum variance estimator

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- Collaborators:

- Matt Hedman

- Gil Holder

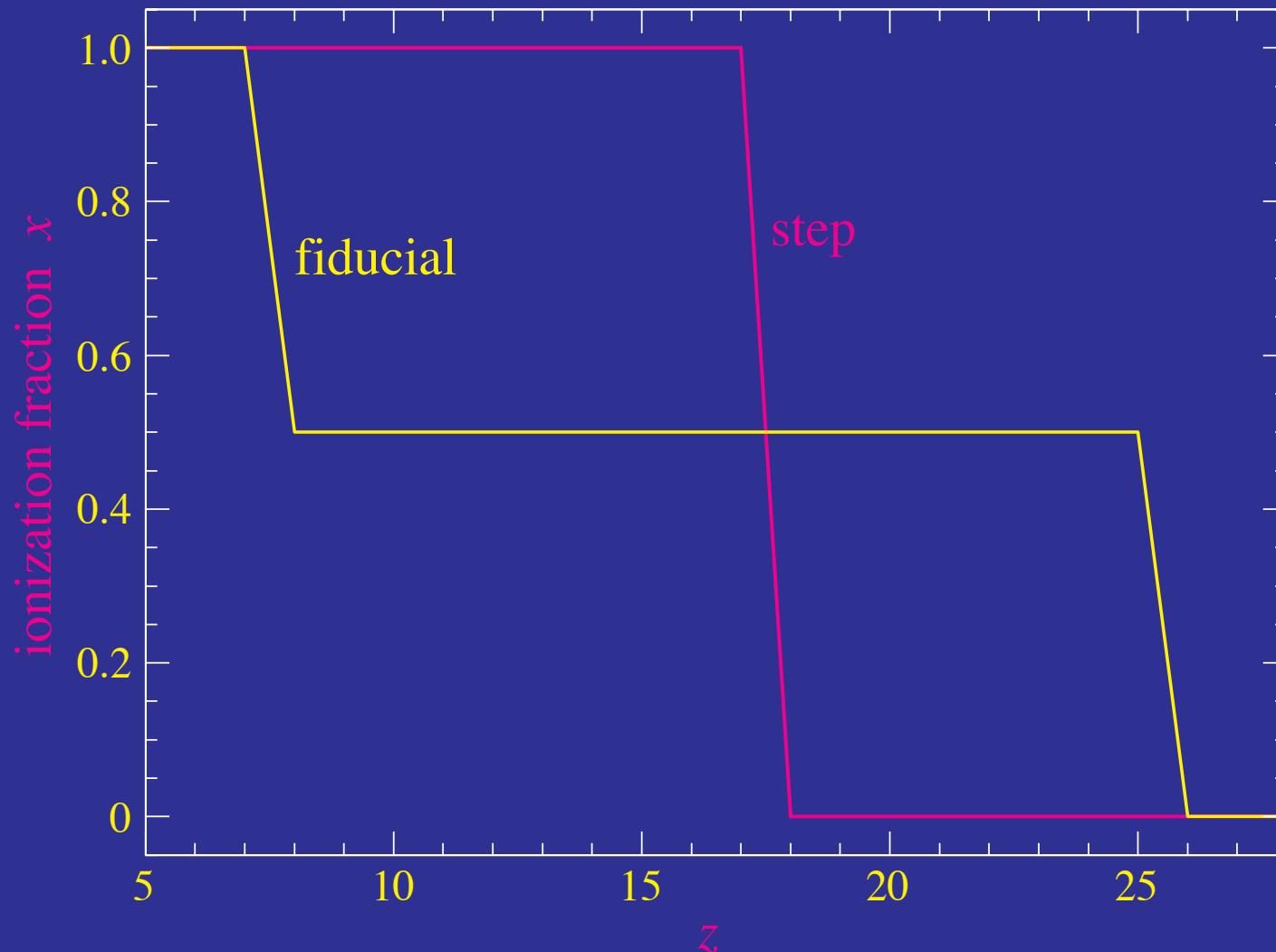
- Takemi Okamoto

- Matias Zaldarriaga

# Reionization

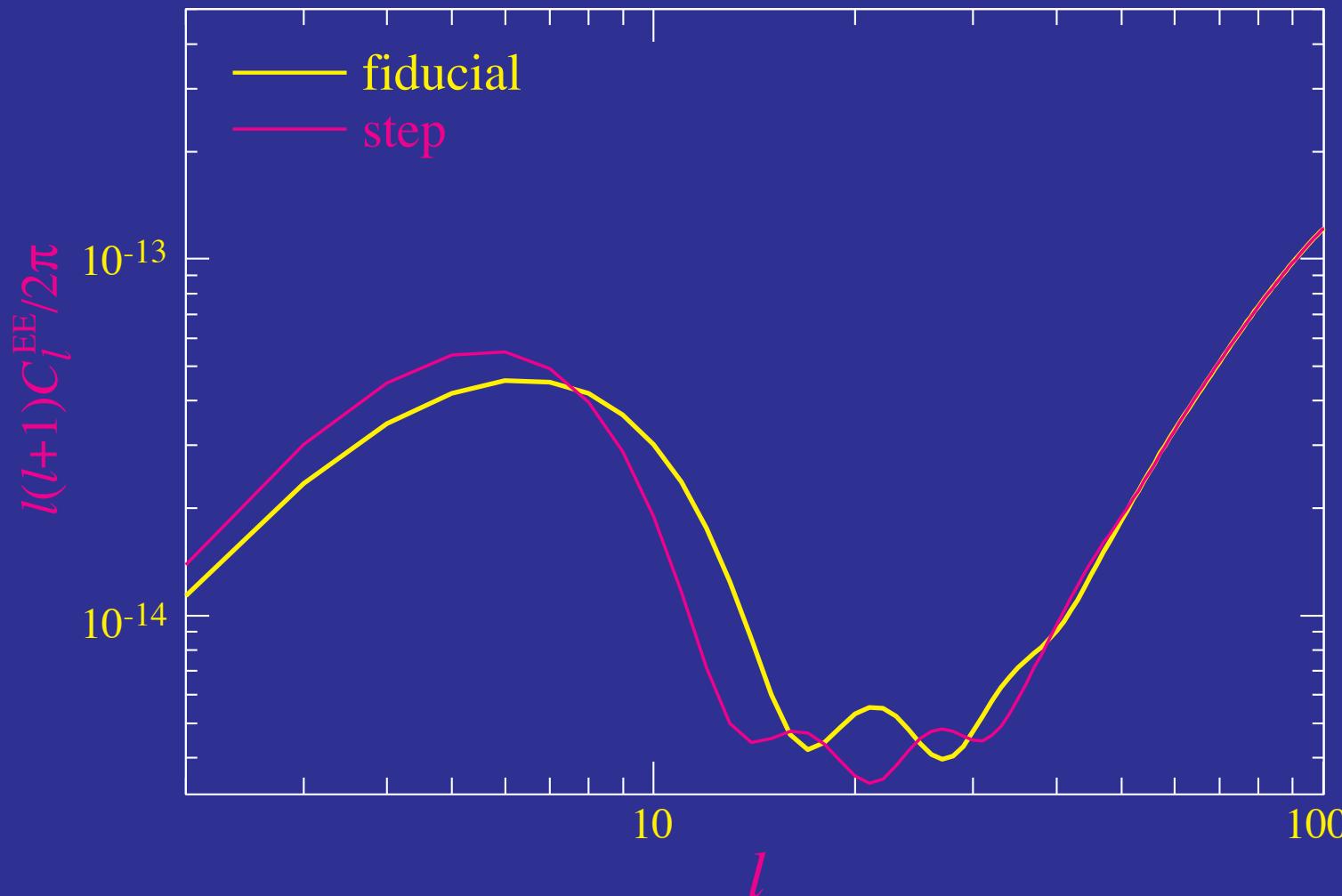
# Ionization History

- Two models with same optical depth  $\tau$  but different ionization history



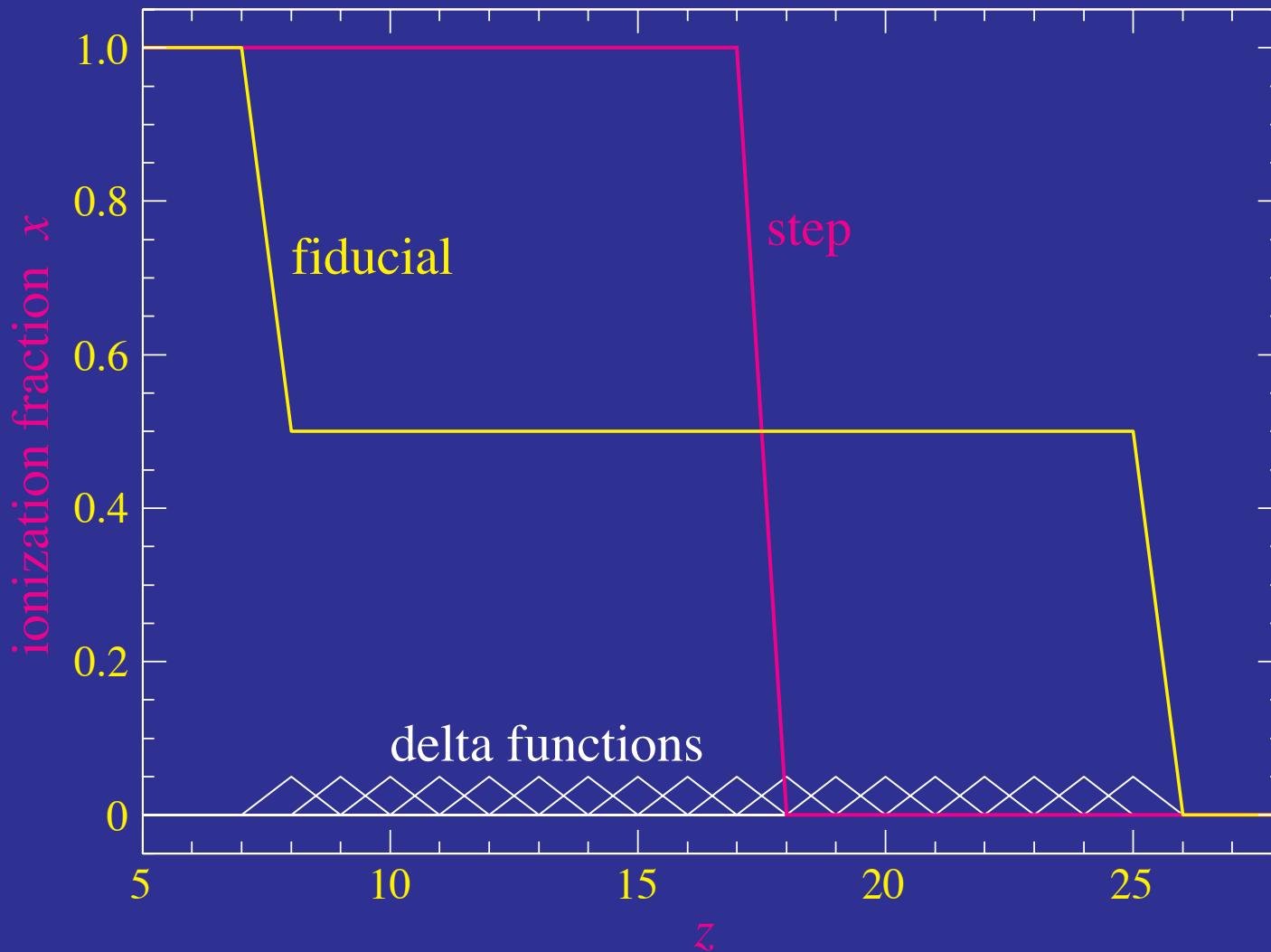
# Distinguishable History

- Same optical depth, but different coherence - horizon scale during scattering epoch



# Complete Basis

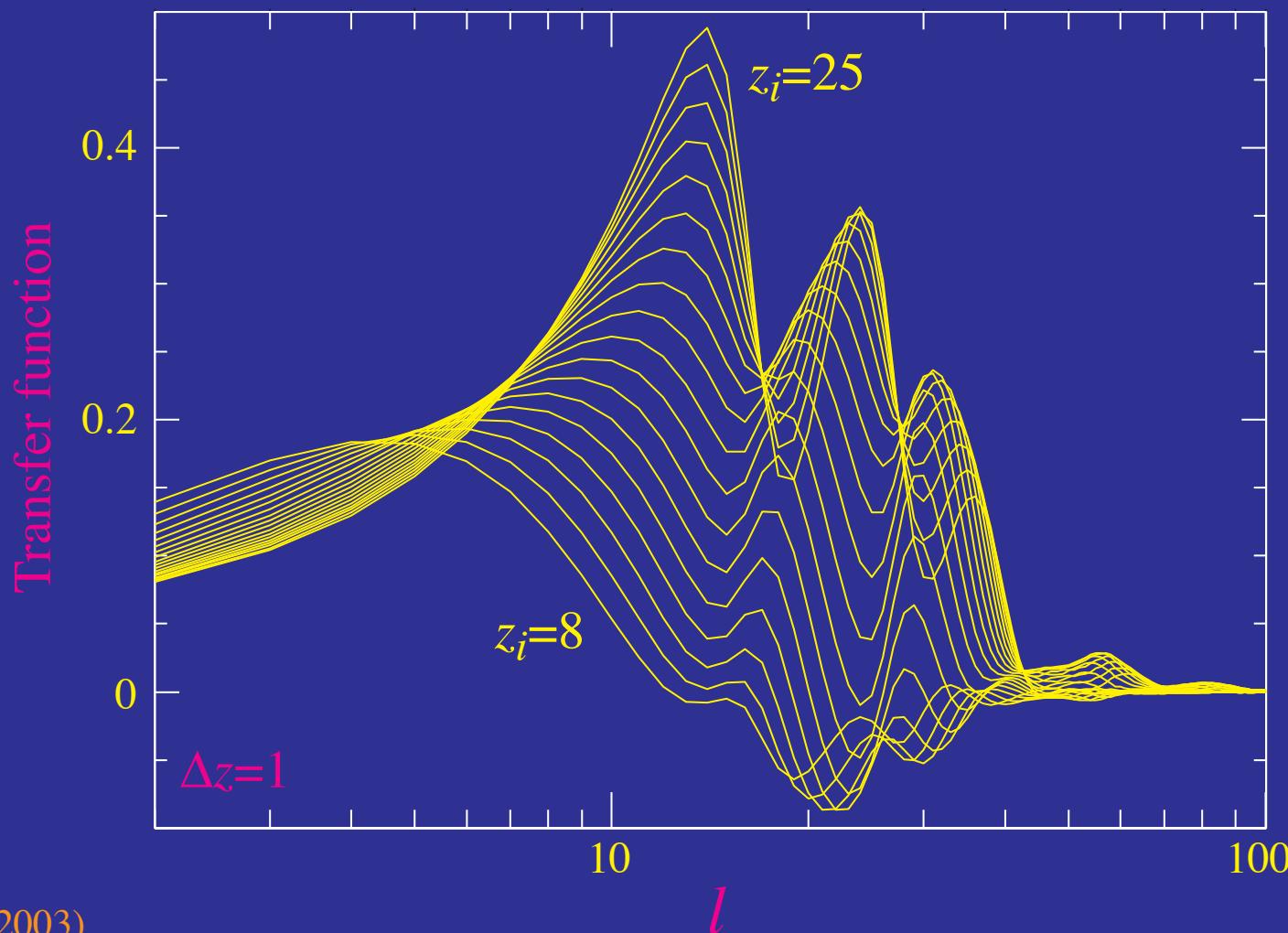
- Define a complete representation of the ionization history in the discrete (linear interpolation) approximation



# Transfer Function

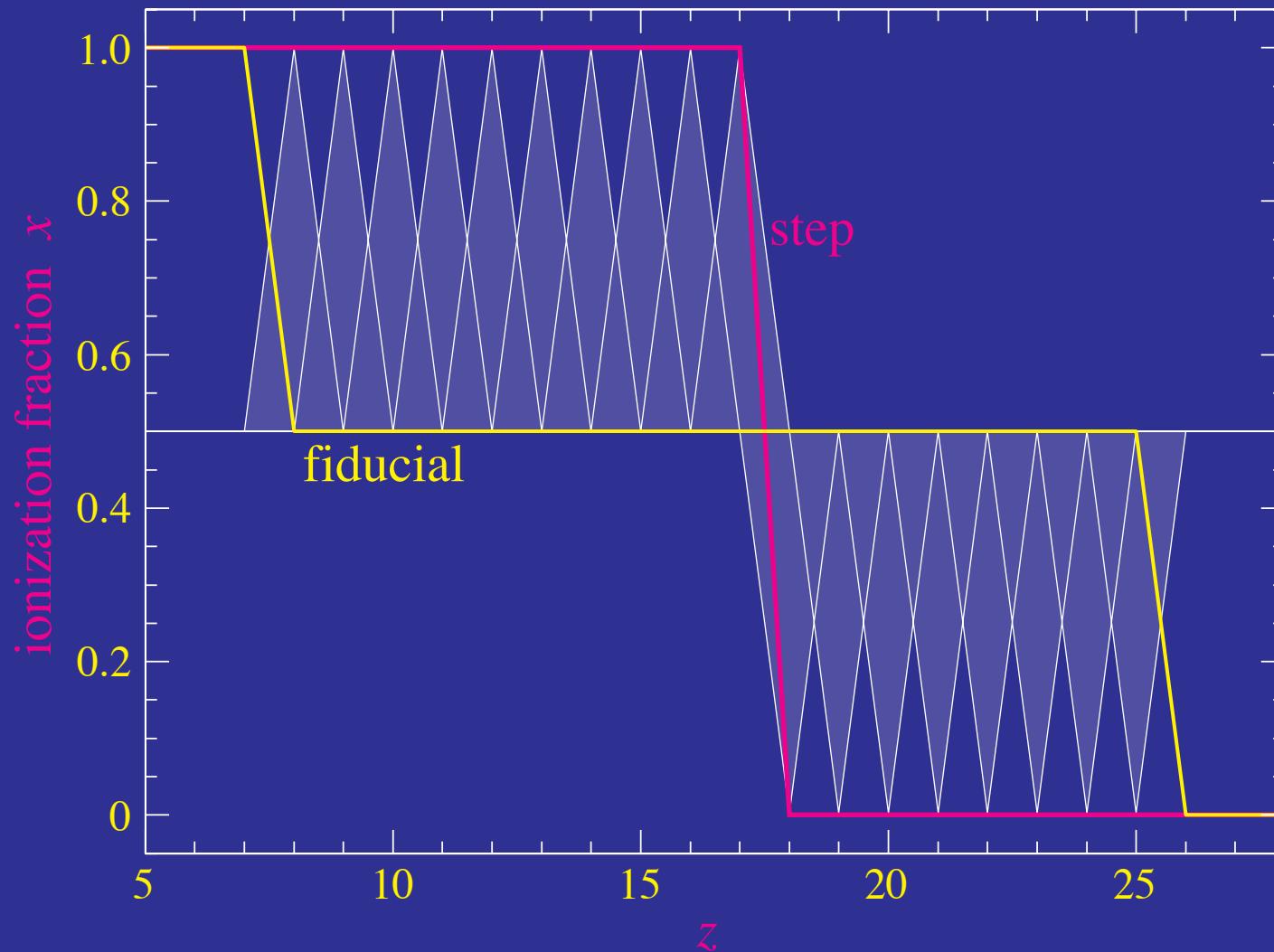
- Linearized response to delta function ionization perturbation

$$T_{\ell i} \equiv \frac{\partial \ln C_\ell^{EE}}{\partial x(z_i)}, \quad \delta C_\ell^{EE} = C_\ell^{EE} \sum_i T_{\ell i} \delta x(z_i)$$



# Linear Response

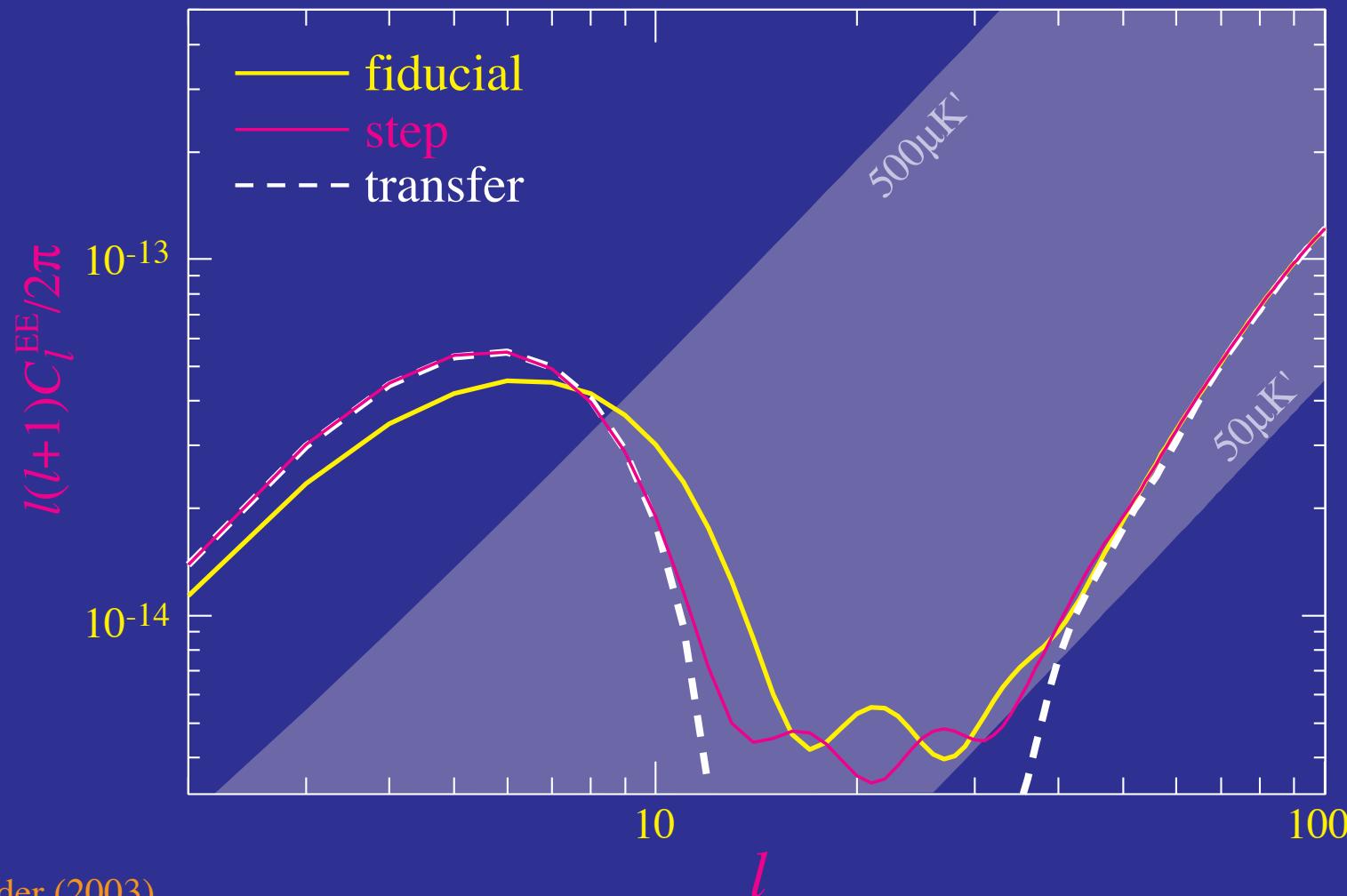
- Worst case scenario: maximal perturbations from fiducial model



# Linear Response

- Worst case scenario: maximal perturbations from fiducial model

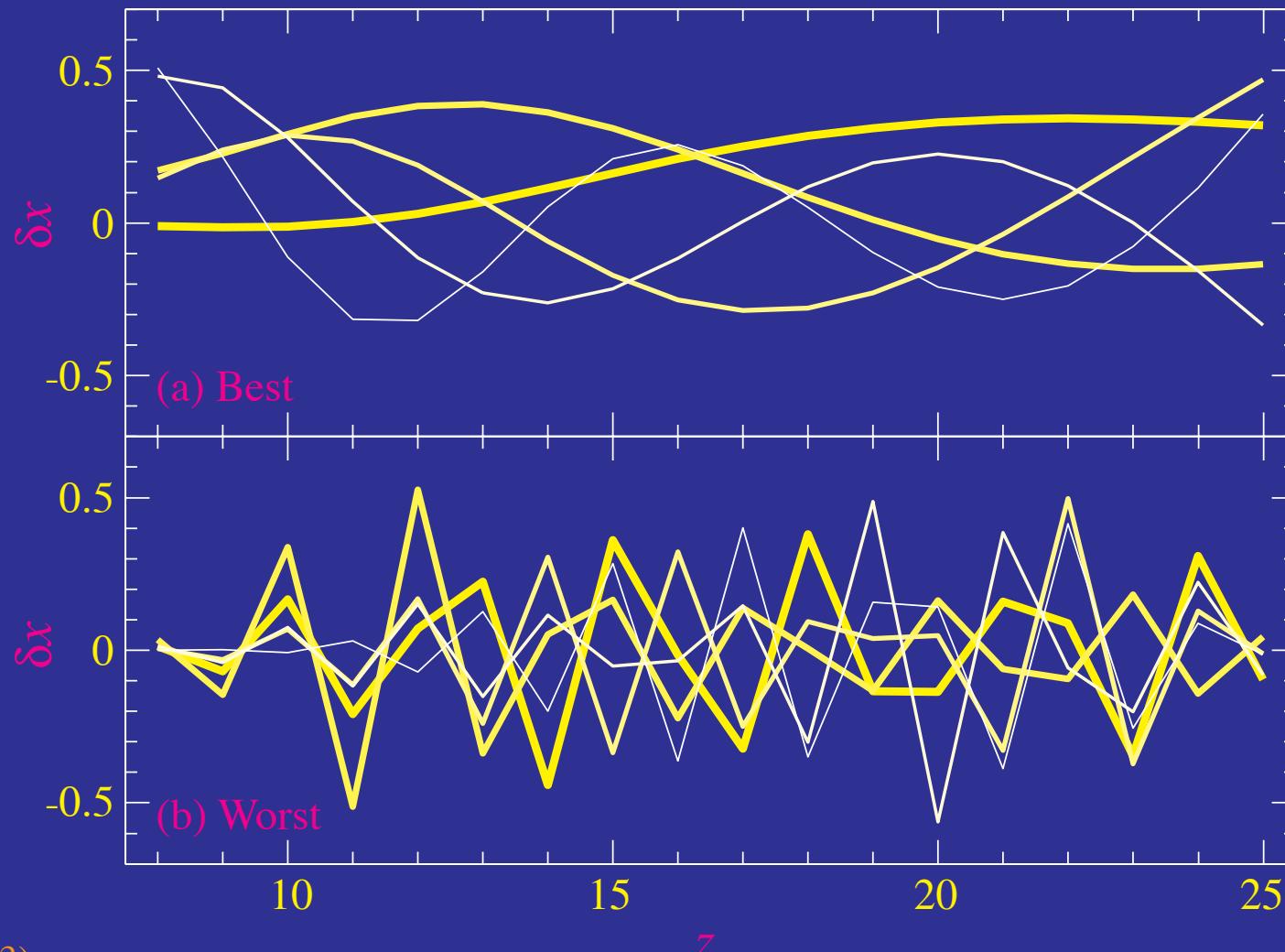
$$\delta C_\ell^{EE} = C_\ell^{EE} \sum_i T_{\ell i} \delta x(z_i) + N_\ell ,$$



# Principal Components

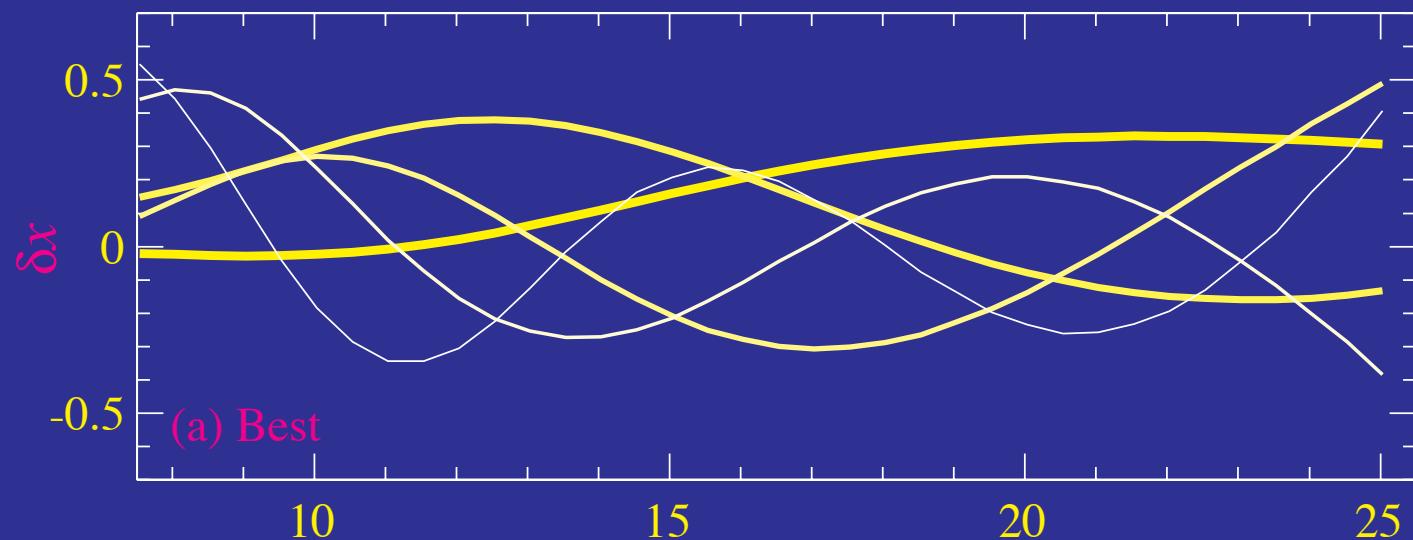
- Eigenvectors of the Fisher Matrix

$$F_{ij} \equiv \sum_{\ell} (\ell + 1/2) T_{\ell i} T_{\ell j} = \sum_{\mu} S_{i\mu} \sigma_{\mu}^{-2} S_{j\mu}$$



# Principal Components

- Low modes **robust** to refinement of **binning**  $\Delta z=0.5$   
(small shift is due to lower  $z_{\min}$ )



# Mode Representation

- Eigenvectors form a complete basis for a new representation

$$m_\mu = \sum_i S_{i\mu} \delta x_i$$

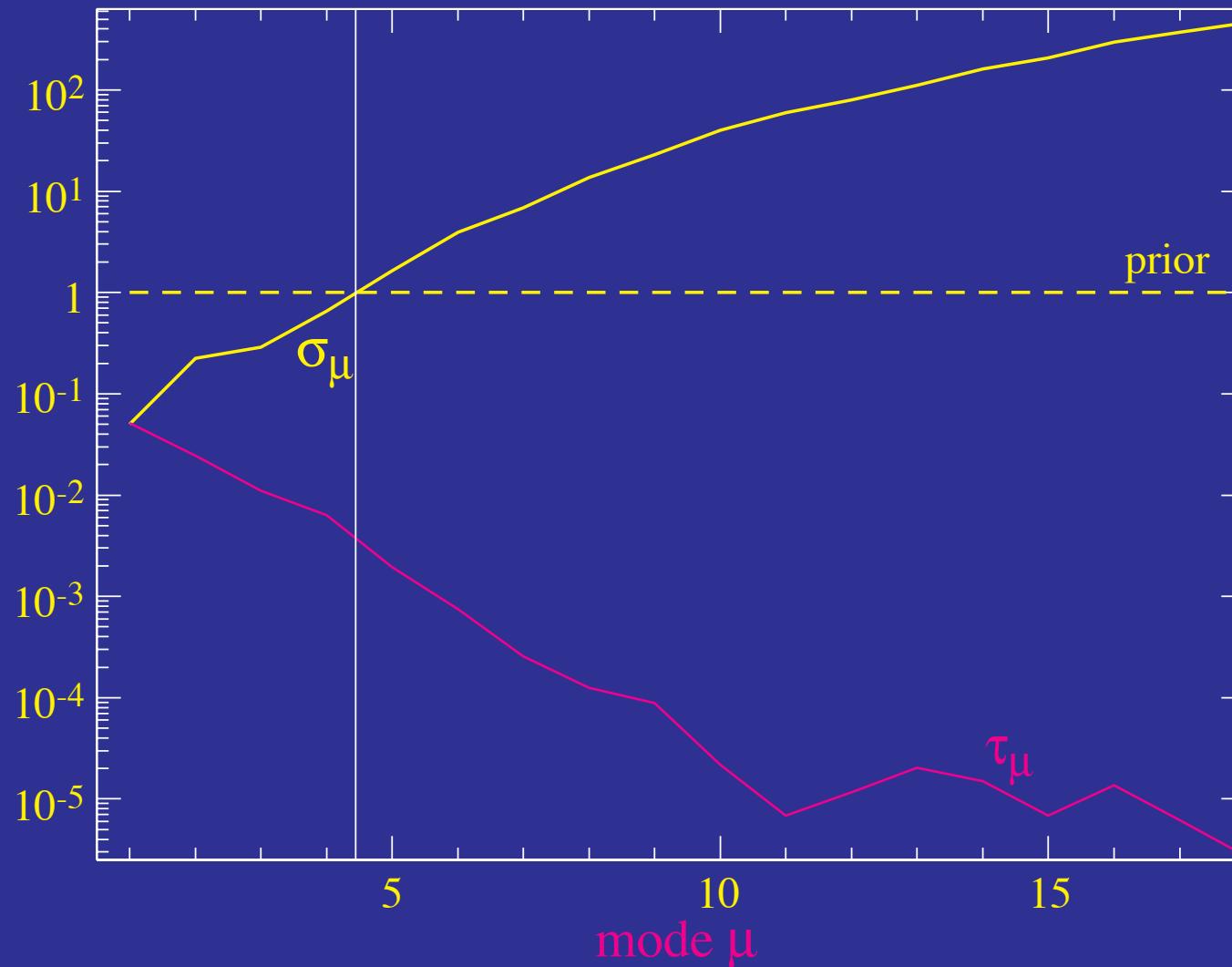
- Yields uncorrelated variance given by the inverse eigenvalue

$$\langle m_\mu m_\nu \rangle = \sigma_\mu^2 \delta_{\mu\nu}$$

- 1st mode: average high  $z$  ionization and low  $\ell$  power
- 2nd mode: average low  $z$  ionization and high  $\ell$  power
- 3rd-5th mode:  $z$  features and ringing in high  $\ell$  power
- $>5$ th mode: compensating ionization fluctuations in neighboring  $z$  and negligible  $\ell$  power

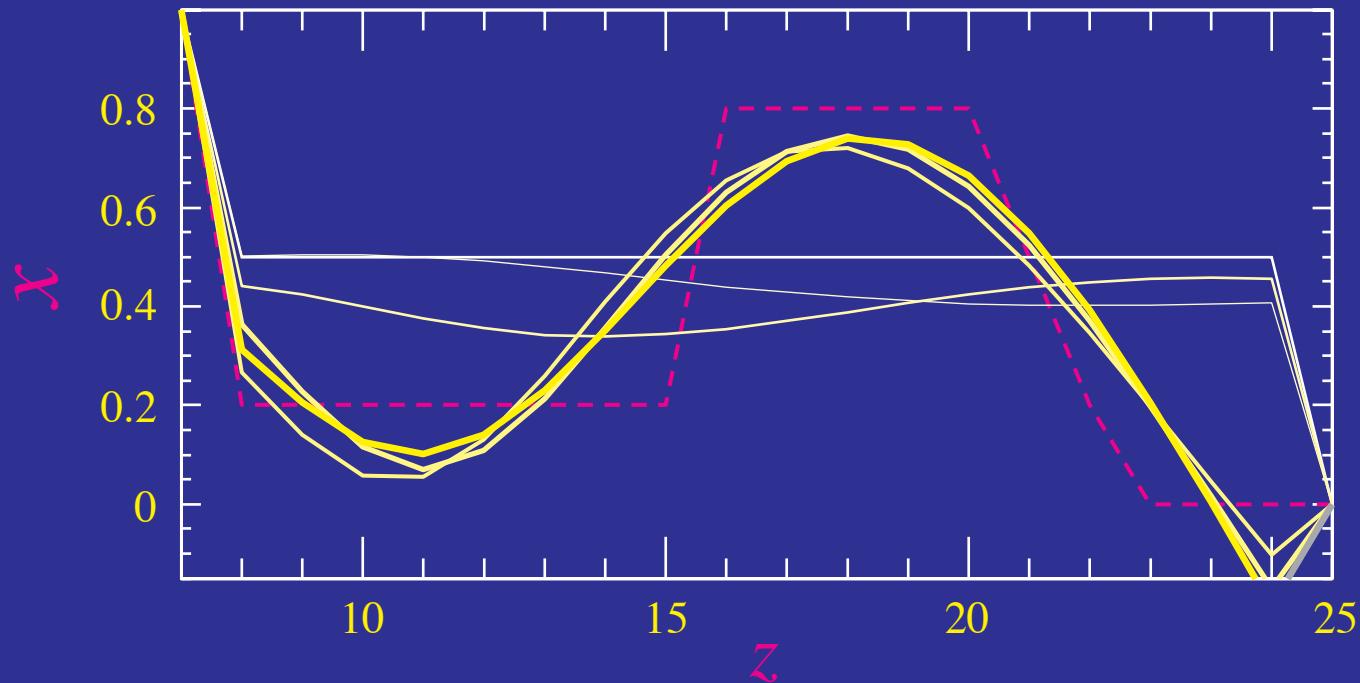
# Capturing the Observables

- First 5 modes have the information content and most of optical depth



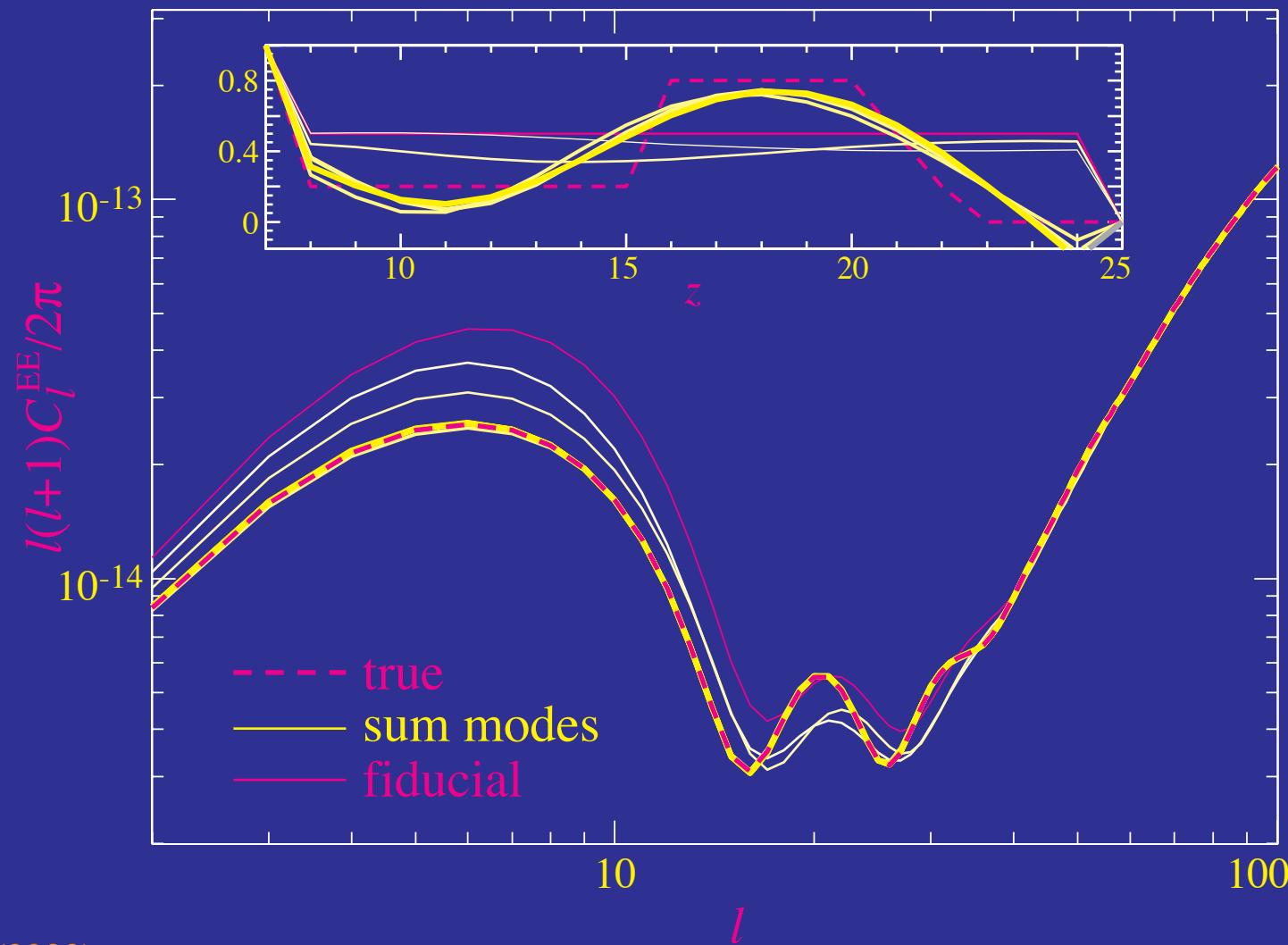
# Representation in Modes

- Truncation at 5 modes leaves a low pass filtered of ionization history
- Ionization fraction allowed to go negative (Boltzmann code has negative sources)



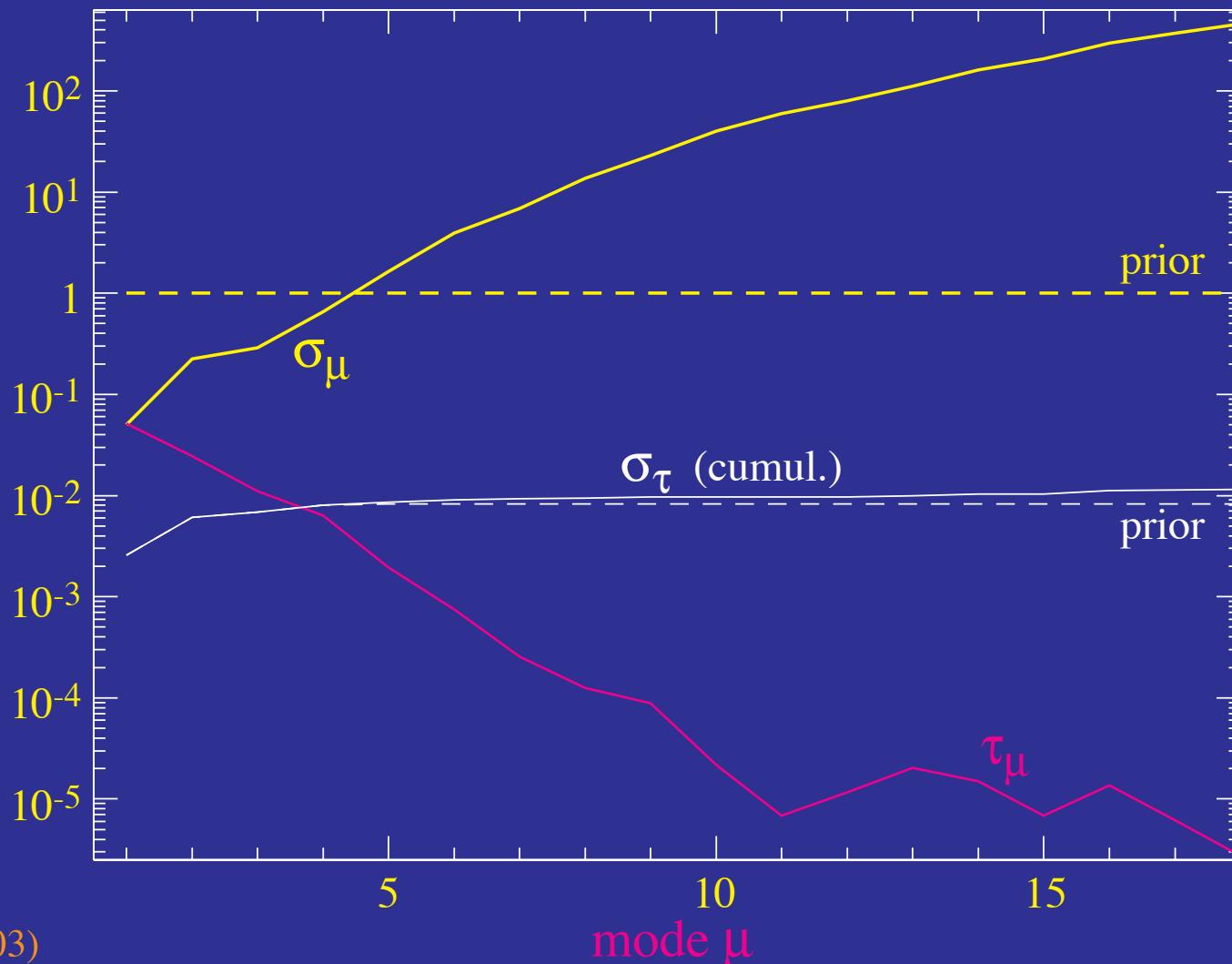
# Representation in Modes

- Reproduces the power spectrum with sum over >3 modes more generally 5 modes suffices: e.g. total  $\tau=0.1375$  vs 0.1377



# Total Optical Depth

- Optical depth measurement unbiased
- Ultimate errors set by cosmic variance here 0.01
- Equivalently 1% measure of initial amplitude, impt for dark energy

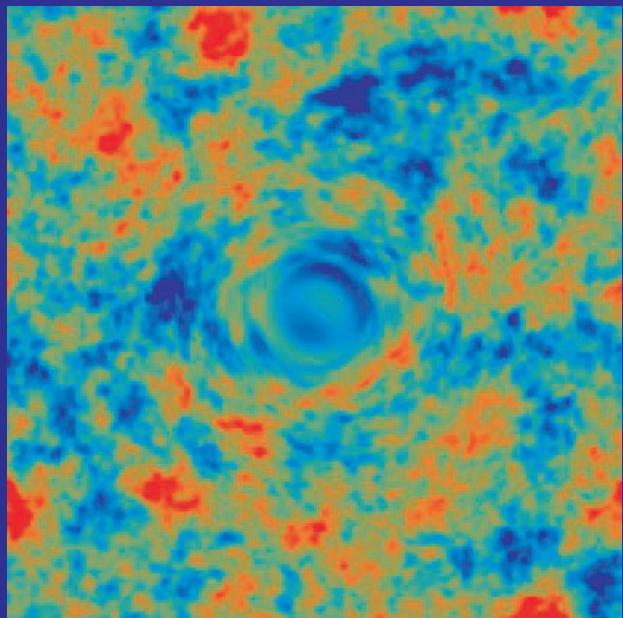




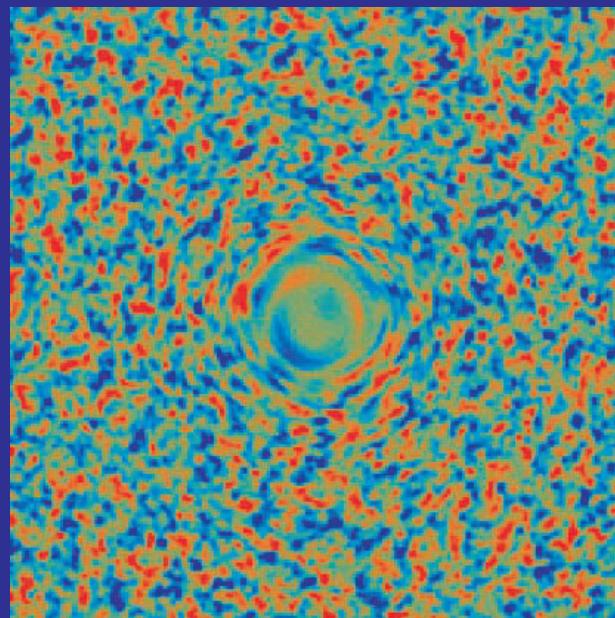
# Gravitational Lensing

# B-Mode Mapping

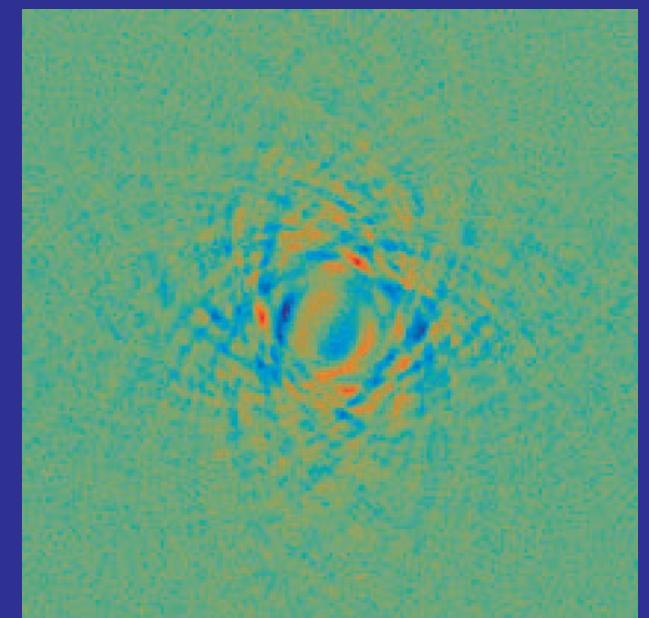
- Lensing warps polarization field and generates B-modes out of E-mode acoustic polarization - hence correlation



Temperature



E-polarization



B-polarization

# Gravitational Lensing

- Lensing is a surface brightness conserving remapping of source to image planes by the gradient of the projected potential

$$\phi(\hat{\mathbf{n}}) = 2 \int_{\eta_*}^{\eta_0} d\eta \frac{(D_* - D)}{D D_*} \Phi(D\hat{\mathbf{n}}, \eta) .$$

such that the fields are remapped as

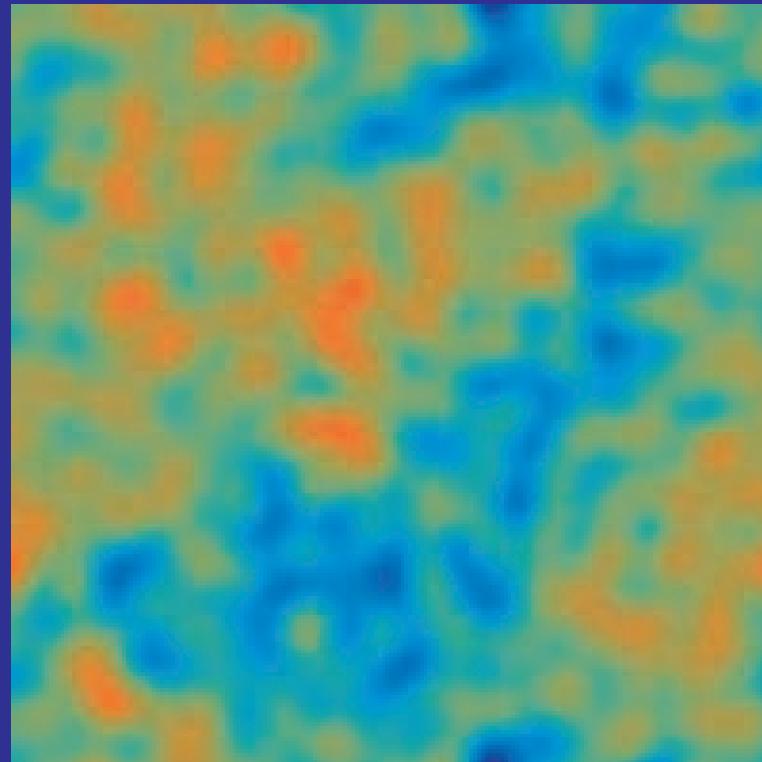
$$x(\hat{\mathbf{n}}) \rightarrow x(\hat{\mathbf{n}} + \nabla\phi) ,$$

where  $x \in \{\Theta, Q, U\}$  temperature and polarization.

- Taylor expansion leads to product of fields and Fourier convolution (or mode coupling) - features in damping tail

# Lensing by a Gaussian Random Field

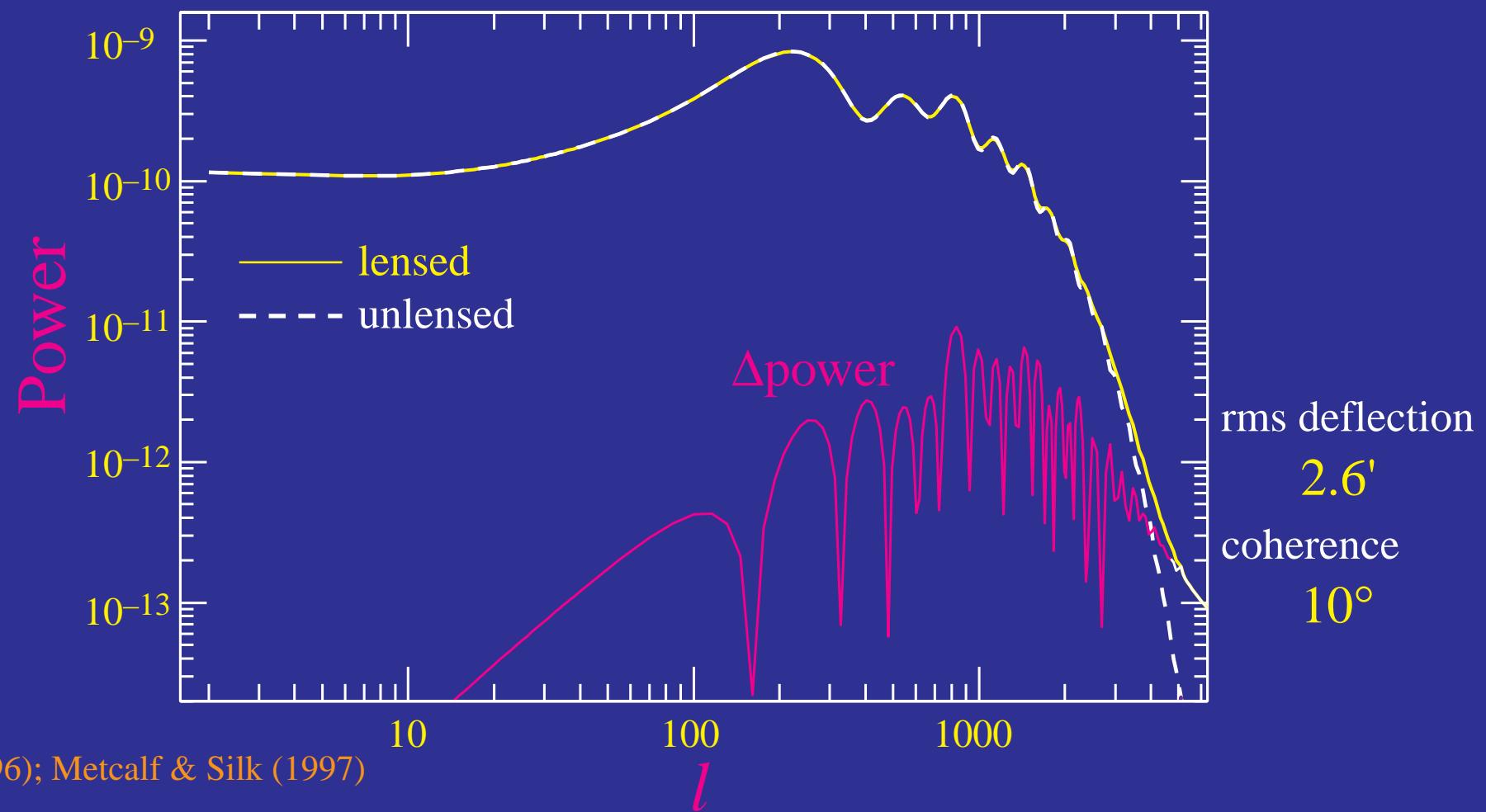
- Mass distribution at large angles and high redshift in the linear regime
- Projected mass distribution (low pass filtered reflecting deflection angles): 1000 sq. deg



rms deflection  
**2.6'**  
deflection coherence  
**10°**

# Lensing in the Power Spectrum

- Lensing smooths the power spectrum with a width  $\Delta l \sim 60$
- Sharp feature of damping tail is best place to see lensing



# Reconstruction from the CMB

- Correlation between Fourier moments reflect lensing potential

$$\kappa = \nabla^2 \phi$$

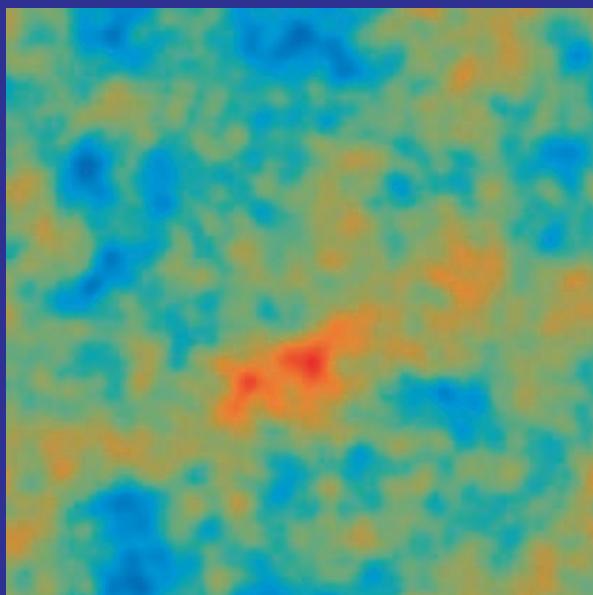
$$\langle x(\mathbf{l})x'(\mathbf{l}') \rangle_{\text{CMB}} = f_\alpha(\mathbf{l}, \mathbf{l}') \phi(\mathbf{l} + \mathbf{l}'),$$

where  $x \in$  temperature, polarization fields and  $f_\alpha$  is a fixed weight that reflects geometry

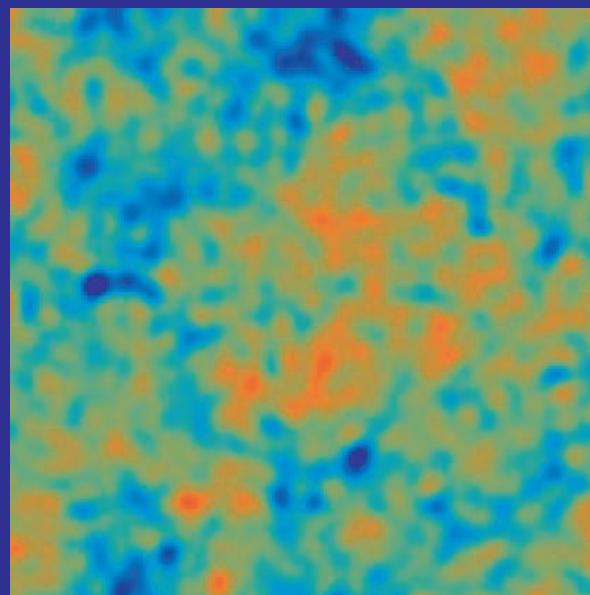
- Each pair forms a noisy estimate of the potential or projected mass
  - just like a pair of galaxy shears
- Fundamentally relies on features in the power spectrum as found in the damping tail

# Ultimate (Cosmic Variance) Limit

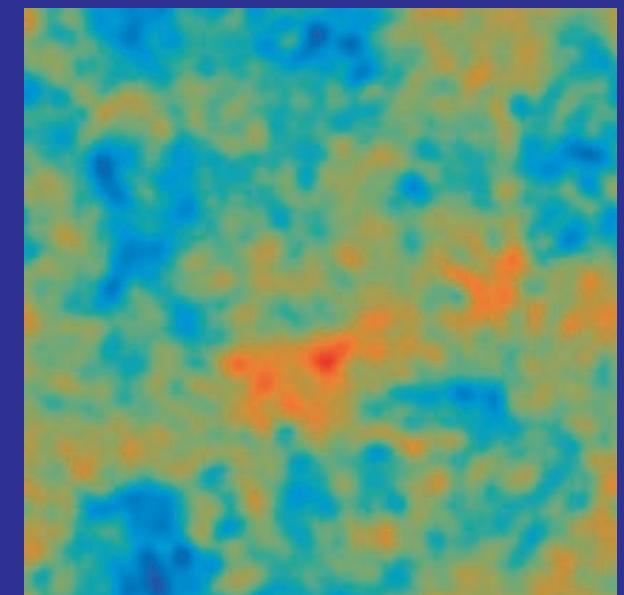
- Cosmic variance of CMB fields sets ultimate limit
- Polarization allows mapping to finer scales ( $\sim 10'$ )



mass



temp. reconstruction

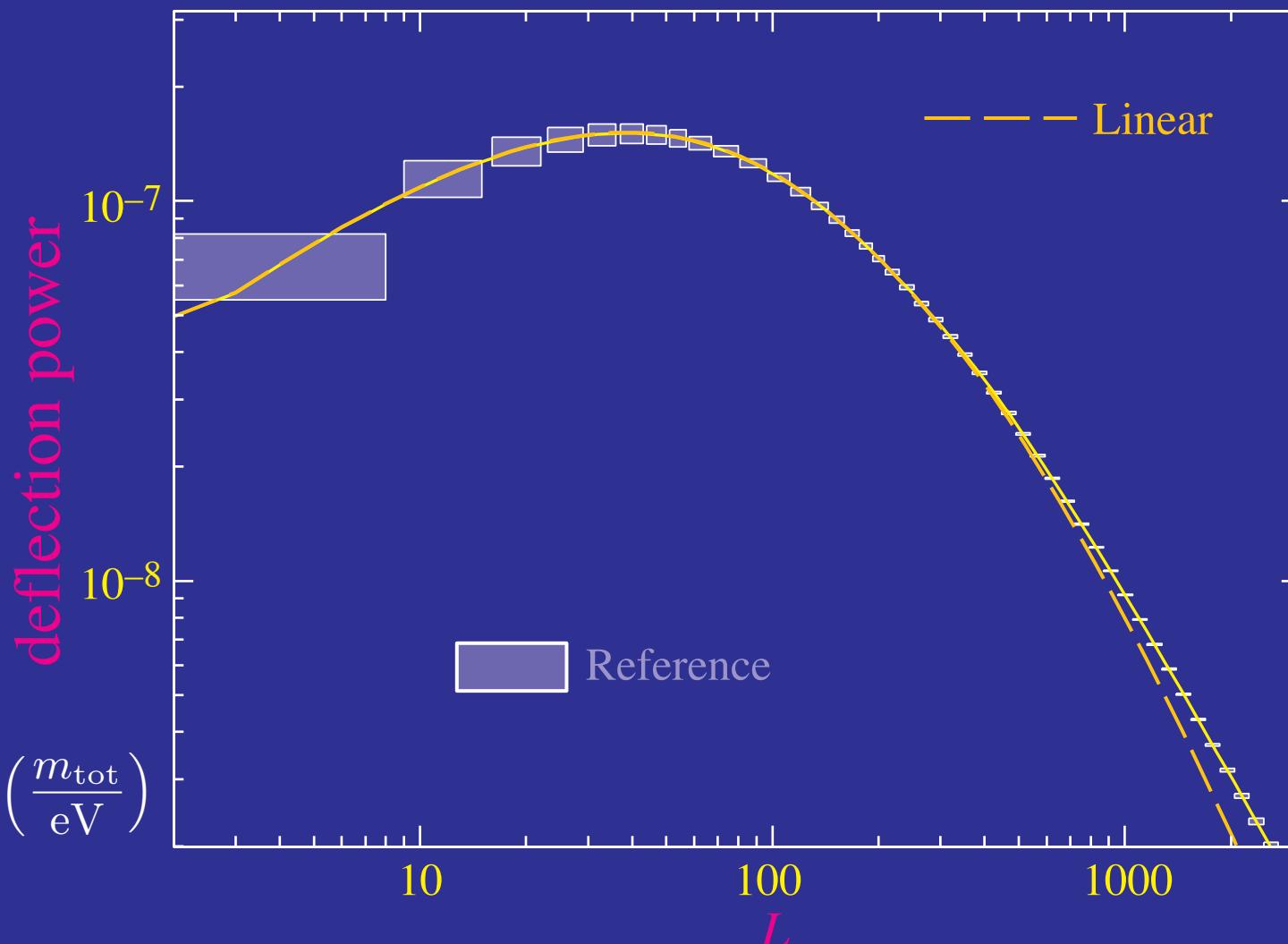


EB pol. reconstruction

100 sq. deg; 4' beam; 1 $\mu$ K-arcmin

# Matter Power Spectrum

- Measuring projected matter power spectrum to cosmic variance limit across whole linear regime  $0.002 < k < 0.2 \text{ } h/\text{Mpc}$

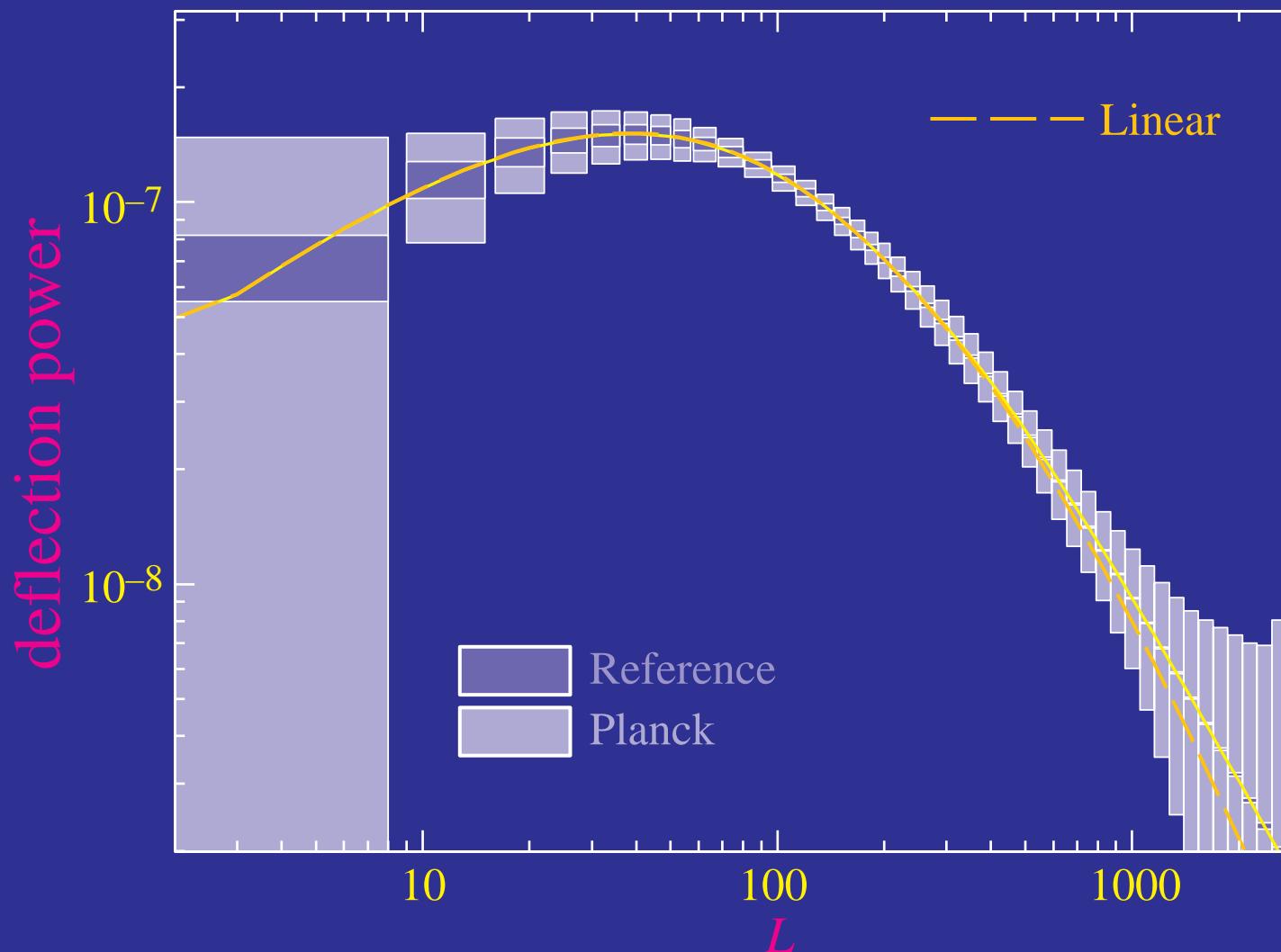


Hu & Okamoto (2001)

$\sigma(w) \sim 0.06$

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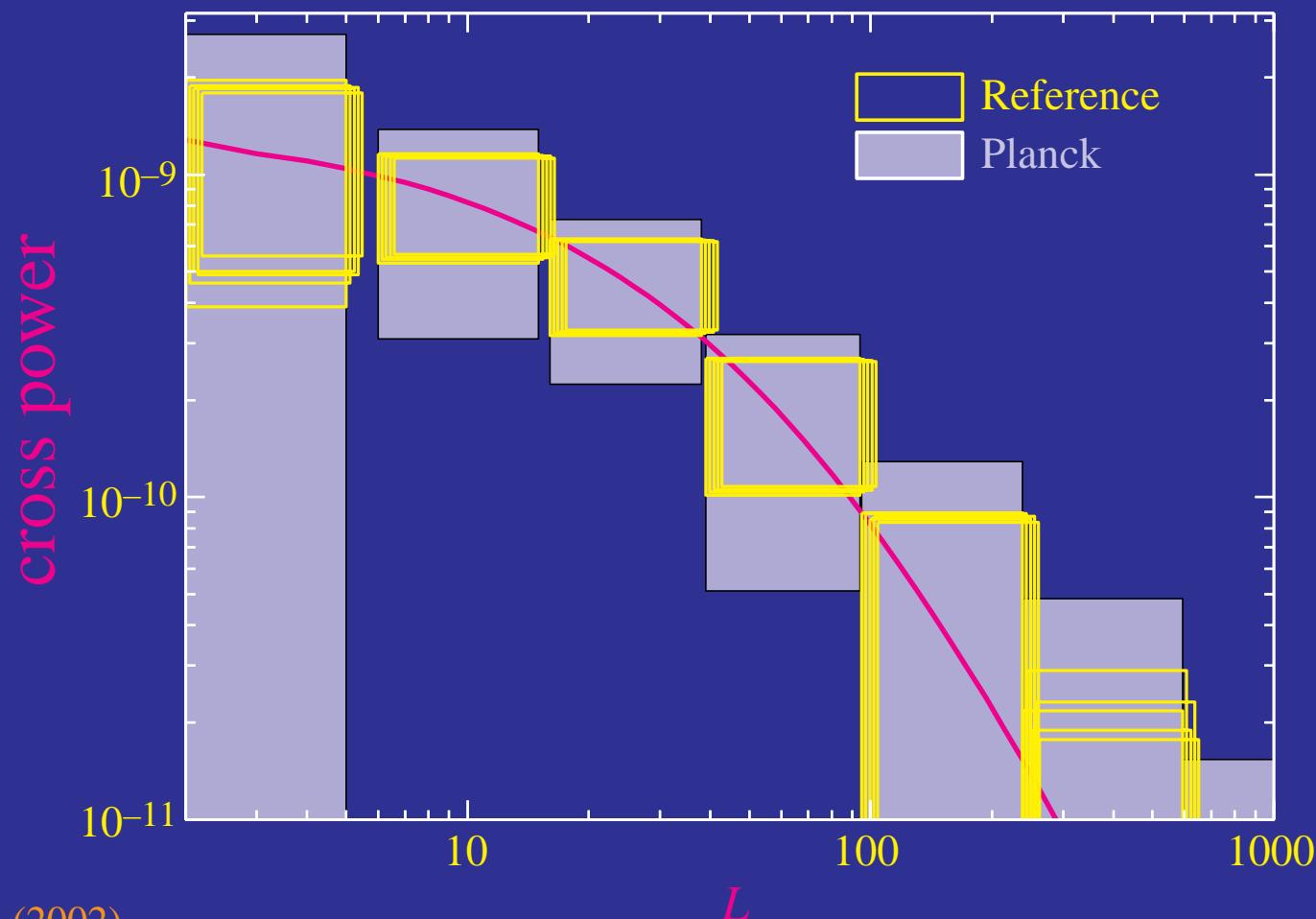


Hu & Okamoto (2001)

$\sigma(w) \sim 0.06; 0.14$

# Cross Correlation with Temperature

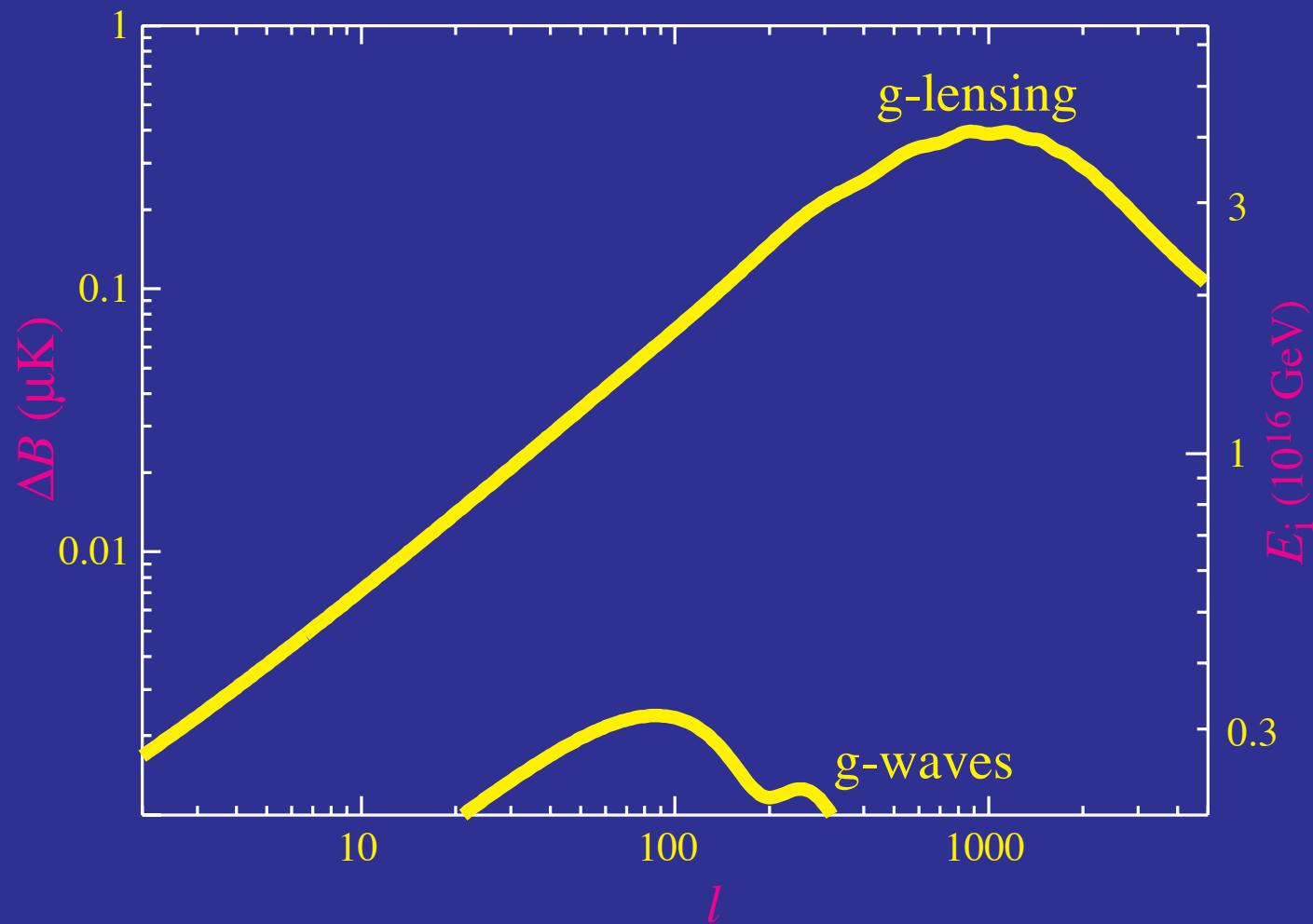
- Any correlation is a direct detection of a smooth energy density component through the ISW effect
- Dark energy smooth >5-6 Gpc scale, test scalar field nature



# Contamination for Gravitational Waves

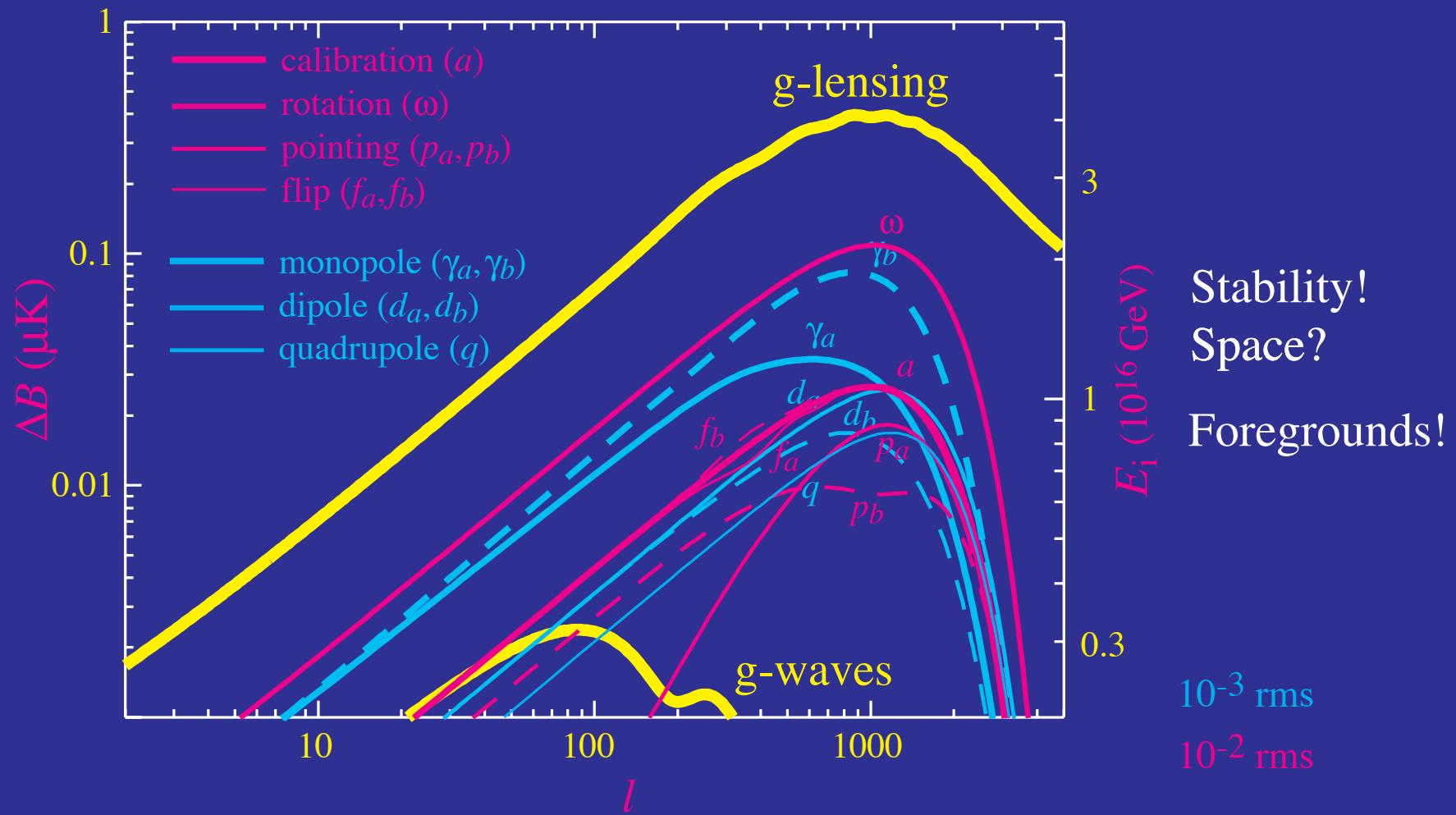
- Gravitational lensing contamination of B-modes from gravitational waves cleaned to  $E_i \sim 0.3 \times 10^{16}$  GeV

Hu & Okamoto (2002) limits by Knox & Song (2002); Cooray, Kedsen, Kamionkowski (2002)



# A (Partial) Catalogue of B Systematics

- Small scale systematics can leak to large scales due to the small, damping scale coherence of T and E modes



# Summary

- Form of reionization bump depends on ionization history, mainly through horizon scale at scattering epoch
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- Modes are a good meeting ground between observations, models
- Best modes can be precisely constrained but even the total optical depth, hence the initial amplitude of fluctuations to 1%
- Gravitational lensing of polarization can pin down the absolute amplitude of structure at intermediate redshifts
- Combination constrains the growth of structure and hence the high redshift properties of the dark energy